

CS 1571 Introduction to AI Lecture 24b

Learning

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Machine Learning

- The field of **machine learning** studies the design of computer programs (agents) capable of learning from past experience or adapting to changes in the environment
- The need for building agents capable of learning is everywhere
 - Predictions in medicine, text classification, speech recognition, image/text retrieval, commercial software
- Machine learning is not only the deduction but induction of rules from examples that facilitate prediction and decision making

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Learning

Learning process:

Learner (a computer program) processes data D representing past experiences and tries to either to develop an appropriate response to future data, or describe in some meaningful way the data seen

Example:

Learner sees a set of patient cases (patient records) with corresponding diagnoses. It can either try:

- to predict the presence of a disease for future patients
- describe the dependencies between diseases, symptoms

Types of learning

- **Supervised learning**
 - Learning mapping between inputs x and desired outputs y
 - Teacher gives me y 's for the learning purposes
- **Unsupervised learning**
 - Learning relations between data components
 - No specific outputs given by a teacher
- **Reinforcement learning**
 - Learning mapping between inputs x and desired outputs y
 - Critic does not give me y 's but instead a signal (reinforcement) of how good my answer was
- **Other types of learning:**
 - explanation-based learning, etc.

Supervised learning

Data: $D = \{d_1, d_2, \dots, d_n\}$ a set of n examples

$$d_i = \langle \mathbf{x}_i, y_i \rangle$$

\mathbf{x}_i is input vector, and y is desired output (given by a teacher)

Objective: learn the mapping $f : X \rightarrow Y$

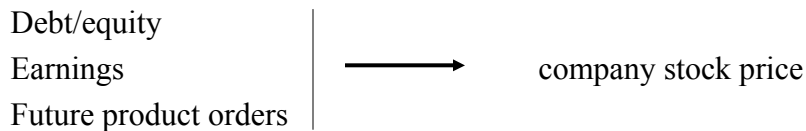
$$\text{s.t. } y_i \approx f(x_i) \quad \text{for all } i = 1, \dots, n$$

Two types of problems:

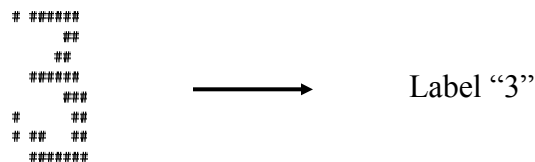
- **Regression:** X discrete or continuous \rightarrow
 Y is **continuous**
- **Classification:** X discrete or continuous \rightarrow
 Y is **discrete**

Supervised learning examples

- **Regression:** Y is **continuous**



- **Classification:** Y is **discrete**



Handwritten digit (array of 0,1s)

Unsupervised learning

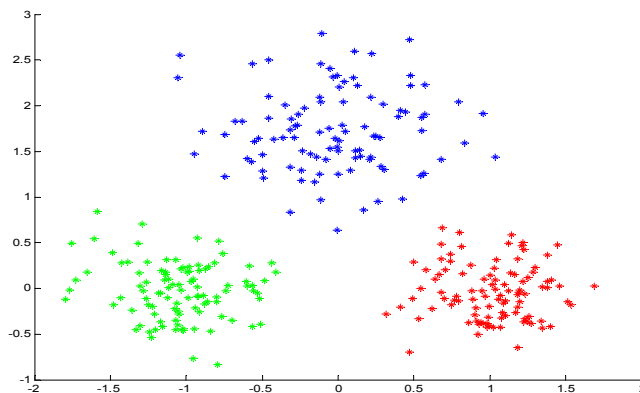
- **Data:** $D = \{d_1, d_2, \dots, d_n\}$
 $d_i = \mathbf{x}_i$ vector of values
No target value (output) y
- **Objective:**
 - learn relations between samples, components of samples

Types of problems:

- **Clustering**
 - Group together “similar” examples, e.g. patient cases
- **Density estimation**
 - Model probabilistically the population of samples

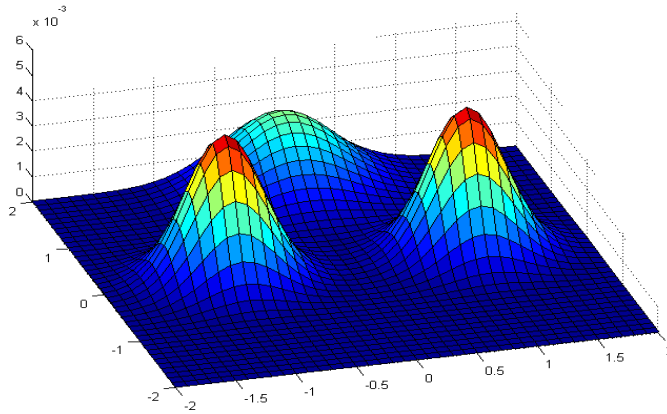
Unsupervised learning example.

- **Density estimation.** We want to build the probability model of a population from which we draw samples $d_i = \mathbf{x}_i$



Unsupervised learning. Density estimation

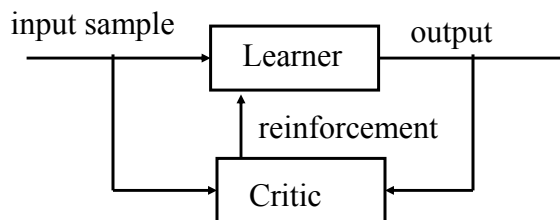
- A probability density of a point in the two dimensional space
 - Model used here: Mixture of Gaussians



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Reinforcement learning

- We want to learn: $f : X \rightarrow Y$
- We see samples of x but not y
- Instead of y we get a feedback (reinforcement) from a **critic** about how good our output was

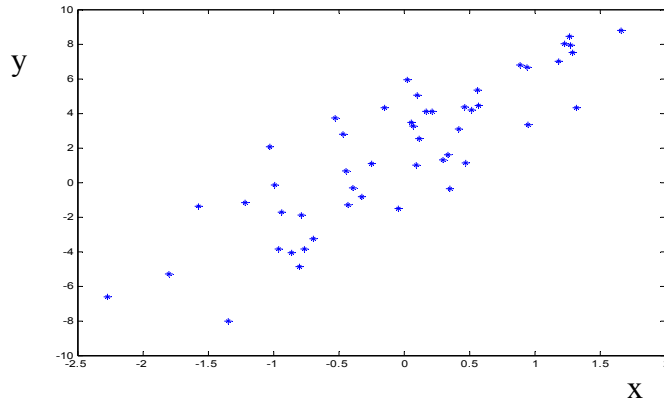


- The goal is to select output that leads to the best reinforcement

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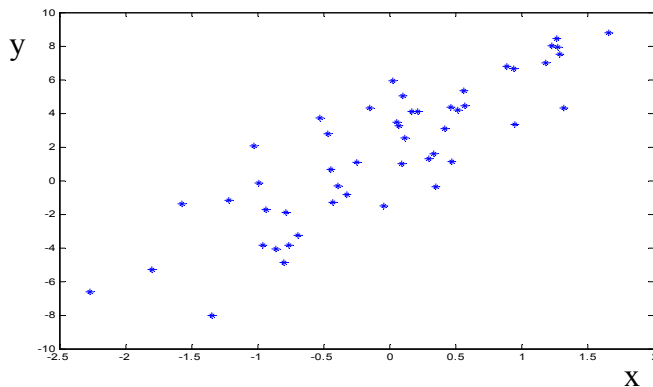
- Assume we see examples of pairs (\mathbf{x}, y) and we want to learn the mapping $f : X \rightarrow Y$ to predict future y s for values of \mathbf{x}
- We get the data what should we do?



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Learning bias

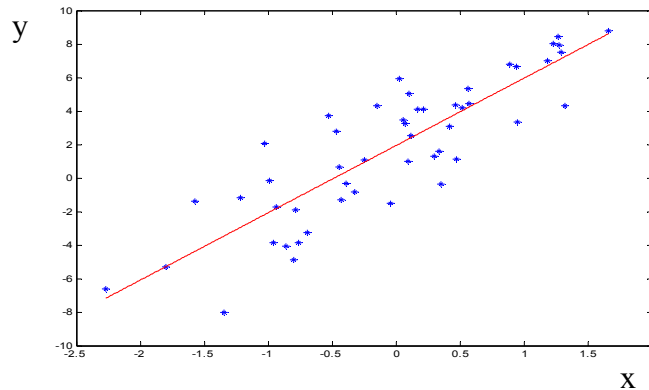
- **Problem:** many possible functions $f : X \rightarrow Y$ exists for representing the mapping between \mathbf{x} and y
- Which one to choose? Many examples still unseen!



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Learning bias

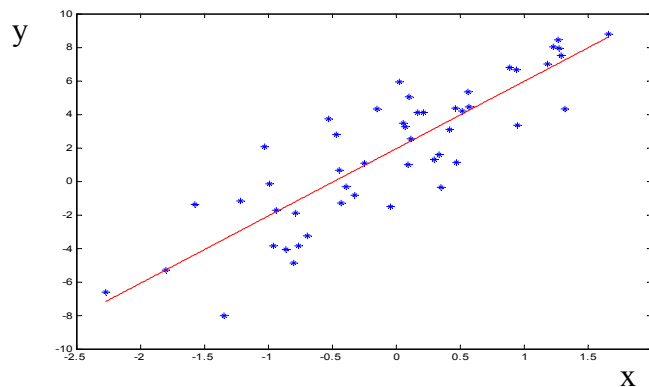
- Problem is easier when we make an assumption about the model, say, $f(x) = ax + b + \varepsilon$
 $\varepsilon = N(0, \sigma)$ - random (normally distributed) noise
- Restriction to a linear model is an example of the learning bias



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Learning bias

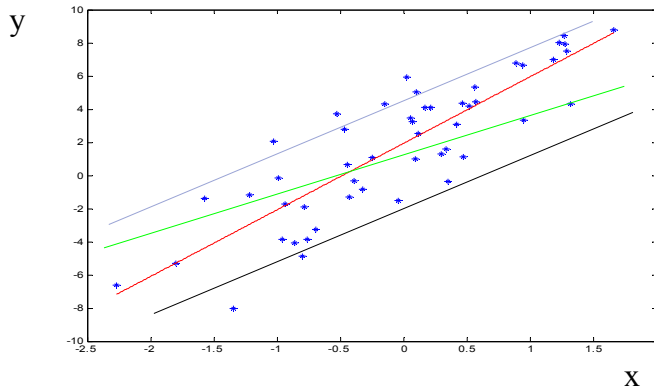
- **Bias** provides the learner with some basis for choosing among possible representations of the function.
- **Forms of bias:** constraints, restrictions, model preferences
- **Important:** There is no learning without a bias!



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Learning bias

- Choosing a parametric model or a set of models is not enough
Still too many functions $f(x) = ax + b + \varepsilon$ $\varepsilon = N(0, \sigma)$
 - One for every pair of parameters a, b



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Fitting the data to the model

- We are interested in finding the **best set** of model parameters
- Objective:** Find the set of parameters that:
- reduce the misfit between what model suggests and what data say
 - Or, (in other words) that explain the data the best

Error function:

Measure of misfit between the data and the model

- Examples of error functions:

- Mean square error

$$\frac{1}{n} \sum_{i=1}^n (y_i - f(x_i))^2$$

- Misclassification error

Average # of misclassified cases $y_i \neq f(x_i)$

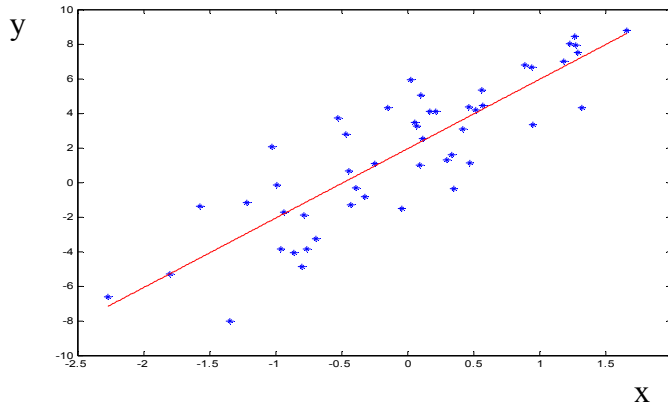
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Fitting the data to the model

- **Linear regression**

- Least squares fit with the linear model

- minimizes
$$\frac{1}{n} \sum_{i=1}^n (y_i - f(x_i))^2$$



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Typical learning

Three basic steps:

- **Select a model** or a set of models (with parameters)

E.g. $y = ax + b + \varepsilon$ $\varepsilon = N(0, \sigma)$

- **Select the error function** to be optimized

E.g.
$$\frac{1}{n} \sum_{i=1}^n (y_i - f(x_i))^2$$

- **Find the set of parameters optimizing the error function**

- The model and parameters with the smallest error represent the best fit of the model to the data

But there are problems one must be careful about ...

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