CS 1571 Introduction to AI
Lecture 19

Planning

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Planning

Planning problem:

- find a sequence of actions that achieves some goal
- an instance of a search problem
- the state description is typically very complex and relies on a logic-based representation

Methods for modeling and solving a planning problem:

- State space search
- Situation calculus based on FOL
- STRIPS – state space search algorithm
- Partial-order planning algorithms

Planning problems

Properties of many (real-world) planning problems:

- The description of the state of the world is very complex
- Many possible actions to apply in any step
- Actions are typically local
  - – they affect only a small portion of a state description
- Goals are defined as conditions referring only to a small portion of state
- Plans consists of a large number of actions

The state space search and situation calculus frameworks may be

- too cumbersome and inefficient to represent and solve the planning problems

STRIPS planner

Defines a **restricted representation language** as compared to the situation calculus

Advantage: leads to more efficient planning algorithms.

- State-space search with structured representations of states, actions and goals
- Action representation avoids the frame problem

STRIPS planning problem:

- much like a standard search problem

STRIPS planner

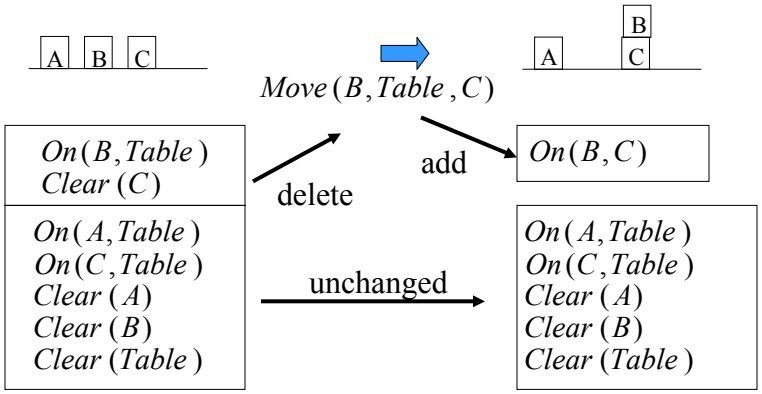
- **States:**
  - conjunction of literals, e.g. *On(A,B), On(B,Table), Clear(A)*
  - represent facts that are true at a specific point in time
- **Actions (operators):**
  - **Action:** *Move (x,y,z)*
  - **Preconditions:** conjunctions of literals with variables

    On(x,y), Clear(x), Clear(z)
  - **Effects.** Two lists:
    - **Add list:** *On(x,z), Clear(y)*
    - **Delete list:** *On(x,y), Clear(z)*
    - Everything else remains untouched (is preserved)

STRIPS planning

Operator: *Move (x,y,z)*

- **Preconditions:** *On(x,y), Clear(x), Clear(z)*
- **Add list:** *On(x,z), Clear(y)*
- **Delete list:** *On(x,y), Clear(z)*



STRIPS planning

Initial state:

- Conjunction of literals that are true

Goals in STRIPS:

- A goal is a partially specified state
- Is defined by a conjunction of ground literals
  - No variables allowed in the description of the goal

Example:

$On(A,B) \wedge On(B,C)$

Search in STRIPS

Objective:

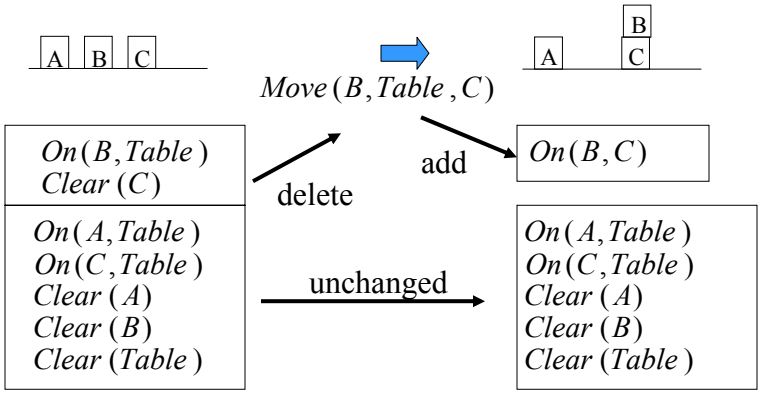
Find a sequence of operators (a plan) from the initial state to the state satisfying the goal

Two approaches to build a plan:

- **Forward state space search (goal progression)**
  - Start from what is known in the initial state and apply operators in the order they are applied
- **Backward state space search (goal regression)**
  - Start from the description of the goal and identify actions that help to reach the goal

Forward search (goal progression)

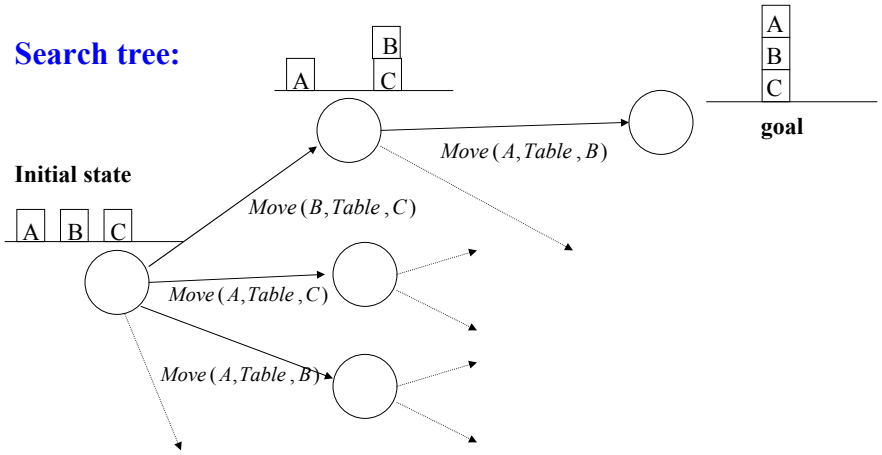
- **Idea:** Given a state *s*
  - Unify the preconditions of some operator *a* with *s*
  - Add and delete sentences from the add and delete list of an operator *a* from *s* to get a new state



Forward search (goal progression)

- Use operators to generate new states to search
- Check new states whether they satisfy the goal

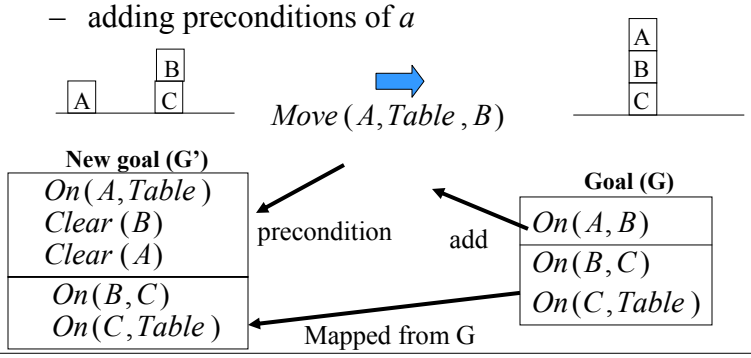
Search tree:



Backward search (goal regression)

Idea: Given a goal G

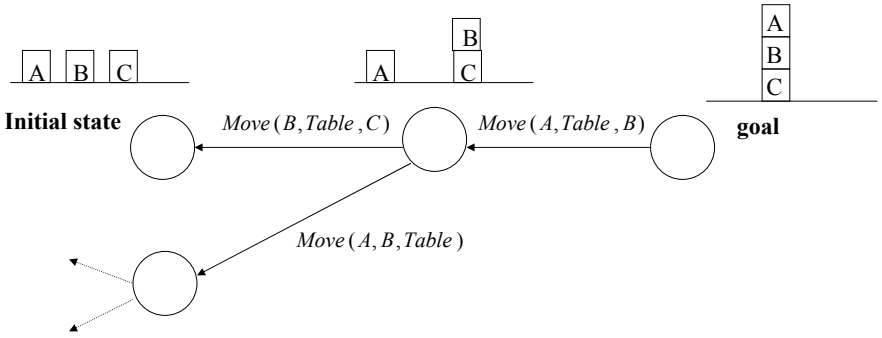
- Unify the add list of some operator a with a subset of G
- If the delete list of a does not remove elements of G, then the goal regresses to a new goal G' that is obtained from G by:
  - deleting add list of a
  - adding preconditions of a



Backward search (goal regression)

- Use operators to generate new goals
- Check whether the initial state satisfies the goal

Search tree:



State-space search

- **Forward and backward state-space planning approaches:**
  - Work with strictly linear sequences of actions

- **Disadvantages:**
  - They cannot take advantage of the **problem decompositions** in which the goal we want to reach consists of a set of independent or nearly independent sub-goals
  - Action sequences cannot be **built from the middle**
  - No mechanism to represent **least commitment** in terms of the action ordering

Divide and conquer

- **Divide and conquer strategy**:
  - divide the problem to a set of smaller sub-problems,
  - solve each sub-problem independently
  - combine the results to form the solution

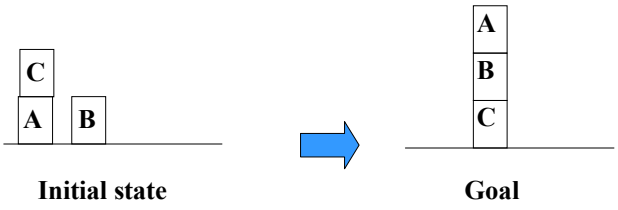
In planning we would like to satisfy a set of goals

- **Divide and conquer in planning:**
  - Divide the planning goals along individual goals
  - Solve (find a plan for) each of them independently
  - Combine the plan solutions in the resulting plan

- Is it always safe to use divide and conquer?
  - No. There can be interacting goals.

Sussman's anomaly.

- An example from the blocks world in which the divide and conquer fails due to interacting goals

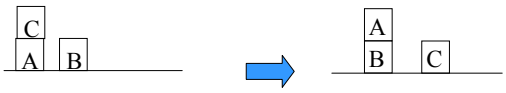


Initial state **Goal**

$On(A,B)$
$On(B,C)$

Sussman's anomaly

1. Assume we want to satisfy $On(A,B)$ first



Initial state

But now we cannot satisfy $On(B,C)$ without undoing $On(A,B)$

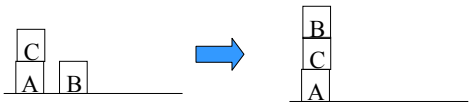
Sussman's anomaly

1. Assume we want to satisfy $On(A,B)$ first

Initial state

But now we cannot satisfy $On(B,C)$ without undoing $On(A,B)$

2. Assume we want to satisfy $On(B,C)$ first.



Initial state

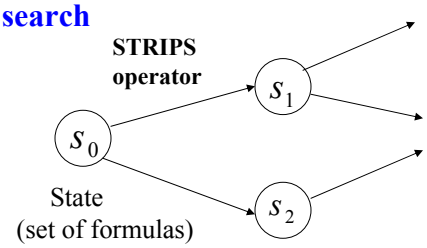
But now we cannot satisfy $On(A,B)$ without undoing $On(B,C)$

State space vs. plan space search

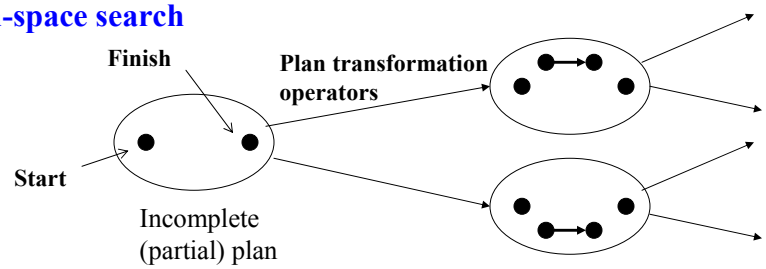
- An alternative to planning algorithms that search states (configurations of world)
- **Plan:** Defines a sequence of operators to be performed
- **Partial plan:**
  - plan that is not complete
    - Some plan steps are missing
  - some orderings of operators are not finalized
    - Only relative order is given
- **Benefits of working with partial plans:**
  - We do not have to build the sequence from the initial state or the goal
  - We do not have to commit to a specific action sequence
  - We can work on sub-goals individually (divide and conquer)

State-space vs. plan-space search

State-space search



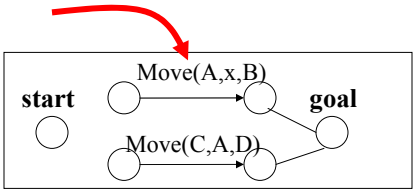
Plan-space search



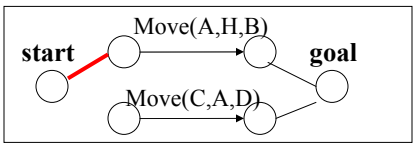
Plan transformation operators

Examples of :

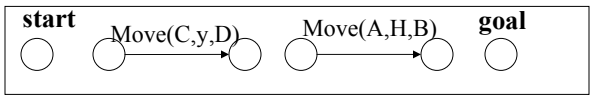
- **Add an operator to a plan so that it satisfies some open condition**



- **Add link (+ instantiate)**



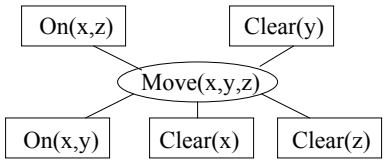
- **Order (reorder) operators**



Partial-order planners (POP)

- also called **Non-linear planners**
- Use STRIPS operators

Graphical representation of an **operator Move(x,y,z)**



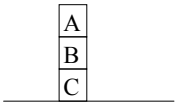
add list

preconditions

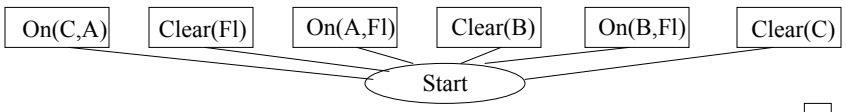
Delete list is not shown !!!

Illustration of a POP on the Sussman's anomaly case

Partial order planning. Start and finish.

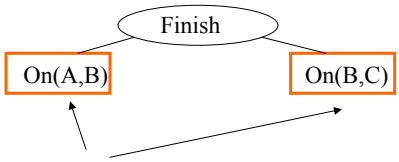


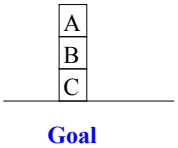
Goal



Start

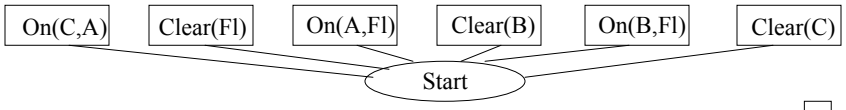
Partial order planning. Start and finish.



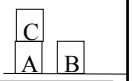


Goal

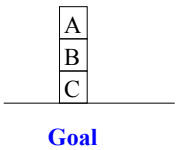
Open conditions: conditions yet to be satisfied



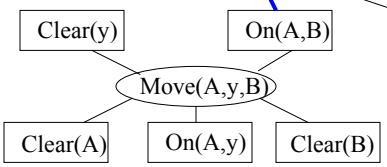
Start



Partial order planning. Add operator.

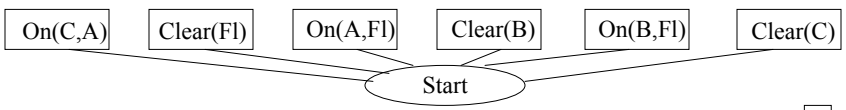


Goal

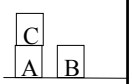


We want to satisfy **an open condition**

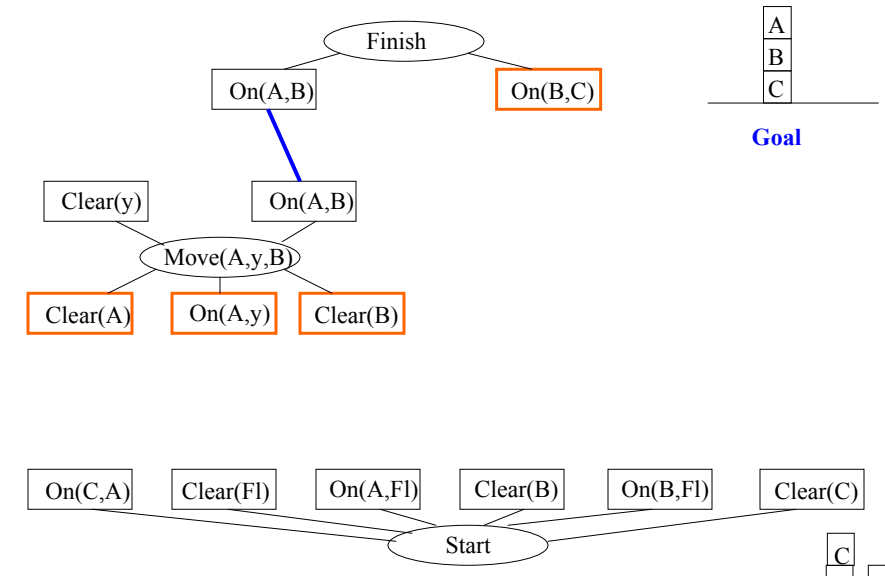
Always select an operator that helps to satisfy one of the open conditions



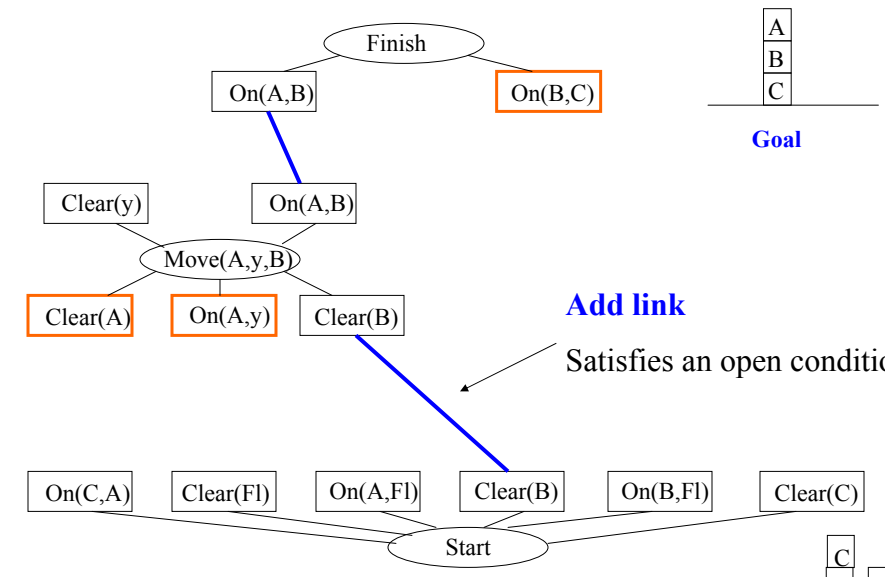
Start



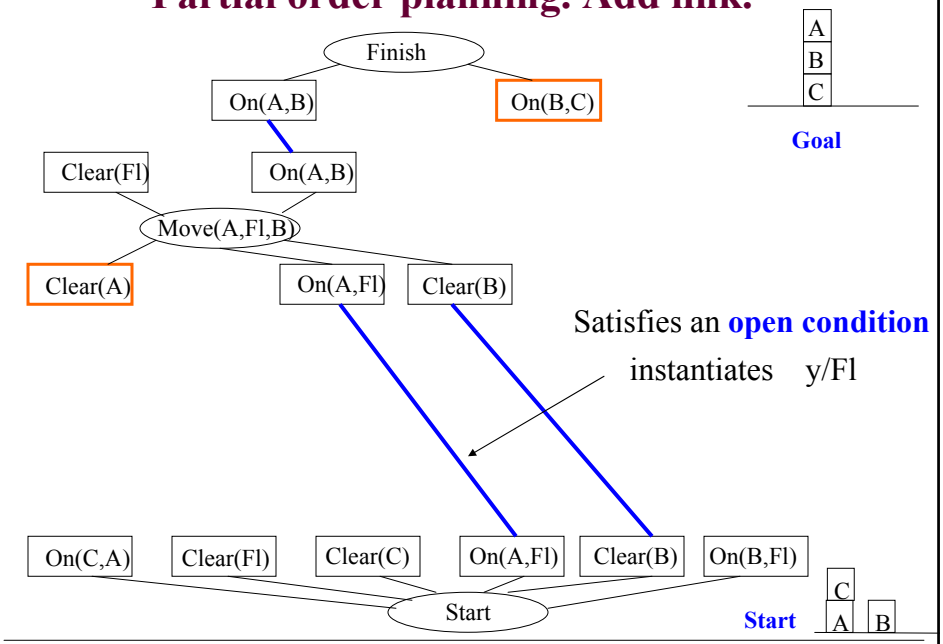
Partial order planning. Add link.



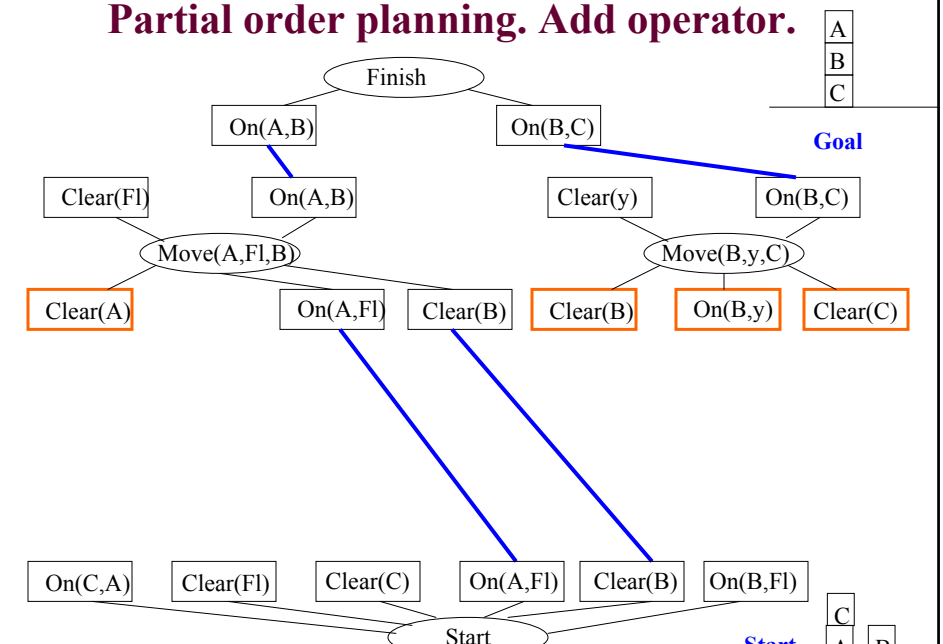
Partial order planning. Add link.



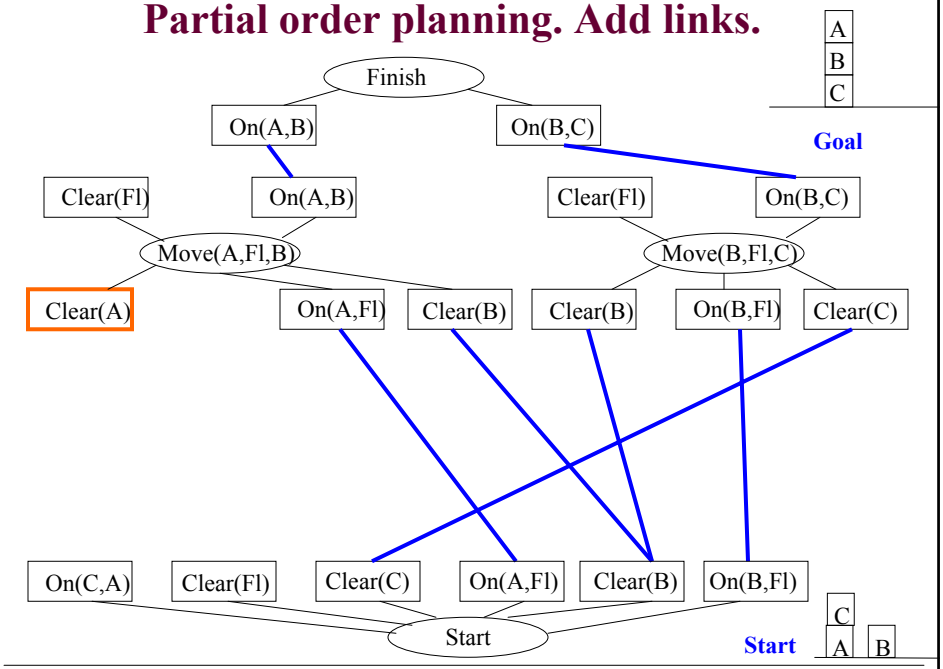
Partial order planning. Add link.



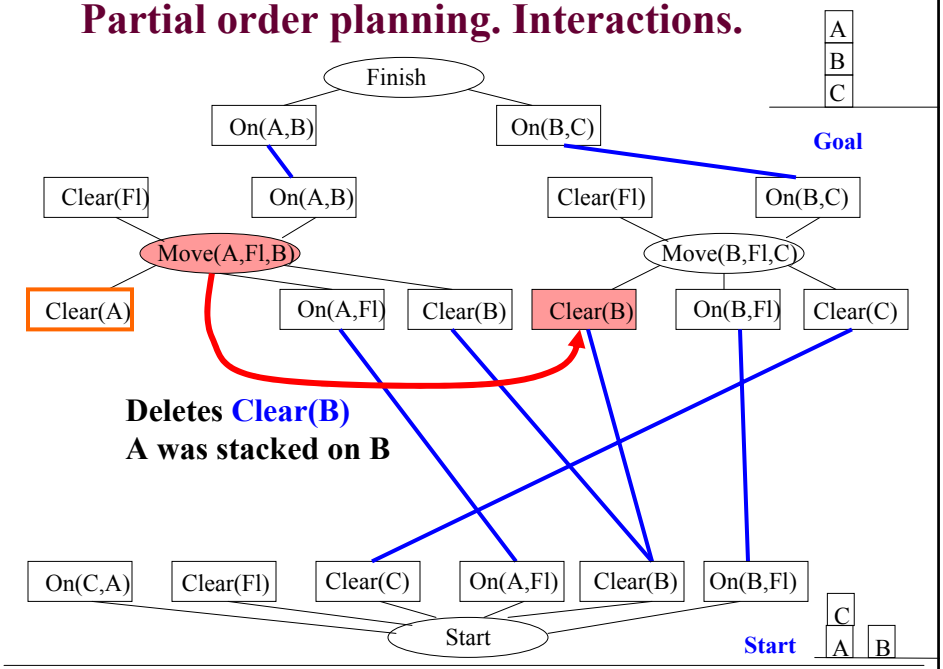
Partial order planning. Add operator.



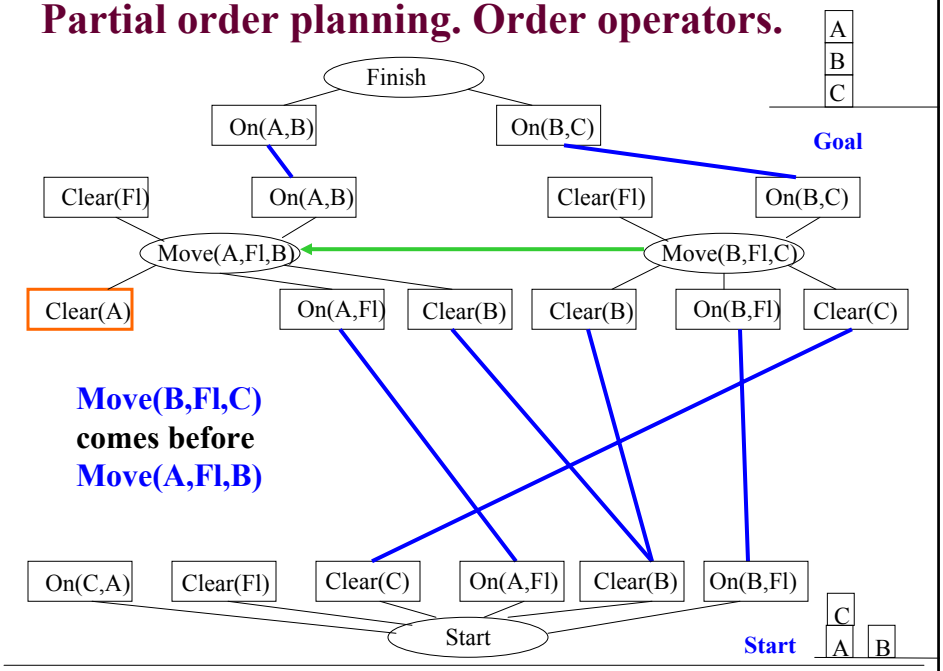
Partial order planning. Add links.



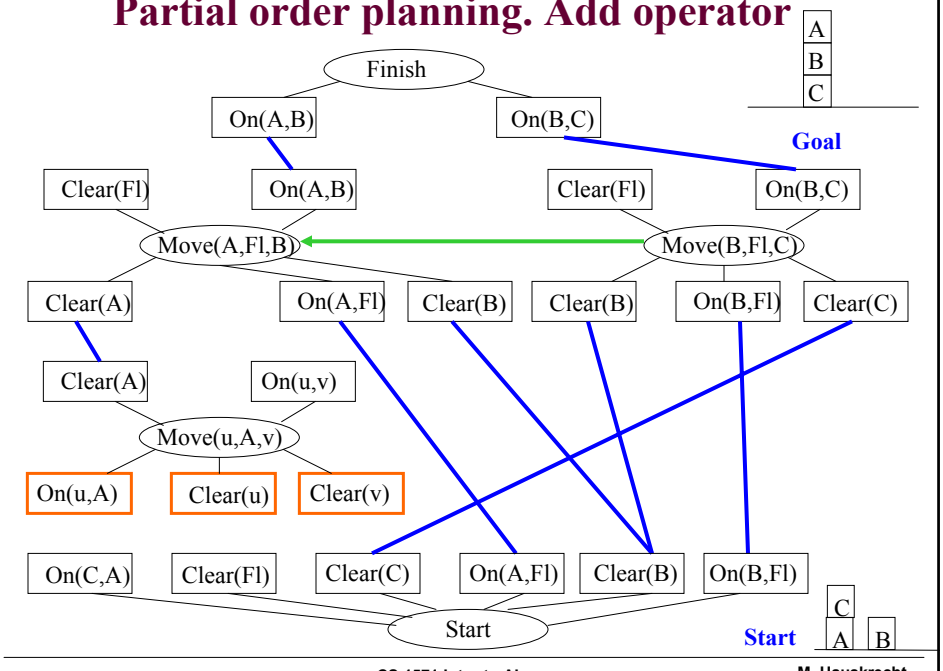
Partial order planning. Interactions.



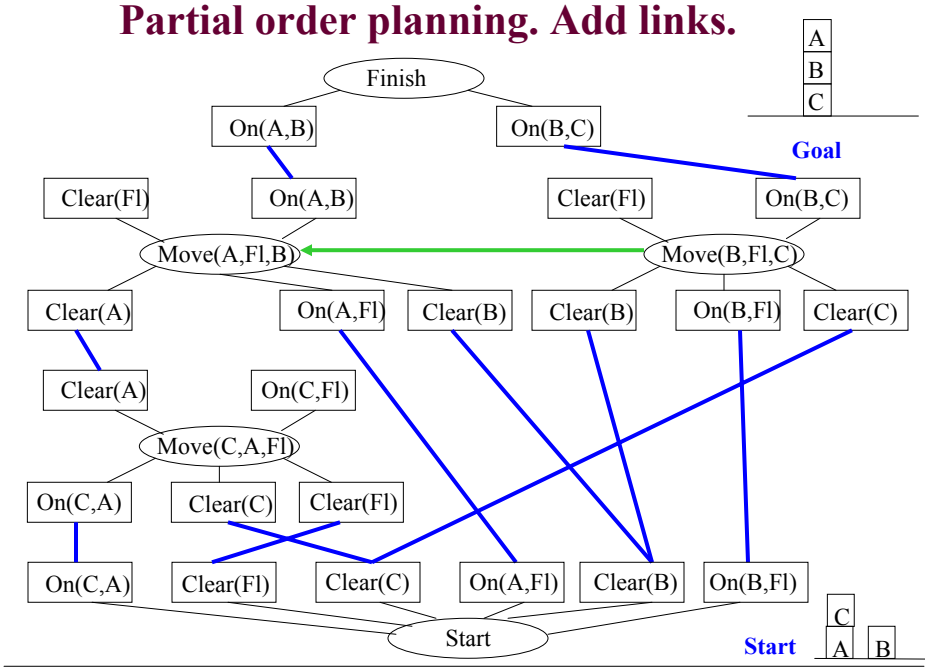
Partial order planning. Order operators.



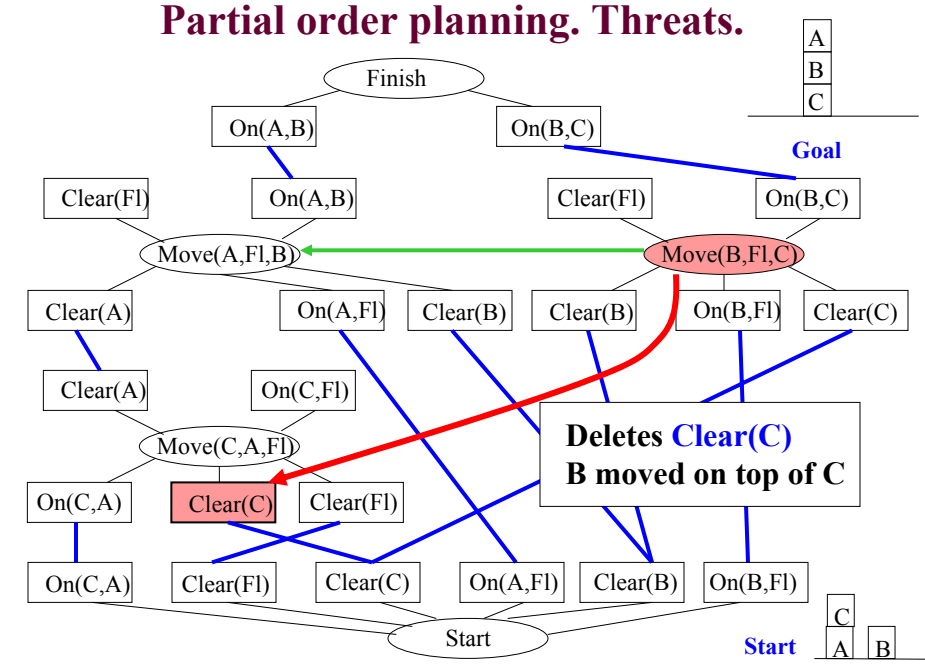
Partial order planning. Add operator



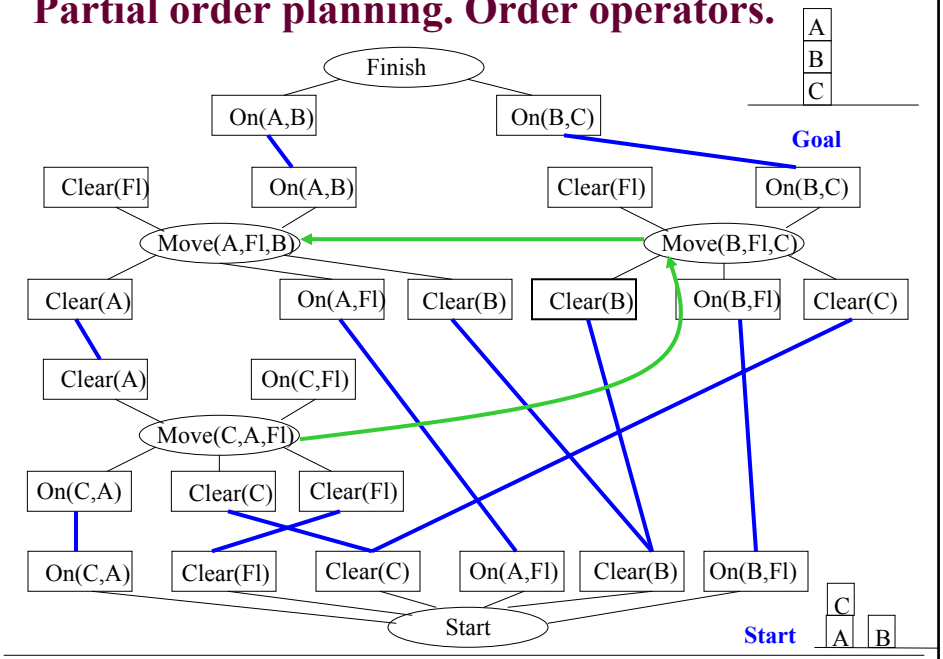
Partial order planning. Add links.



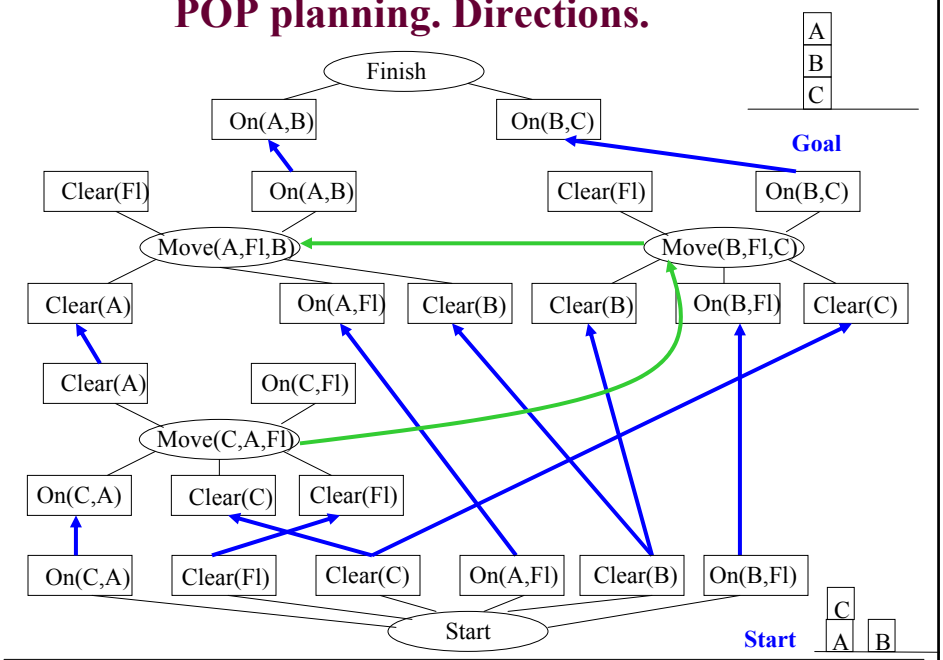
Partial order planning. Threats.



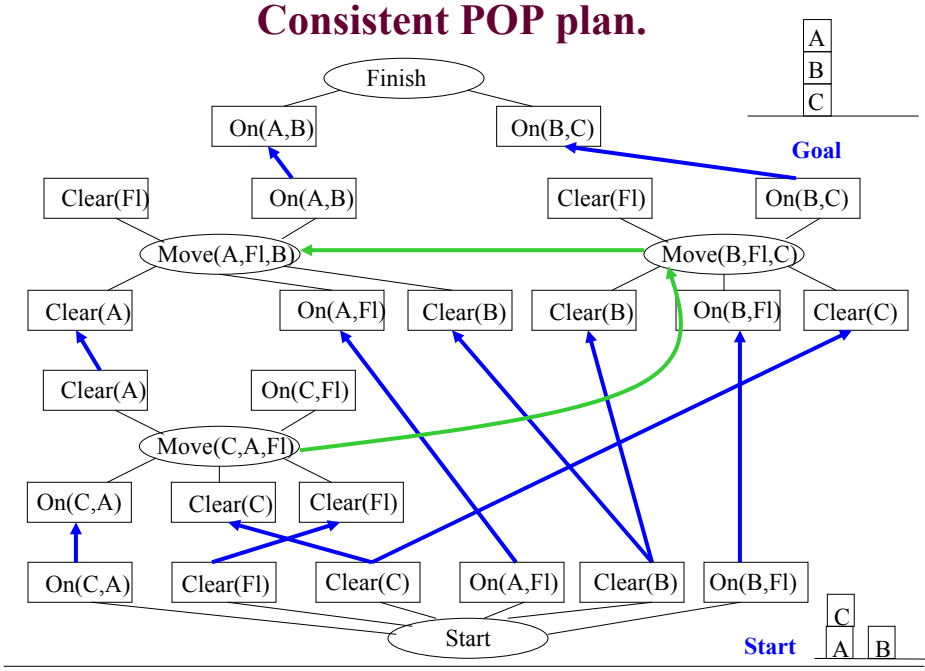
Partial order planning. Order operators.



POP planning. Directions.

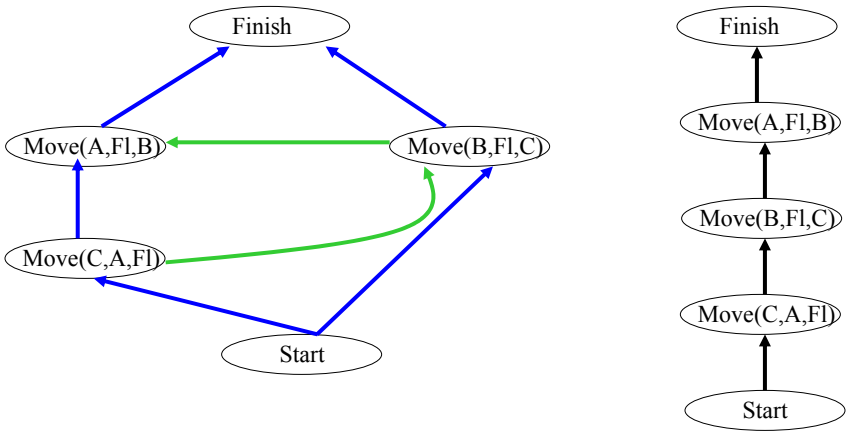


Consistent POP plan.



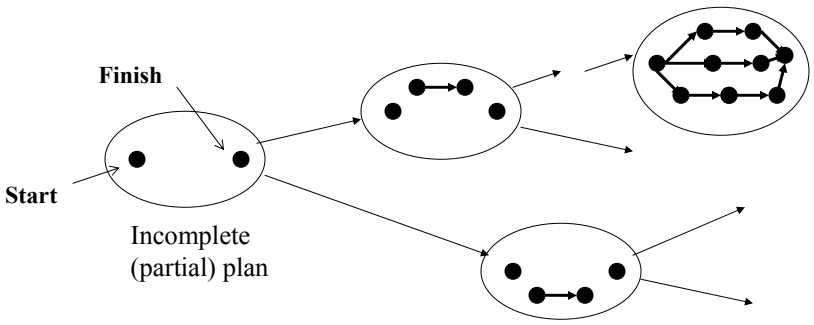
Partial order planning. Result plan.

Plan: a topological sort of a graph



Partial order planning.

- **Remember** we search the space of partial plans



- POP: **is sound and complete**

Hierarchical planners

Extension of STRIPS planners.

- Example planner: ABSTRIPS.

Idea:

- Assign a **criticality level** to each conjunct in preconditions list of the operator
- Planning process refines the plan gradually based on criticality threshold, starting from the highest criticality value:
  - Develop the plan ignoring preconditions of criticality less than the criticality threshold value (assume that preconditions for lower criticality levels are true)
  - Lower the threshold value by one and repeat previous step

Towers of Hanoi

Start position Goal position

Hierarchical planning

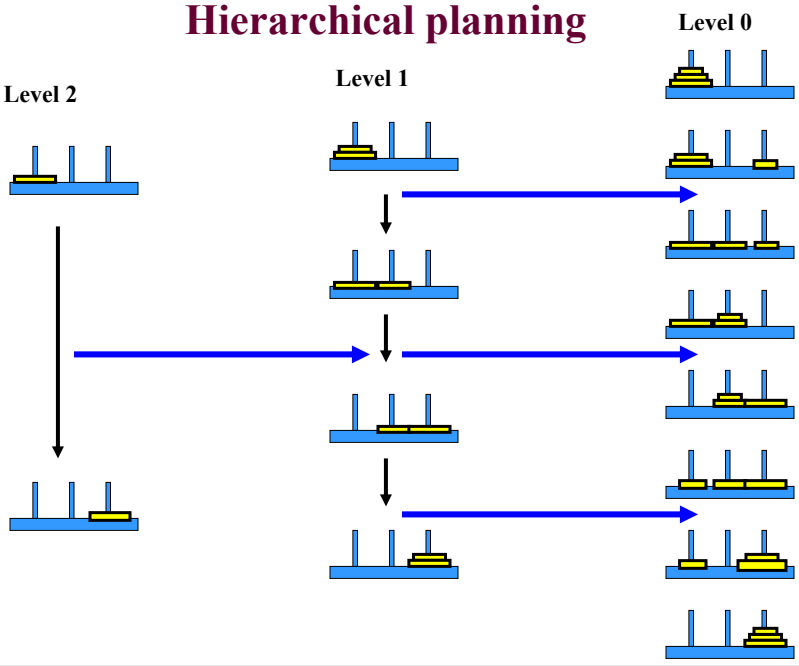
Assume:

the largest disk – criticality level 2

the medium disk – criticality level 1

the smallest disk – criticality level 0

Hierarchical planning



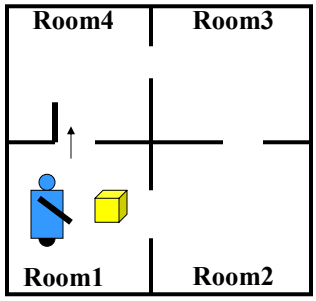
Planning with incomplete information

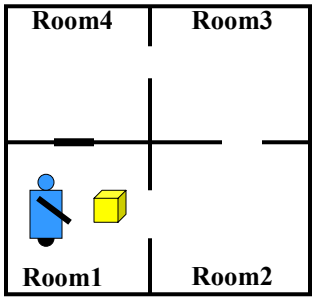
Some conditions relevant for planning can be:

- **true, false or unknown**

Example:

- Robot and the block is in Room 1
- **Goal:** get the block to Room 4
- **Problem:** The door between Room1 and 4 can be closed

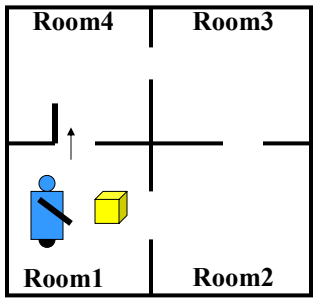


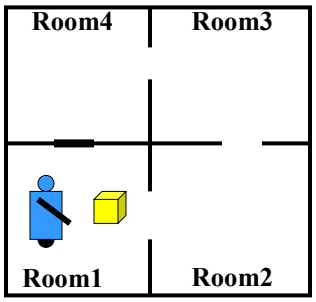


Planning with incomplete information

Initially we do not know whether the door is opened or closed:

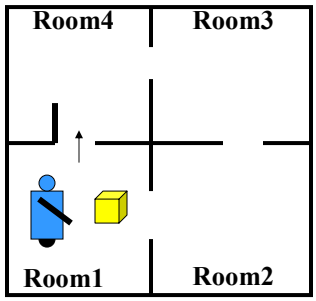
- **Different plans:**
  - **If not closed**: pick the block, go to room 4, drop the block
  - **If closed**: pick the block, go to room2, then room3 then room4 and drop the block

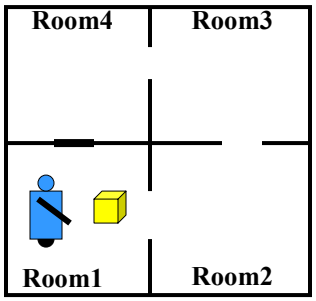




Conditional planners

- Are capable to create conditional plans that cover all possible situations (contingencies) – also called **contingency planners**
- Plan choices are applied when the missing information becomes available
- Missing information can be sought actively through actions
  - **Sensing actions**





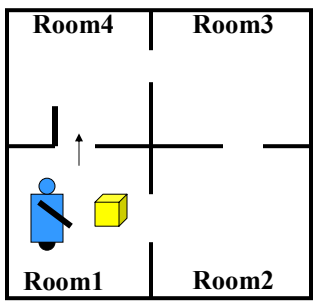
Sensing actions

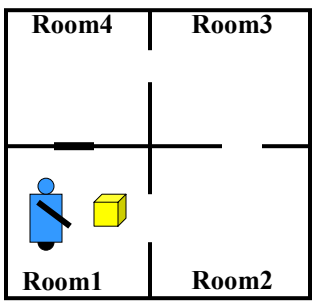
Example:

CheckDoor(d): checks the door d

Preconditions: Door(d,x,y) – one way door between x and y
& At(Robot,x)

Effect: (Closed(d) v ¬Closed(d)) - one will become true





Conditional plans

Sensing actions and conditions incorporated within the plan: