CS 1571 Introduction to AI Lecture 20

Planning: situation calculus

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Knowledge-based system

Knowledge base

Inference engine

Knowledge base:

- A set of sentences that describe the world in some formal (representational) language (e.g. first-order logic)
- Domain specific knowledge

• Inference engine:

- A set of procedures that work upon the representational language and can infer new facts or answer KB queries (e.g. resolution algorithm, forward chaining)
- Domain independent

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Automated reasoning systems

Examples and main differences:

- Theorem provers
 - Prove sentences in the first-order logic. Use inference rules, resolution rule and resolution refutation.
- Deductive retrieval systems
 - Systems based on rules (KBs in Horn form)
 - Prove theorems or infer new assertions (forward, backward chaining)
- Production systems



- Systems based on rules with actions in antecedents
- Forward chaining mode of operation
- Semantic networks



 Graphical representation of the world, objects are nodes in the graphs, relations are various links

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Production systems

Based on rules, but different from KBs in the Horn form Knowledge base is divided into:

- A Rule base (includes rules)
- A Working memory (includes facts)

A special type of if – then rule

$$p_1 \wedge p_2 \wedge \dots p_n \Rightarrow a_1, a_2, \dots, a_k$$

- Antecedent: a conjunction of literals
 - facts, statements in predicate logic
- Consequent: a conjunction of actions. An action can:
 - ADD the fact to the KB (working memory)
 - **REMOVE** the fact from the KB (consistent with logic?)
 - **QUERY** the user, etc ...

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 - **ADD** the fact to the KB (working memory)
 - REMOVE the fact from the KB ← !!! Different from logic
 - **QUERY** the user, etc ...

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Production systems

- Use forward chaining to do reasoning:
 - If the antecedent of the rule is satisfied (rule is said to be "active") then its consequent can be executed (it is "fired")
- **Problem:** Two or more rules are active at the same time. Which one to execute next?

R27 Conditions R27
$$\bigvee \Longrightarrow$$
 Actions R27 R105 Conditions R105 $\bigvee \Longrightarrow$ Actions R105

• Strategy for selecting the rule to be fired from among possible candidates is called **conflict resolution**

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Production systems

- Why is conflict resolution important? Or, Why do we care about the order?
- Assume that we have two rules and the preconditions of both are satisfied:

R1:
$$A(x) \wedge B(x) \wedge C(y) \Rightarrow add D(x)$$

R2:
$$A(x) \wedge B(x) \wedge E(z) \Rightarrow delete \ A(x)$$

• What can happen if rules are triggered in different order?

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Production systems

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- What can happen if rules are triggered in different order?
 - If R1 goes first, R2 condition is still satisfied and we infer D(x)
 - If R2 goes first we may never infer D(x)

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Production systems

- Problems with production systems:
 - Additions and Deletions can change a set of active rules;
 - If a rule contains variables testing all instances in which the rule is active may require a large number of unifications.
 - Conditions of many rules may overlap, thus requiring to repeat the same unifications multiple times.
- · Solution: Rete algorithm
 - gives more efficient solution for managing a set of active rules and performing unifications
 - Implemented in the system OPS-5 (used to implement XCON – an expert system for configuration of DEC computers)

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Rete algorithm

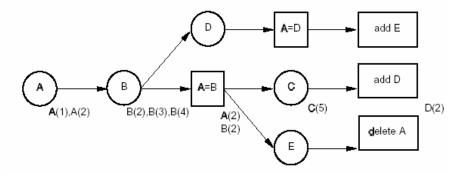
Assume a set of rules:

$$A(x) \land B(x) \land C(y) \Rightarrow add \ D(x)$$

 $A(x) \land B(y) \land D(x) \Rightarrow add \ E(x)$
 $A(x) \land B(x) \land E(z) \Rightarrow delete \ A(x)$

- And facts:
 - A(1), A(2), B(2), B(3), B(4), C(5)
- Rete:
 - Compiles the rules to a network that merges conditions of multiple rules together (avoid repeats)
 - Propagates valid unifications
 - Reevaluates only changed conditions

Rete algorithm. Network.



Rules: $A(x) \wedge B(x) \wedge C(y) \Rightarrow add D(x)$

 $A(x) \wedge B(y) \wedge D(x) \Rightarrow add E(x)$

 $A(x) \wedge B(x) \wedge E(z) \Rightarrow delete \ A(x)$

Facts: A(1), A(2), B(2), B(3), B(4), C(5)

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Conflict resolution strategies

- **Problem:** Two or more rules are active at the same time. Which one to execute next?
- Solutions:
 - **No duplication** (do not execute the same rule twice)
 - Recency. Rules referring to facts newly added to the working memory take precedence
 - **Specificity.** Rules that are more specific are preferred.
 - Priority levels. Define priority of rules, actions based on expert opinion. Have multiple priority levels such that the higher priority rules fire first.

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Semantic network systems

- Knowledge about the world described in terms of graphs. Nodes correspond to:
 - Concepts or objects in the domain.

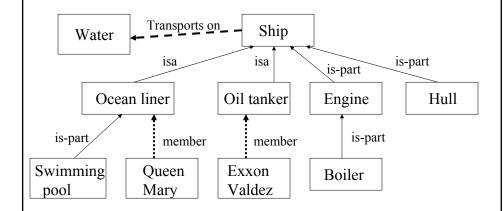
Links to relations. Three kinds:

- Subset links (isa, part-of links)
- Inheritance relation links
- Member links (instance links)
- Function links.
- Can be transformed to the first-order logic language
- Graphical representation is often easier to work with
 - better overall view on individual concepts and relations

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Semantic network. Example.



Inferred properties: Queen Mary is a ship
Queen Mary has a boiler

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Planning: situation calculus

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Representation of actions, situations, events

The world is dynamic:

- What is true now may not be true tomorrow
- Changes in the world may be triggered by our activities

Problems:

- Logic (FOL) as we had it referred to a static world. How to represent the change in the FOL?
- How to represent actions we can use to change the world?

Planning problem:

- find a sequence of actions that achieves some goal in this complex world?
- A very complex search problem

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Situation calculus

Provides a framework for representing change, actions and reasoning about them

• Situation calculus

- based on first-order logic,
- a situation variable models new states of the world
- action objects model activities
- uses inference methods developed for FOL to do the reasoning

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Situation calculus

- Logic for reasoning about changes in the state of the world
- The world is described by:
 - Sequences of **situations** of the current state
 - Changes from one situation to another are caused by actions
- The situation calculus allows us to:
 - Describe the initial state and a goal state
 - Build the KB that describes the effect of actions (operators)
 - Prove that the KB and the initial state lead to a goal state
 - extracts a plan as side-effect of the proof

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Situation calculus

The language is based on the First-order logic plus:

- Special variables: s,a objects of type situation and action
- Action functions: return actions.
 - E.g. Move(A, TABLE, B) represents a move action
 - -Move(x,y,z) represents an action schema
- Two special function symbols of type situation
 - $-s_0$ initial situation
 - -DO(a,s) denotes the situation obtained after performing an action a in situation s
- Situation-dependent functions and relations (also called fluents)
 - **Relation:** On(x,y,s) object x is on object y in situation s;
 - **Function:** Above(x,s) object that is above x in situation s.

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Situation calculus. Blocks world example.

	A
	В
A B C	С
Initial state	Goal

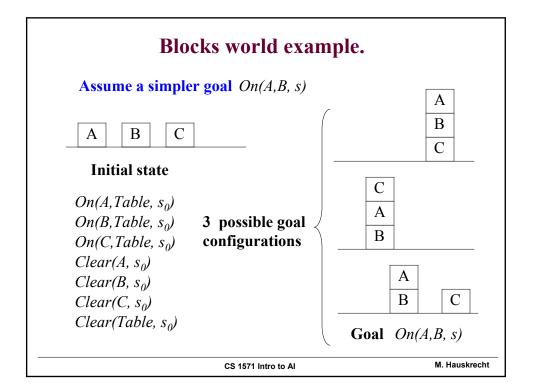
 $On(A, Table, s_0)$ $On(B, Table, s_0)$ $On(C, Table, s_0)$ On(A, B, s)Find a state (situation) s, such that

Clear(A, s_0) On(B, C, s)
Clear(B, s_0) On(C, Table, s)
Clear(C, s_0)

Clear(Table, s_0)

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Blocks world example. В В \mathbf{C} C **Initial state** Goal On(A,B,s) $On(A, Table, s_0)$ On(B,C,s) $On(B, Table, s_0)$ On(C, Table, s) $On(C, Table, s_0)$ $Clear(A, s_0)$ **Note:** It is not necessary that Clear(B, s_0) the goal describes all relations $Clear(C, s_0)$ Clear(A, s)Clear(Table, s_0) CS 1571 Intro to Al M. Hauskrecht



Knowledge base: Axioms.

Knowledge base needed to support the reasoning:

• Must represent changes in the world due to actions.

Two types of axioms:

- Effect axioms
 - changes in situations that result from actions
- Frame axioms
 - things preserved from the previous situation

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Blocks world example. Effect axioms.

Effect axioms:

Moving x from y to z. MOVE(x, y, z)

Effect of move changes on On relations

$$On(x, y, s) \land Clear(x, s) \land Clear(z, s) \rightarrow On(x, z, DO(MOVE(x, y, z), s))$$

$$On(x, y, s) \land Clear(x, s) \land Clear(z, s) \rightarrow \neg On(x, y, DO(MOVE(x, y, z), s))$$

Effect of move changes on Clear relations

$$On(x, y, s) \land Clear(x, s) \land Clear(z, s) \rightarrow Clear(y, DO(MOVE(x, y, z), s))$$

$$On(x, y, s) \land Clear(x, s) \land Clear(z, s) \land (z \neq Table)$$

 $\rightarrow \neg Clear(z, DO(MOVE(x, y, z), s))$

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Blocks world example. Frame axioms.

- Frame axioms.
 - Represent things that remain unchanged after an action.

On relations:

$$On(u, v, s) \land (u \neq x) \land (v \neq y) \rightarrow On(u, v, DO(MOVE(x, y, z), s))$$

Clear relations:

$$Clear(u, s) \land (u \neq z) \rightarrow Clear(u, DO(MOVE(x, y, z), s))$$

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Planning in situation calculus

Planning problem:

- find a sequence of actions that lead to a goal
- Planning in situation calculus is converted to the theorem proving problem

Goal state:

$$\exists s \ On(A,B,s) \land On(B,C,s) \land On(C,Table,s)$$

- Possible inference approaches:
 - Inference rule approach
 - Conversion to SAT
- Plan (solution) is a byproduct of theorem proving.

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Example: blocks world

Planning in a blocks world.

A B C

A B C

Initial state

 $On(A, Table, s_0)$ $On(B, Table, s_0)$ $On(C, Table, s_0)$ $Clear(A, s_0)$ $Clear(B, s_0)$ $Clear(C, s_0)$

Clear(Table, s_0)

On(A,B, s) On(B,C, s)On(C,Table, s)

Goal

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Planning in the blocks world.



Initial state (s0)

 $s_0 =$

s1

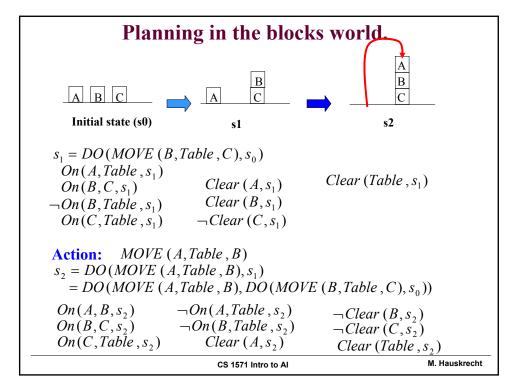
$$On(A, Table, s_0)$$
 $Clear(A, s_0)$
 $On(B, Table, s_0)$ $Clear(B, s_0)$
 $On(C, Table, s_0)$ $Clear(C, s_0)$

Action: MOVE(B, Table, C) $s_1 = DO(MOVE(B, Table, C), s_0)$ $On(A, Table, s_1)$ $On(B, C, s_1)$ $\neg On(B, Table, s_1)$ $On(C, Table, s_1)$ $On(C, Table, s_1)$ $On(C, Table, s_1)$ $On(C, Table, s_1)$

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Clear (Table, s_0)



Planning in situation calculus.

Planning problem:

- Find a sequence of actions that lead to a goal
- Is a special type of a search problem
- Planning in situation calculus is converted to theorem proving.

• Problems:

- Large search space
- Large number of axioms to be defined for one action
- Proof may not lead to the best (shortest) plan.

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Planning

Planning problem:

- find a sequence of actions that achieves some goal
- An instance of a search problem

Methods for modeling and solving a planning problem:

- State space search
- Situation calculus based on FOL
 - Inference rules
 - Resolution refutation

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