

# CS 1571 Introduction to AI

## Lecture 15

### Partial order planning

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### Administration

- **Problem sets:**
  - **PS 1-5** graded and available for pick up
  - **PS solutions** are on the web
- **Midterms:**
  - at the end of the class

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# Planning

## Planning problem:

- find a sequence of actions that lead to a goal
- this requires to model and reason about effects of agent's actions on the real-world.

## Planning problem:

- is a special type of a **search problem**
- **State space:** states of the world.
- **Initial state:** A world state we start from.
- **Operators.** Application of actions that change the state.
- **Goal condition.** Desired state of the world.

# Planning

## Specifics of a planning problem:

- Complex description of world states
- Large number of actions
- Every action effects only a “small” subset of relations in the state
- Goals are defined over a “small” set of relations

## This causes:

- a large branching factor of the search tree,
- long action sequences (solution length is large)

## Planning systems design.

Two planning systems designs:

- **Situation calculus**
  - based on first-order logic,
  - a situation variable models new states of the world
  - use inference methods developed for FOL to do the reasoning
- **STRIPS –planners**
  - STRIPS – Stanford research institute problem solver
  - Restricted language as compared to the situation calculus
  - Allows for more efficient planning algorithms

## STRIPS representation.

- More restricted representation language as compared to the situation calculus
- **States:**
  - represent facts that are true at a specific point in time
  - conjunction of literals, e.g.  $On(A,B)$ ,  $On(B,Table)$ ,  $Clear(A)$
- **Actions (operators):**

**Operator:**  $Move(x,y,z)$

  - **Preconditions:**  $On(x,y)$ ,  $Clear(x)$ ,  $Clear(z)$
  - **Effect lists:**
    - **Add list:**  $On(x,z)$ ,  $Clear(y)$
    - **Delete list:**  $On(x,y)$ ,  $Clear(z)$   
(Everything else is unaffected)
- **Goals:** conjunctions of literals, e.g.  $On(A,B)$ ,  $On(B,C)$ ,

## STRIPS representation. Benefits.

### Benefits:

- States, actions and goals have structure
- **Action representation:**
  - Leads to more intuitive and compact description of actions (no need to write many axioms !!!)
  - Avoids the frame problem
- Restrictions lead to more efficient planning algorithms.

### STRIPS planning:

- find a sequence of operators from the initial state to the goal
- Search problem definition in STRIPS looks much like the standard search problem definition

## STRIPS planning.

### STRIPS planning problem:

- Find a sequence of actions that lead to a goal
- States and goals are defined by a conjunctions of literals

### Two basic search methods:

- **Forward search** (goal progression)
  - From the initial state try to reach the goal
- **Backward search** (goal regression)
  - Start from the goal and try to project it to the initial state

### More complex planning method:

- **Partial-order planning (POP)**
  - Search the space of partially build plans

## Divide and conquer.

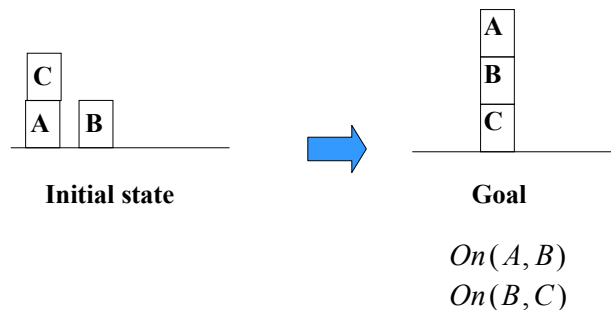
- **Divide and conquer strategy:**
  - divide the problem to a set of smaller sub-problems,
  - solve each sub-problem independently
  - combine the results to form the

In planning we would like to satisfy a set of goals

- **Divide and conquer in planning:**
  - Divide the planning goals along individual goals
  - Solve (find a plan for) each of them independently
  - Combine the plan solutions in the resulting plan
- Is it always safe to use divide and conquer?
  - No. There can be interacting goals.

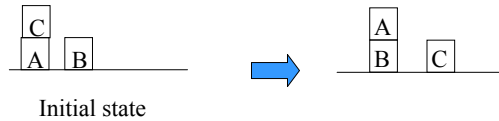
## Sussman's anomaly.

- An example from the blocks world in which divide and conquer fails
- Interacting goals



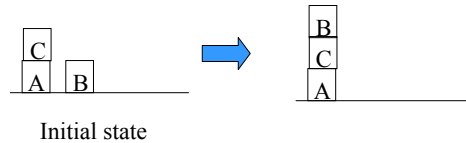
## Sussman's anomaly

1. Assume we want to satisfy  $On(A, B)$  first



But now we cannot satisfy  $On(B, C)$  without undoing  $On(A, B)$

2. Assume we want to satisfy  $On(B, C)$  first.



But now we cannot satisfy  $On(A, B)$  without undoing  $On(B, C)$

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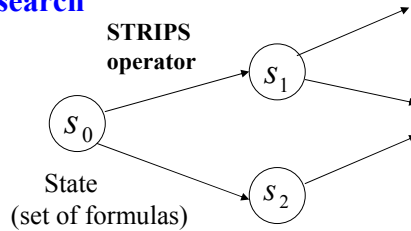
## State space vs. plan space

- An alternative to planning algorithms that search states (configurations of world) is to search the space of plans
- **Plan:** Defines sequences of operators to be performed
- **Partial plan:**
  - plan that is not complete
    - Some plan steps are missing
  - some orderings of operators are not finalized
    - Only relative order is given
- **Benefits of working with partial plans:**
  - We do not have to build the sequence from the initial state or the goal
  - We do not have to commit to a specific action sequence
  - We can work on sub-goals individually (divide and conquer)

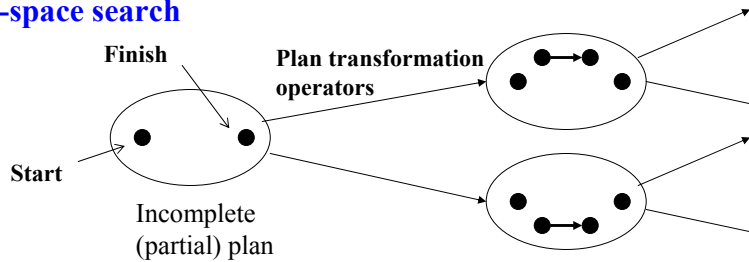
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## State-space vs. plan-space search

### State-space search



### Plan-space search

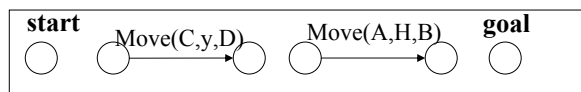
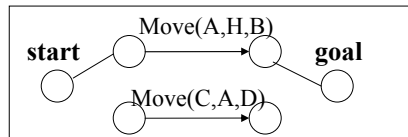
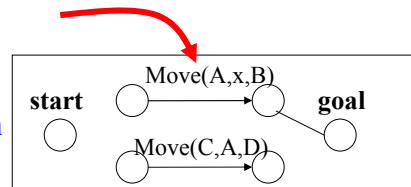


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## Plan transformation operators

Examples of :

- Add an operator to a plan so that it satisfies some open condition
- Add link (+ instantiate)
- Order (reorder) operators

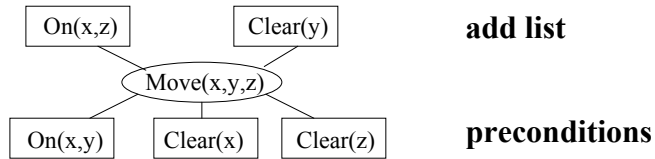


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## Partial-order planners (POP)

- also called **Non-linear planners**
- Use STRIPS operators

Graphical representation of an **operator** **Move(x,y,z)**

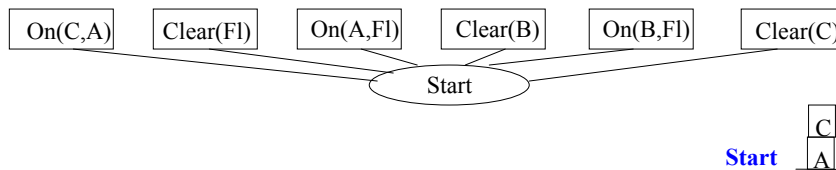
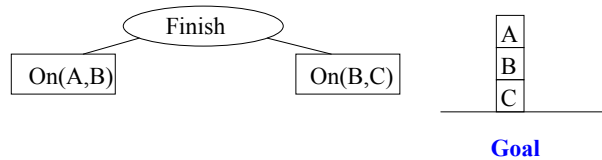


**Delete list is not shown !!!**

Illustration of POP on the Sussman's anomaly case

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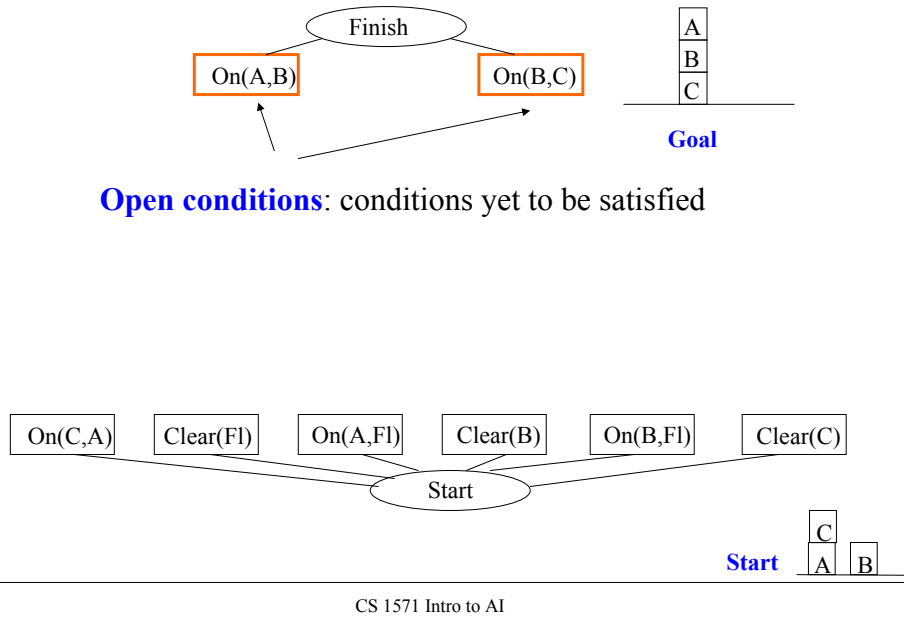
## Partial order planning. Start and finish.



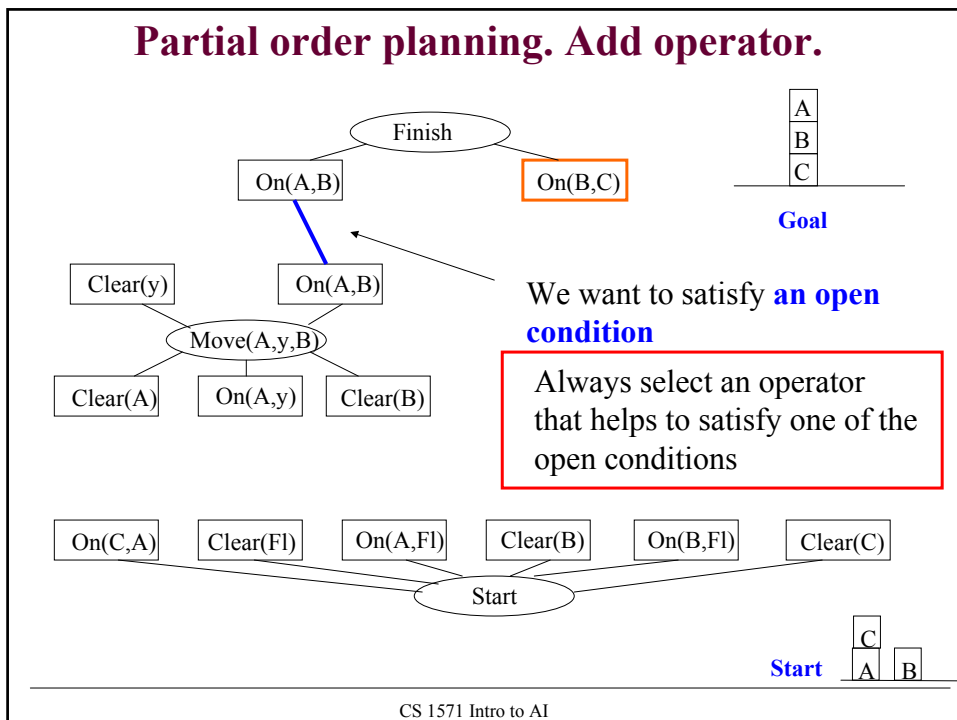
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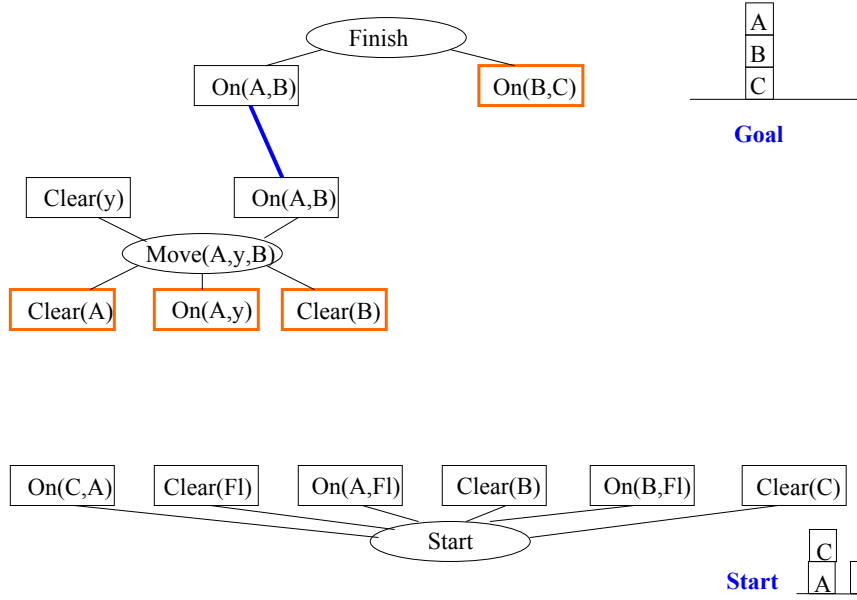
## Partial order planning. Start and finish.



## Partial order planning. Add operator.

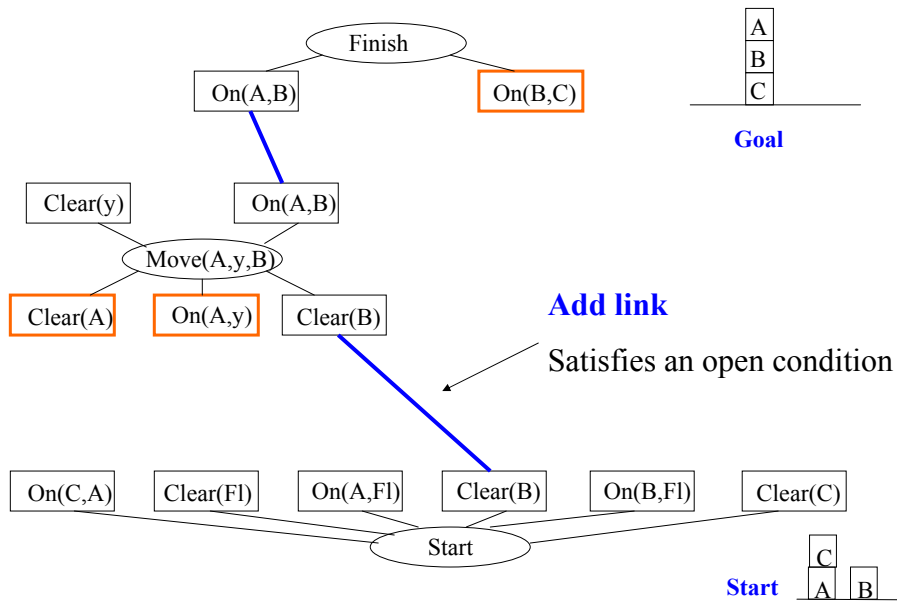


## Partial order planning. Add link.



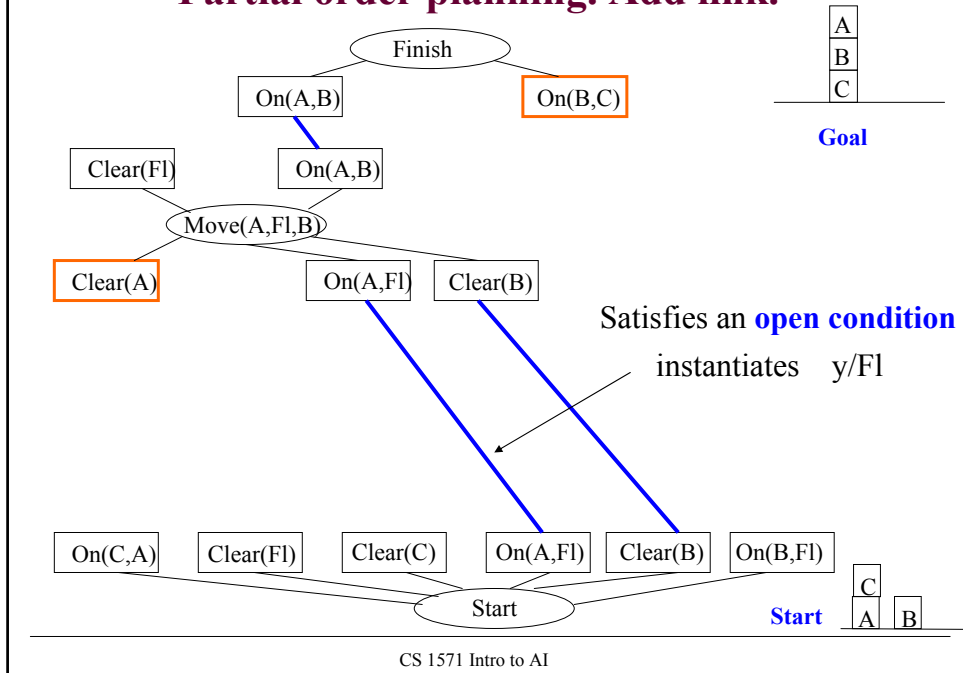
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## Partial order planning. Add link.

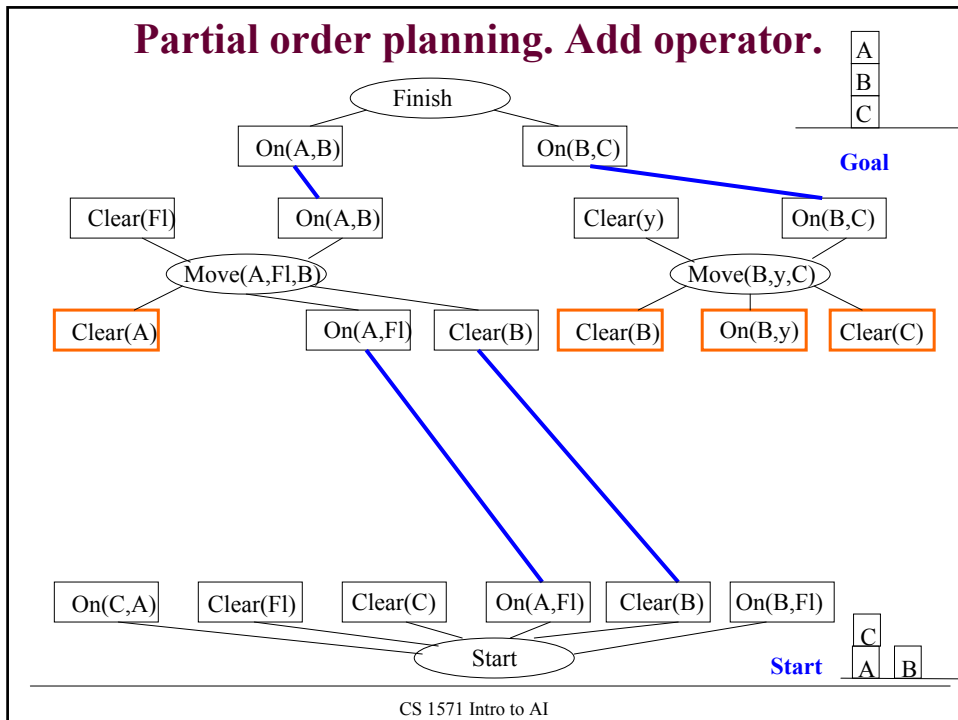


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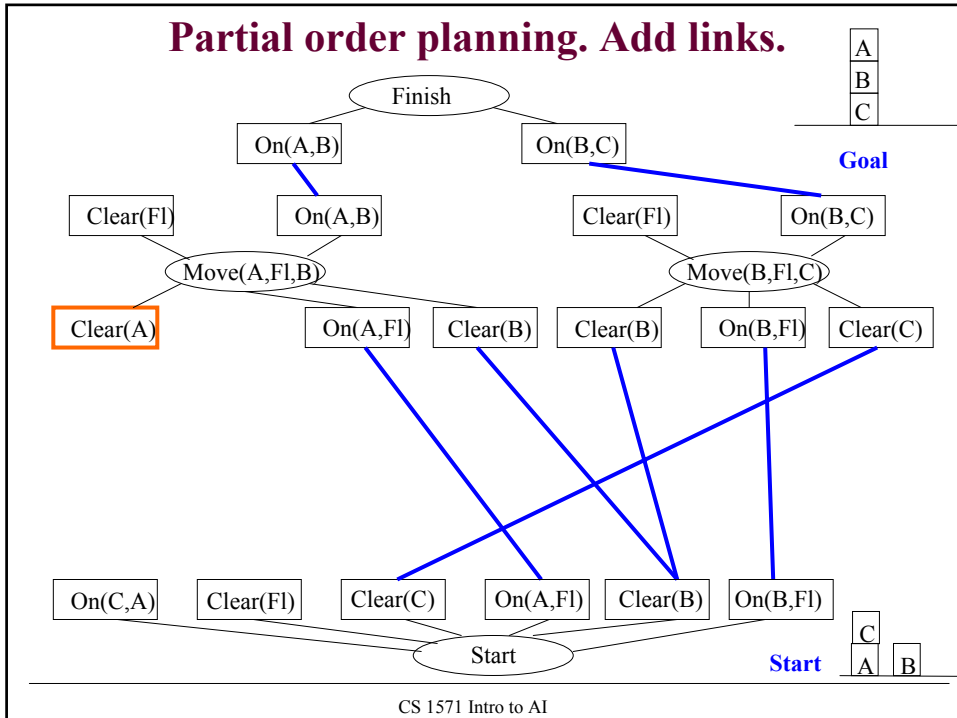
## Partial order planning. Add link.



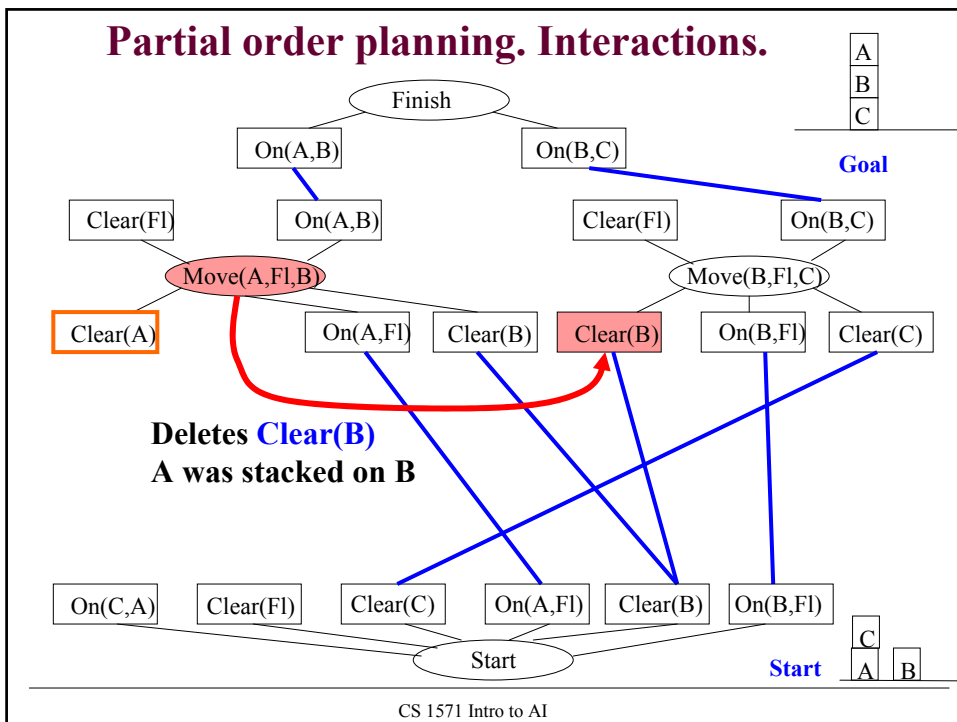
## Partial order planning. Add operator.



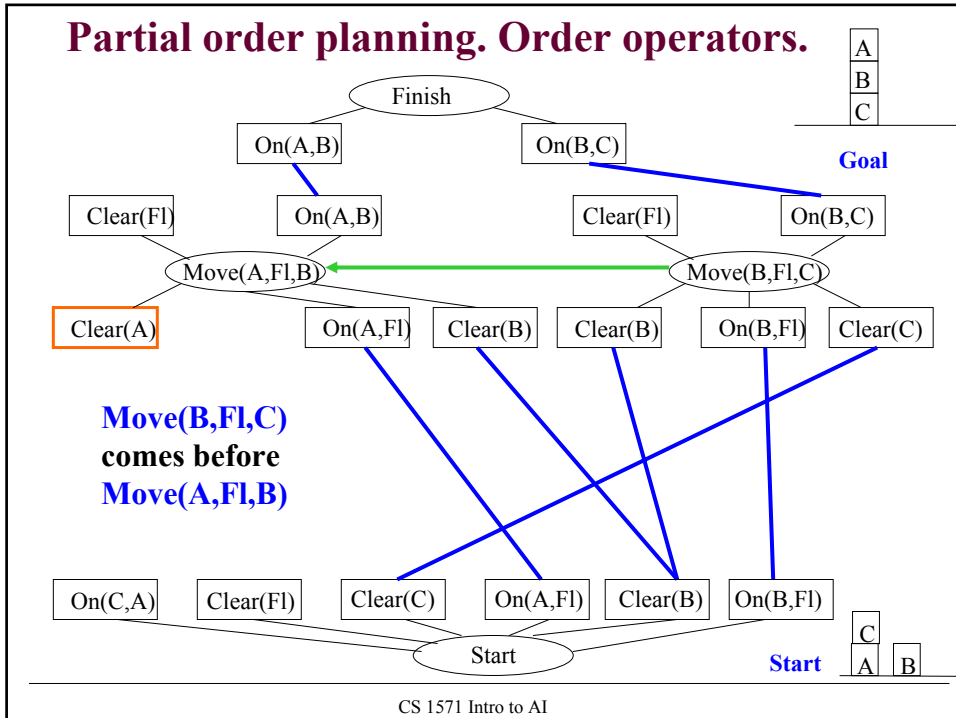
## Partial order planning. Add links.



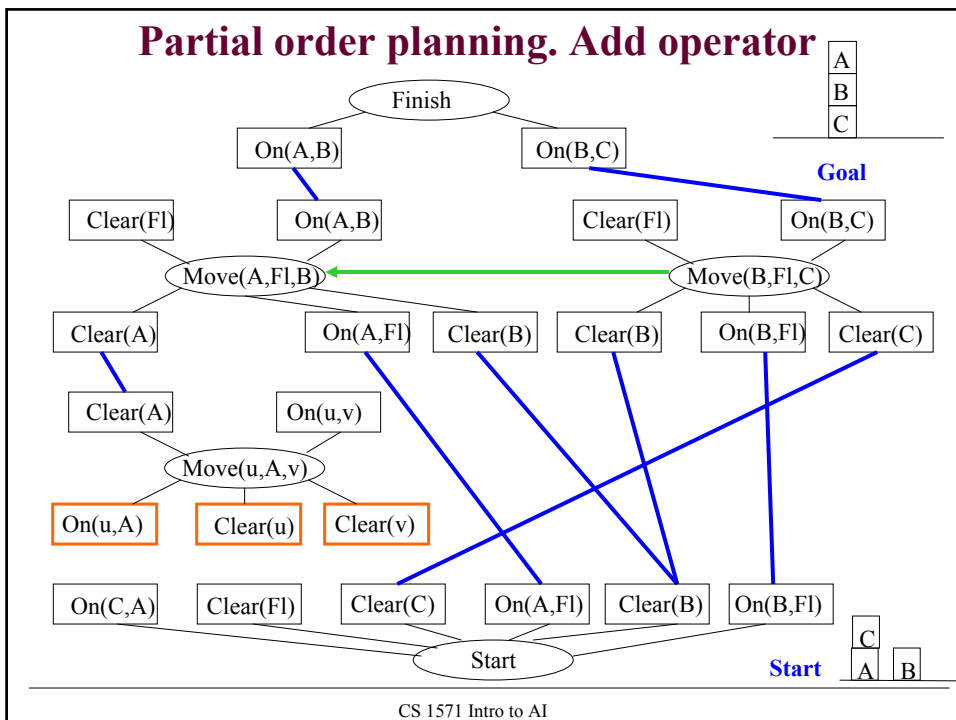
## Partial order planning. Interactions.



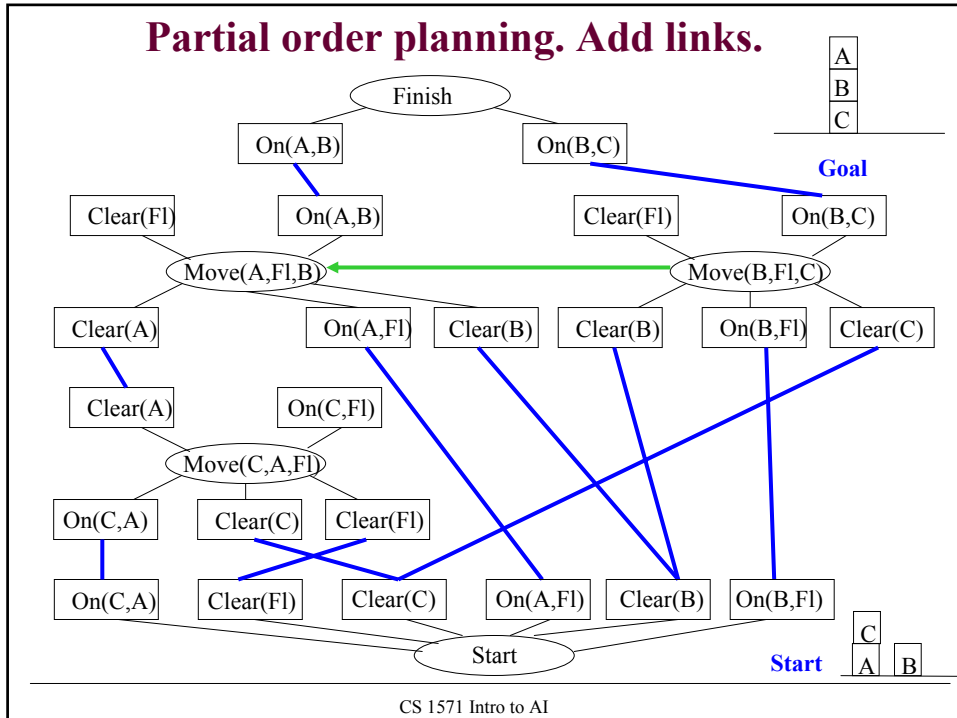
## Partial order planning. Order operators.



## Partial order planning. Add operator

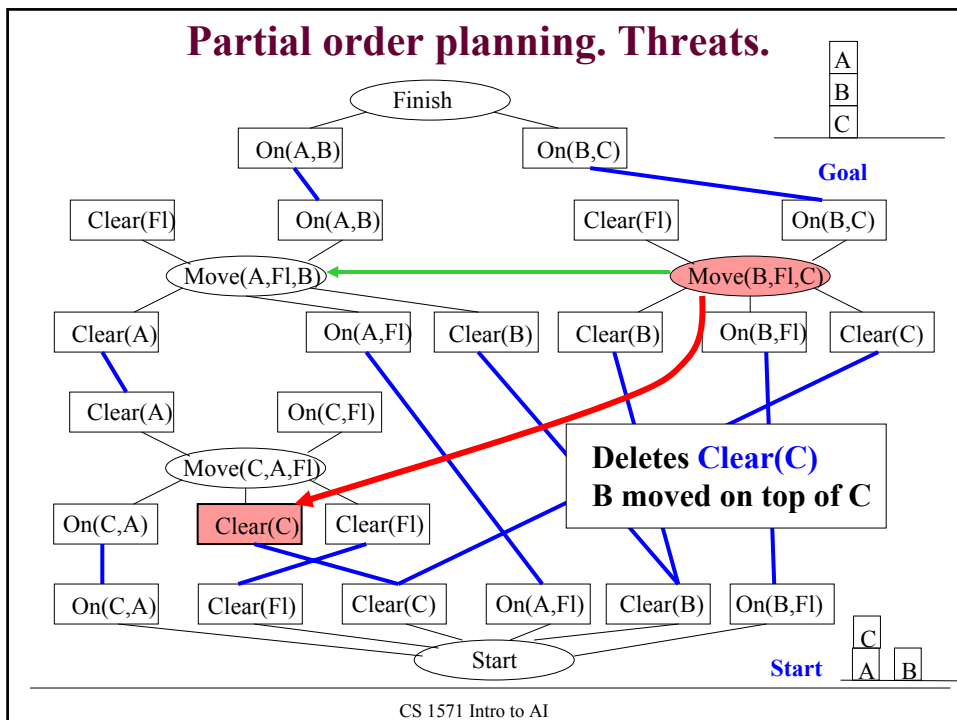


## Partial order planning. Add links.



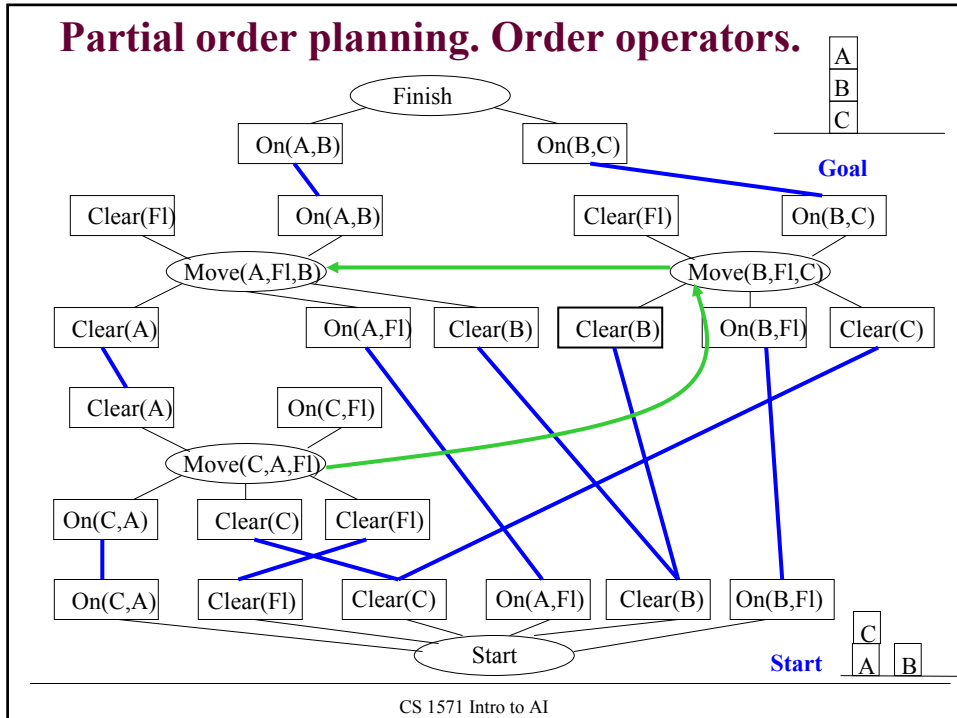
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## Partial order planning. Threats.

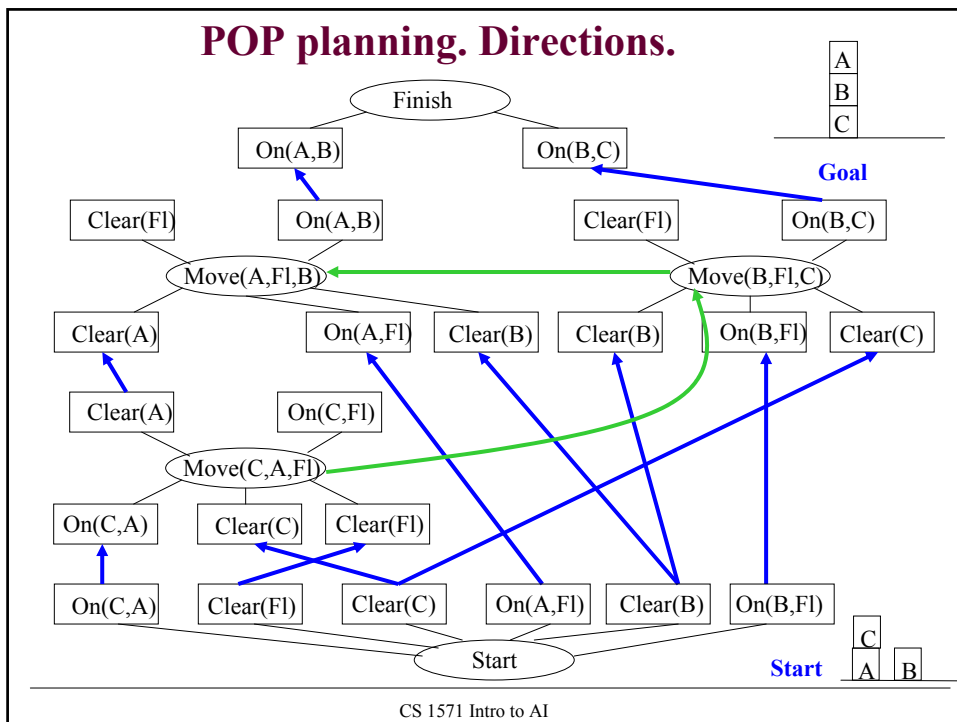


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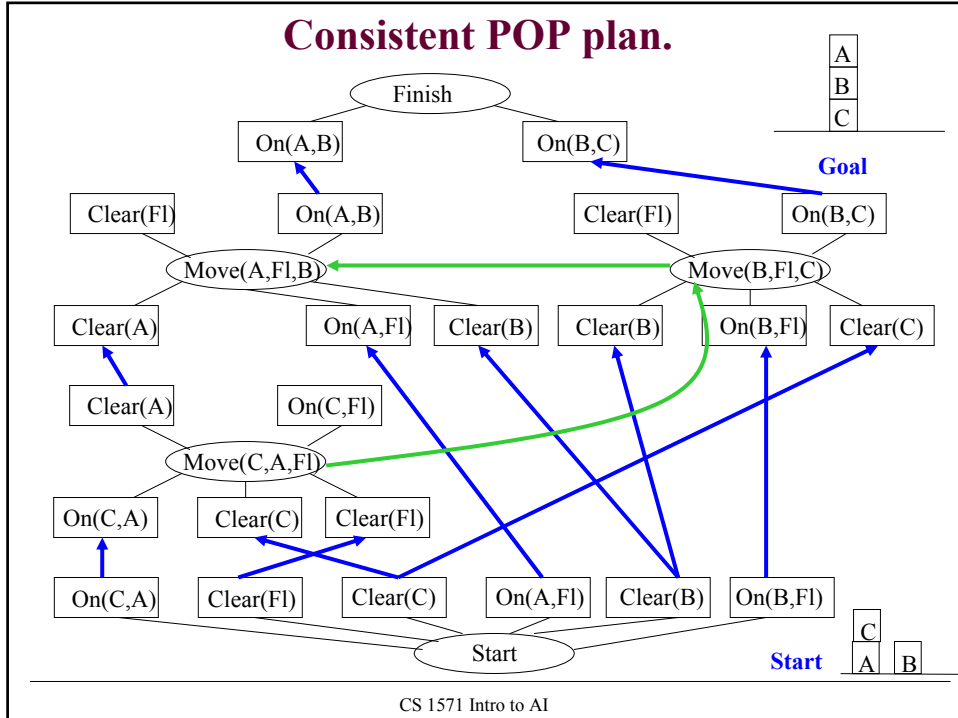
## Partial order planning. Order operators.



## POP planning. Directions.

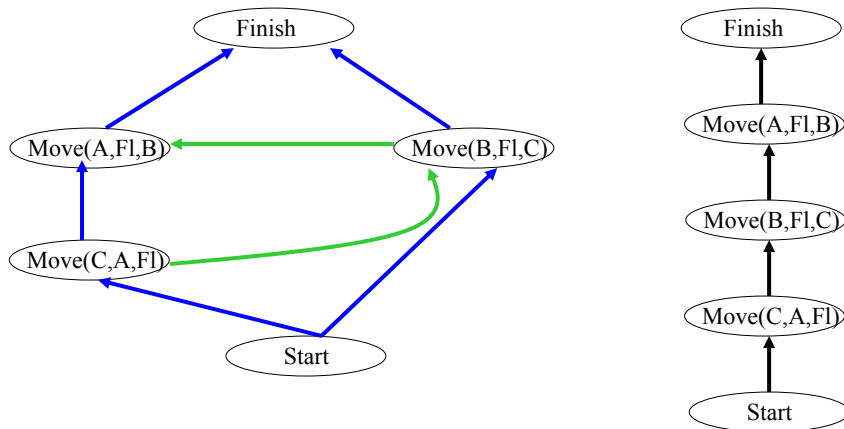


## Consistent POP plan.



## Partial order planning. Result plan.

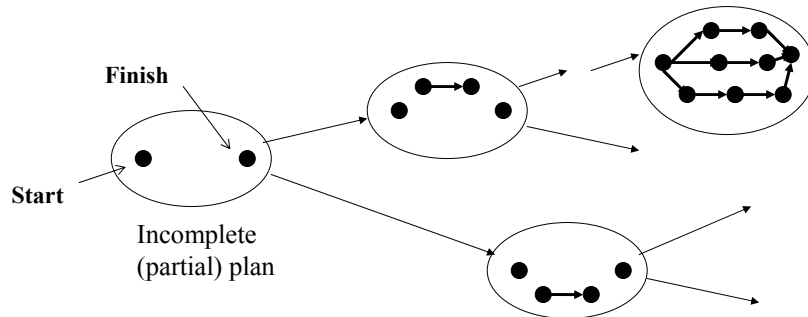
Plan: a topological sort of a graph





## Partial order planning.

- **Remember** we search the space of partial plans



- POP: **is sound and complete**

## Hierarchical planners

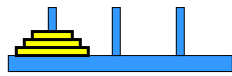
### Extension of STRIPS planners.

- Example planner: ABSTRIPS.

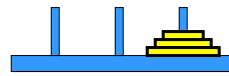
#### Idea:

- Assign a **criticality level** to each conjunct in preconditions list of the operator
- Planning process refines the plan gradually based on criticality threshold, starting from the highest criticality value:
  - Develop the plan ignoring preconditions of criticality less than the criticality threshold value (assume that preconditions for lower criticality levels are true)
  - Lower the threshold value by one and repeat previous step

# Towers of Hanoi



Start position



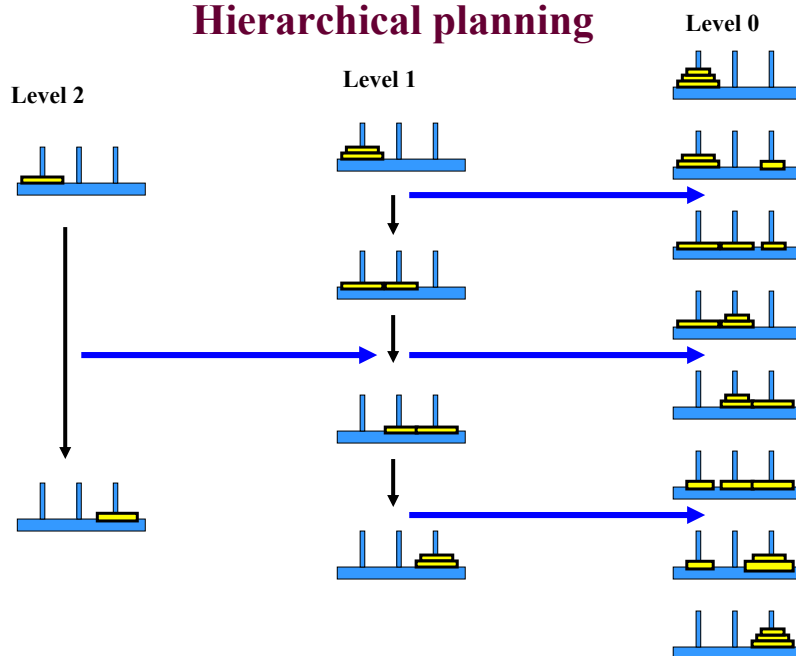
Goal position

## Hierarchical planning

Assume:

- the largest disk – criticality level 2
- the medium disk – criticality level 1
- the smallest disk – criticality level 0

## Hierarchical planning



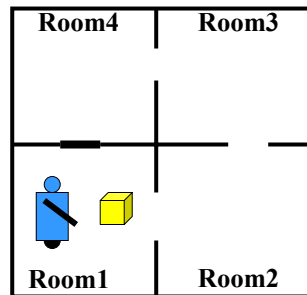
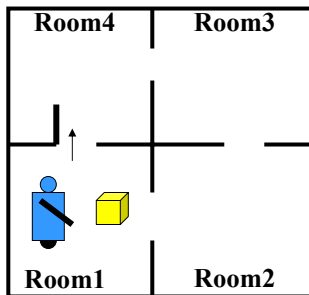
## Planning with incomplete information

Some conditions relevant for planning can be:

- true, false or **unknown**

### Example:

- Robot and the block is in Room 1
- **Goal:** get the block to Room 4
- **Problem:** The door between Room1 and 4 can be closed

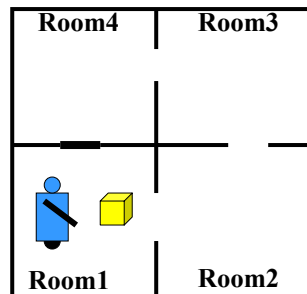
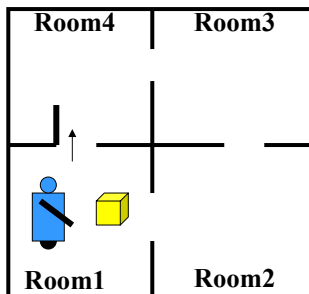


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## Planning with incomplete information

Initially we do not know whether the door is opened or closed:

- **Different plans:**
  - **If not closed:** pick the block, go to room 4, drop the block
  - **If closed:** pick the block, go to room2, then room3 then room4 and drop the block



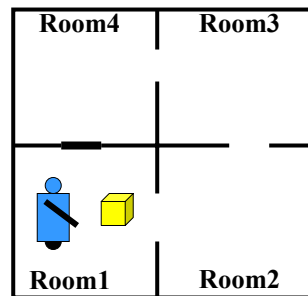
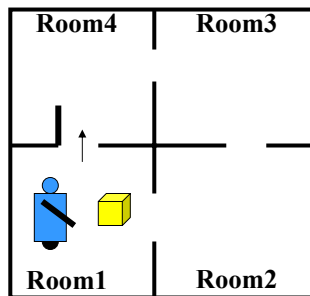
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## Planning with incomplete information

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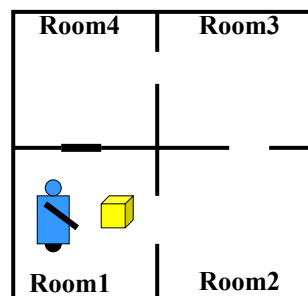
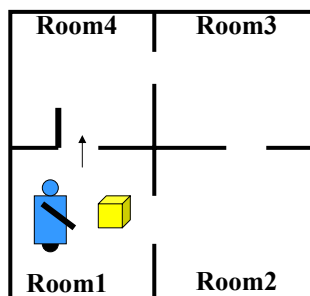
- **If not closed:** pick the block, go to room 4, drop the block
- **If closed:** pick the block, open the door, go to room4, and drop the block



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## Conditional planners

- Are capable to create conditional plans that cover all possible situations (contingencies) – also called **contingency planners**
- Plan choices are applied when the missing information becomes available
- Missing information can be sought actively through actions
  - **Sensing actions**



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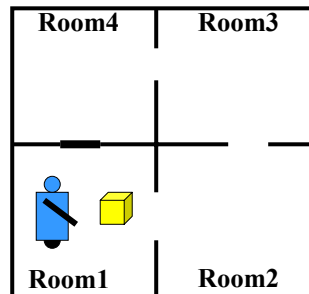
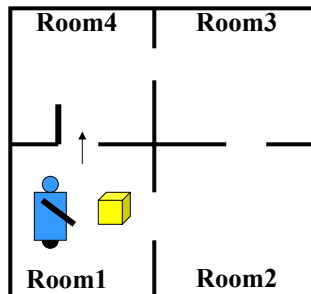
## Sensing actions

**Example:**

**CheckDoor(d):** checks the door d

**Preconditions:**  $\text{Door}(d,x,y)$  – one way door between x and y  
 &  $\text{At}(\text{Robot},x)$

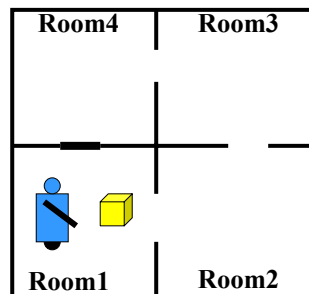
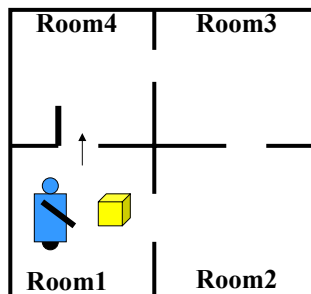
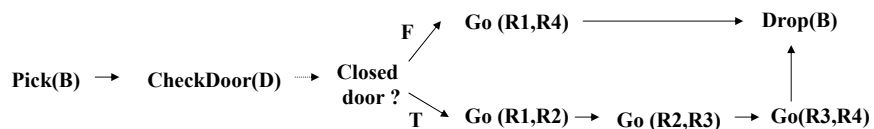
**Effect:**  $(\text{Closed}(d) \vee \neg \text{Closed}(d))$  - one will become true



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## Conditional plans

Sensing actions and conditions incorporated within the plan:



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