CS 2770: Computer Vision Introduction

Prof. Adriana Kovashka University of Pittsburgh January 8, 2019

About the Instructor









Born 1985 in Sofia, Bulgaria







Got BA in 2008 at Pomona College, CA (Computer Science & Media Studies)







Got PhD in 2014 at University of Texas at Austin (Computer Vision)

Course Info

- Course website:
 - http://people.cs.pitt.edu/~kovashka/cs2770 sp18
- Instructor: Adriana Kovashka (kovashka@cs.pitt.edu)
- Office: Sennott Square 5325
- Class: Tue/Thu, 11am-12:15pm
- Office hours: Tue/Thu, 10:30-11am, 12:30-2pm

TA

- Narges Honarvar Nazari (nah114@pitt.edu)
- Office: Sennott Square 5501
- Office hours: TBD
 - Do this Doodle by the end of Friday:

https://doodle.com/poll/fxhsg826gmwcyhuu

Textbooks

- Computer Vision: Algorithms and Applications by Richard Szeliski
- Visual Object Recognition by Kristen Grauman and Bastian Leibe
- More resources available on course webpage

 Your notes from class are your best study material, slides are not complete with notes

Programming Languages

- Homework: Matlab or Python
- Projects: Whatever language you like

Matlab Tutorials and Exercises

http://www.cs.pitt.edu/~kovashka/cs2770 sp18/tutorial.m

http://www.cs.pitt.edu/~kovashka/cs2770 sp18/myfunction.m http://www.cs.pitt.edu/~kovashka/cs2770 sp18/myotherfunction.m

https://people.cs.pitt.edu/~milos/courses/cs2750/Tutorial/ http://www.math.udel.edu/~braun/M349/Matlab_probs2.pdf http://www.facstaff.bucknell.edu/maneval/help211/basicexercises.html

Ask the TA or instructor if you have any problems.

Types of computer vision

- Lower-level vision
 - Analyzing textures, edges and gradients in images, without concern for the semantics (e.g. objects) of the image
- Higher-level vision (our focus)
 - Making predictions about the semantics or higher-level functions of content in images (e.g. objects, attributes, styles, motion, etc.)
 - Involves machine learning

Course Goals

- To learn the basics of low-level image analysis
- To learn the modern approaches to classic high-level computer vision tasks
- To get experience with some computer vision techniques
- To learn/apply basic machine learning (a key component of modern computer vision)
- To get exposure to emerging topics and recent research
- To think critically about vision approaches, and to see connections between works and potential for improvement

Policies and Schedule

http://people.cs.pitt.edu/~kovashka/cs2770 sp19

- Grading and course components
- Project
- Schedule

Should I take this class?

- It will be a lot of work
 - But you will learn a lot
- Some parts will be hard and require that you pay close attention
 - Use instructor's and TA's office hours!
- Some aspects are open-ended are there are no clear correct answers
 - You will learn/practice reading research papers

Questions?

Plan for Today

- Introductions
- What is computer vision?
 - Why do we care?
 - What are the challenges?
- Overview of topics
 - What is current research like?
- Linear algebra blitz review

Introductions

- What is your name?
- What one thing outside of school are you passionate about?
- Do you have any prior experience with computer vision or machine learning?
- What do you hope to get out of this class?

 Every time you speak, please remind me your name, and say it slowly

Computer Vision

What is computer vision?



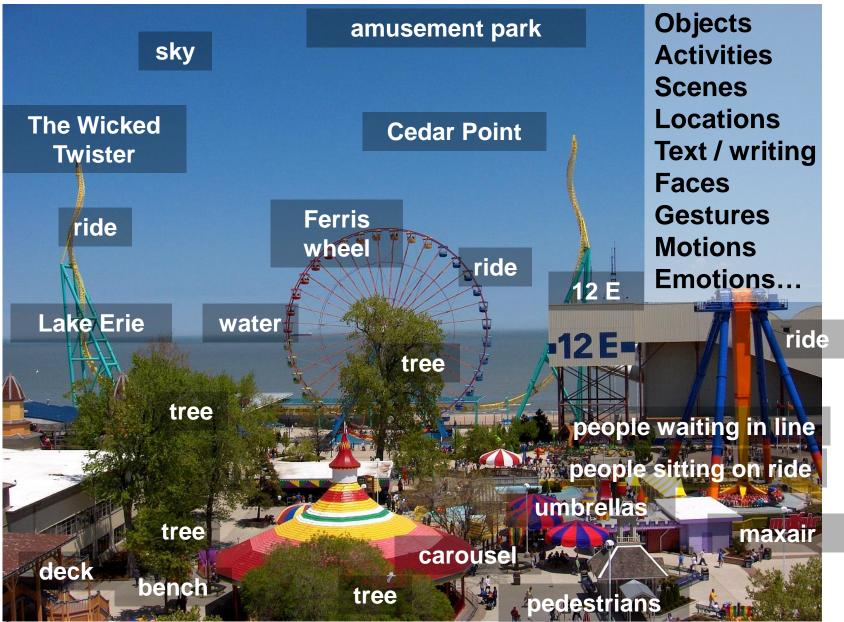
Done?

"We see with our brains, not with our eyes" (Oliver Sacks and others)

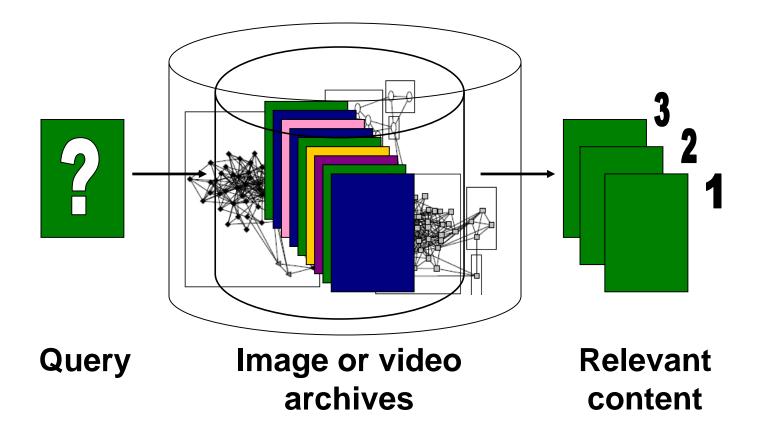
What is computer vision?

- Automatic understanding of images/video, e.g.
 - Algorithms and representations to allow a machine to recognize objects, people, scenes, and activities
 - Algorithms to mine, search, interact with visual data
 - Computing properties of the 3D world from visual data

Vision for recognition

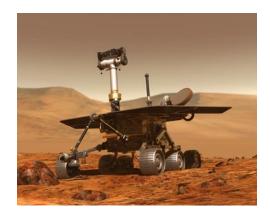


Visual search, organization



Vision for measurement

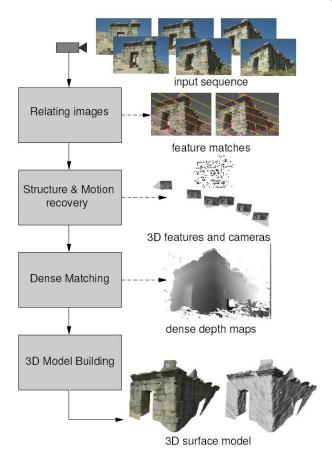
Real-time stereo





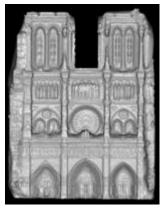
Pollefeys et al.

Structure from motion



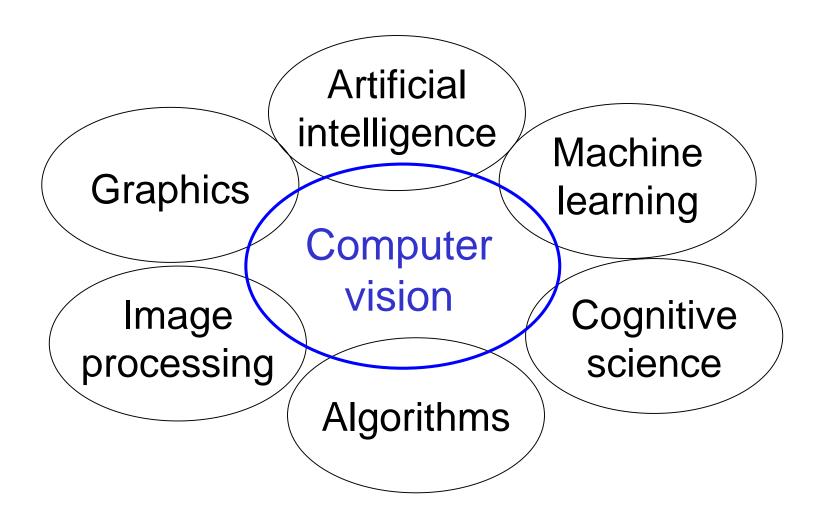
Multi-view stereo for community photo collections



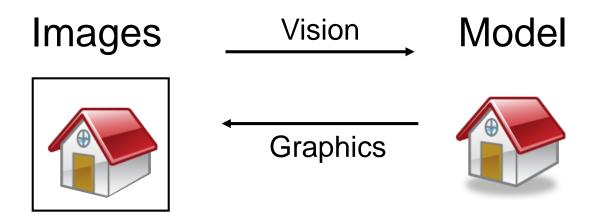


Goesele et al.

Related disciplines



Vision and graphics



Inverse problems: analysis and synthesis.

Why vision?

144k hours uploaded to YouTube daily 4.5 mil photos uploaded to Flickr daily 10 bil images indexed by Google

Images and video are everywhere!





Movies, news, sports

Personal photo albums



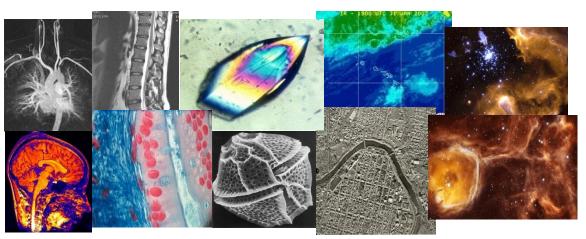








Surveillance and security



Medical and scientific images

Why vision?

- As image sources multiply, so do applications
 - Relieve humans of boring, easy tasks
 - Human-computer interaction
 - Perception for robotics / autonomous agents
 - Organize and give access to visual content
 - Description of image content for the visually impaired
 - Fun applications (e.g. transfer art styles to my photos)

What tasks are currently feasible for computer vision systems?

Faces and digital cameras



Camera waits for everyone to smile to take a photo [Canon]



Setting camera focus via face detection

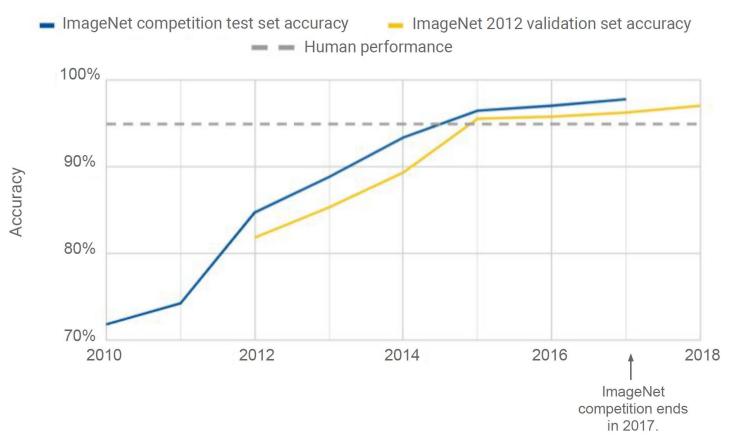
Face recognition



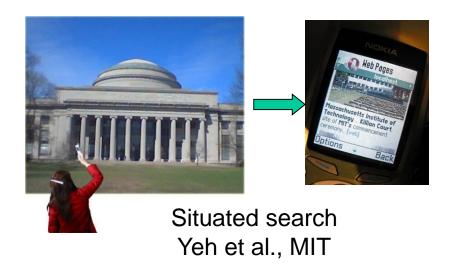
Object classification

ImageNet (2010 -2018)

Source: ImageNet; see appendix



Linking to info with a mobile device





MSR Lincoln



kooaba

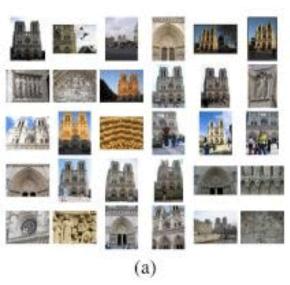
Exploring photo collections

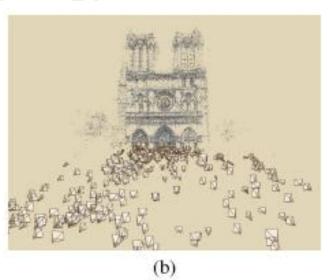


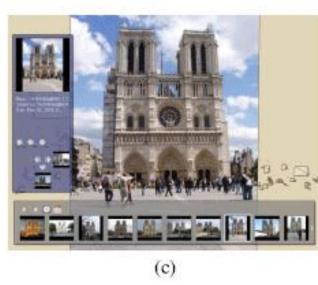
Photo Tourism



Exploring photo collections in 3D



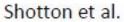




Snavely et al.

Interactive systems







Vision for medical & neuroimages

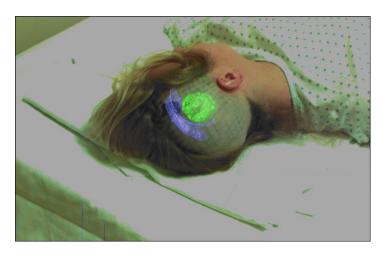
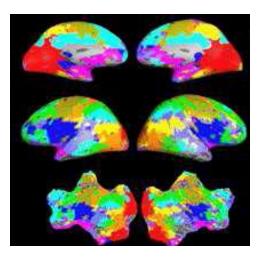
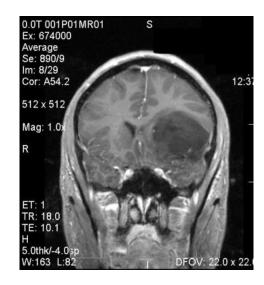


Image guided surgery MIT AI Vision Group



fMRI data Golland et al.



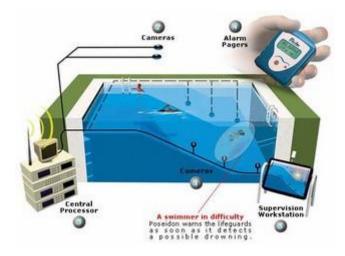
Safety & security



Navigation, driver safety



Pedestrian detection MERL, Viola et al.



Monitoring pool (Poseidon)



Surveillance

Healthy eating



FarmBot.io YouTube Link

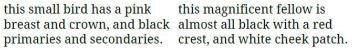
Im2calories by Myers et al., ICCV 2015 <u>figure source</u>

Self-training for sports?



Image generation

this small bird has a pink primaries and secondaries.





the flower has petals that are bright pinkish purple with white stigma



this white and yellow flower have thin white petals and a round yellow stamen





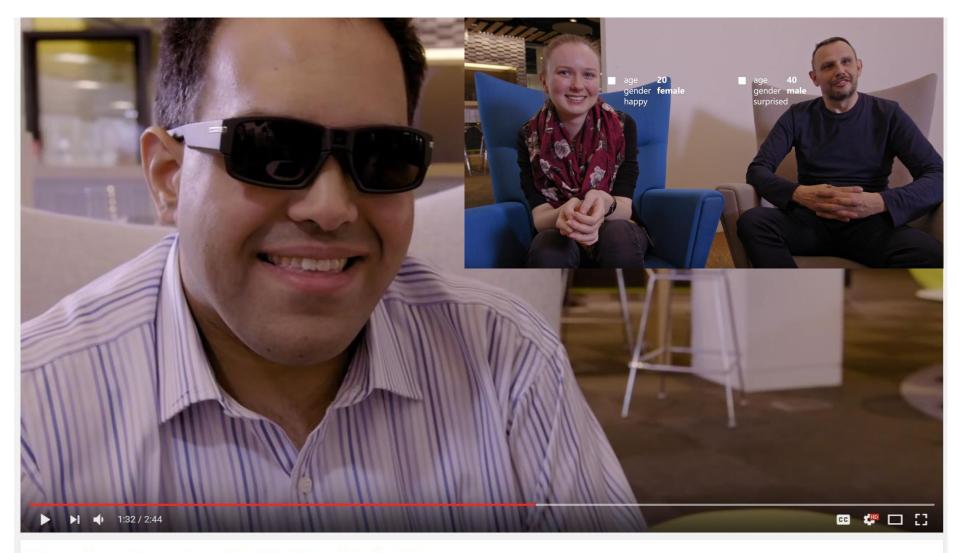
Figure 1. Examples of generated images from text descriptions. Left: captions are from zero-shot (held out) categories. Right: captions are from training set categories.

Reed et al., ICML 2016

Figure 3: Generated bedrooms after five epochs of training. There appears to be evidence of visual under-fitting via repeated noise textures across multiple samples such as the base boards of some of the beds.

Seeing Al

YouTube link



Obstacles?

MASSACHUSETTS INSTITUTE OF TECHNOLOGY PROJECT MAC

Artificial Intelligence Group Vision Memo. No. 100. July 7, 1966

THE SUMMER VISION PROJECT

Seymour Papert

The summer vision project is an attempt to use our summer workers effectively in the construction of a significant part of a visual system. The particular task was chosen partly because it can be segmented into sub-problems which will allow individuals to work independently and yet participate in the construction of a system complex enough to be a real landmark in the development of "pattern recognition".

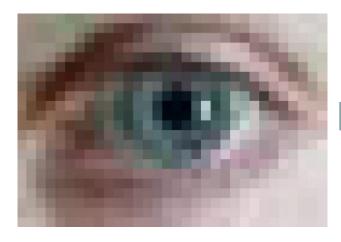
Why is vision difficult?

- Ill-posed problem: real world much more complex than what we can measure in images
 - $-3D \rightarrow 2D$
- Impossible to literally "invert" image formation process with limited information
 - Need information outside of this particular image to generalize what image portrays (e.g. to resolve occlusion)

What the computer gets









Why is this problematic?

Challenges: many nuisance parameters



Illumination



Object pose





Clutter



Occlusions



Intra-class appearance



Viewpoint

Think again about the pixels...

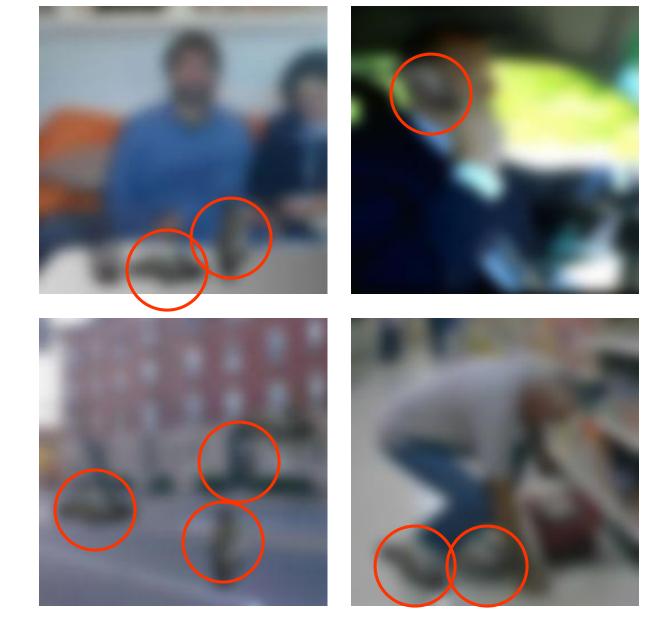
Challenges: intra-class variation







Challenges: importance of context



Challenges: Complexity

- Thousands to millions of pixels in an image
- 3,000-30,000 human recognizable object categories
- 30+ degrees of freedom in the pose of articulated objects (humans)
- Billions of images indexed by Google Image Search
- 1.424 billion smart camera phones sold in 2015
- About half of the cerebral cortex in primates is devoted to processing visual information [Felleman and van Essen 1991]

Challenges: Limited supervision

More Less Multiple objects Classes labeled, parts and to object

Kristen Grauman

Challenges: Vision requires reasoning



What color are her eyes?
What is the mustache made of?



How many slices of pizza are there? Is this a vegetarian pizza?



Is this person expecting company? What is just under the tree?



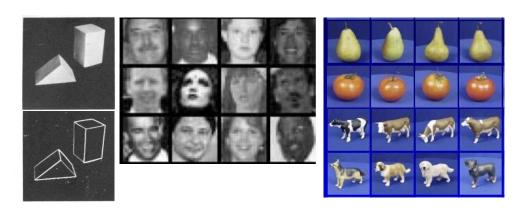
Does it appear to be rainy?

Does this person have 20/20 vision?

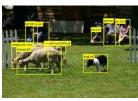
Evolution of datasets

Challenging problem

active research area









PASCAL: 20 categories, 12k images

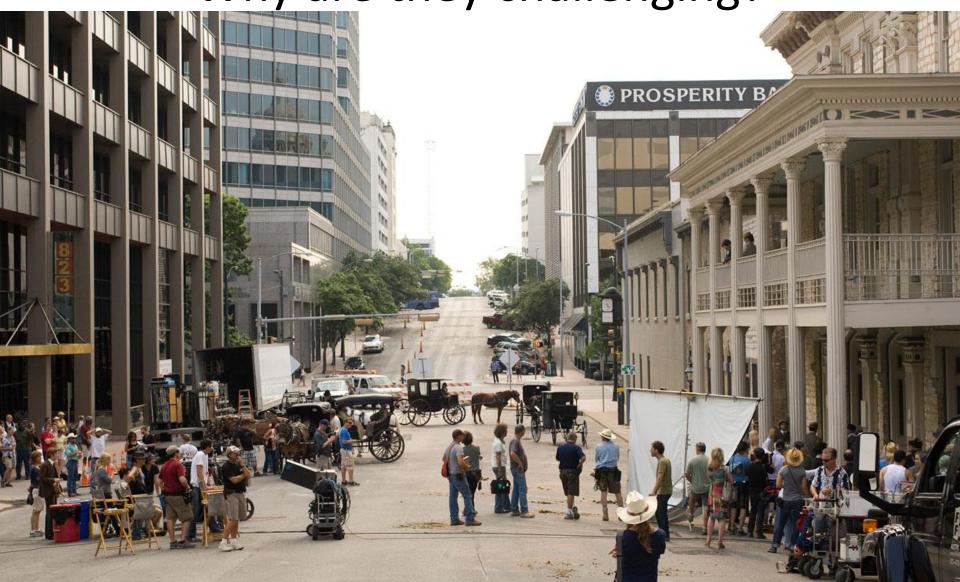


ImageNet: 22k categories, 14mil images

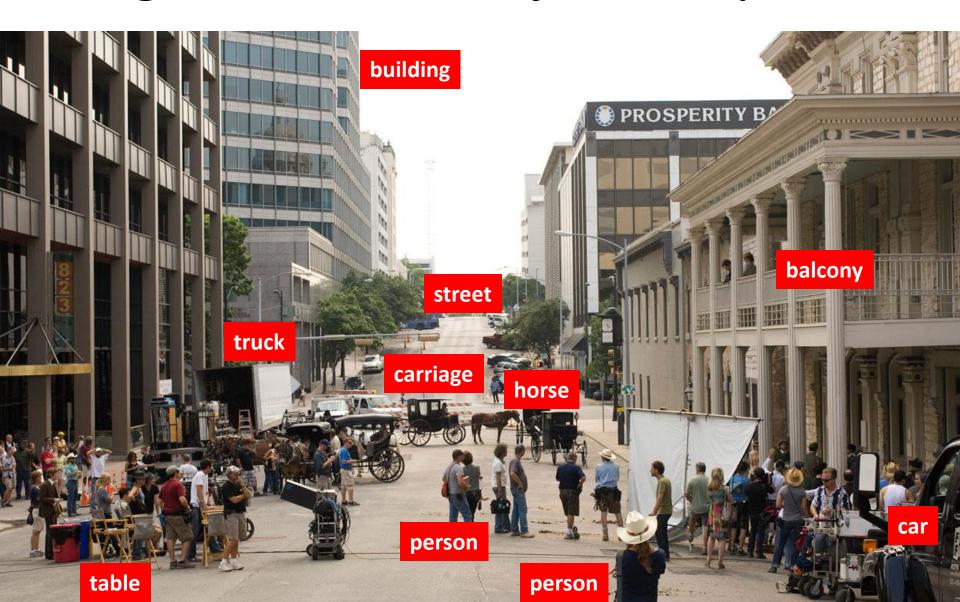


Microsoft COCO: 80 categories, 300k images

Some Visual Recognition Problems: Why are they challenging?



Recognition: What objects do you see?



Detection: Where are the cars?



Activity: What is this person doing?



Scene: Is this an indoor scene?



Instance: Which city? Which building?



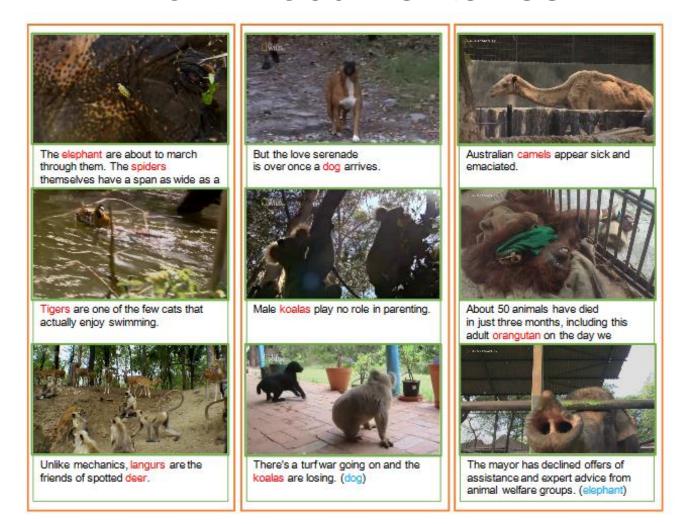
Visual question answering:

Why is there a carriage in the street?

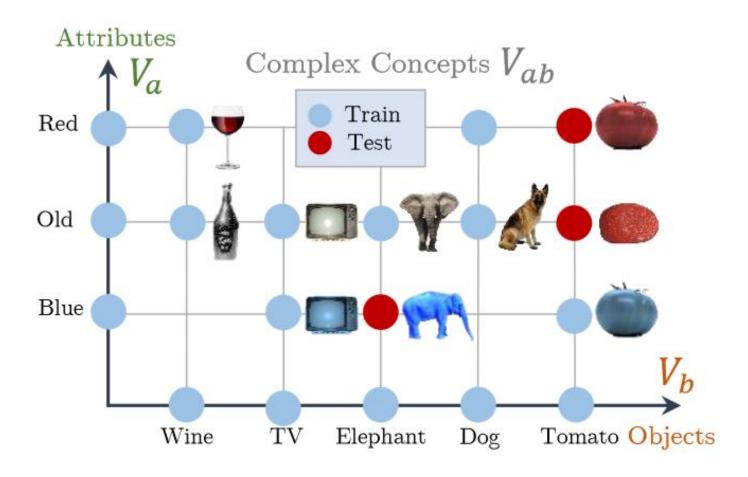


What tasks are computer vision researchers actively working on?

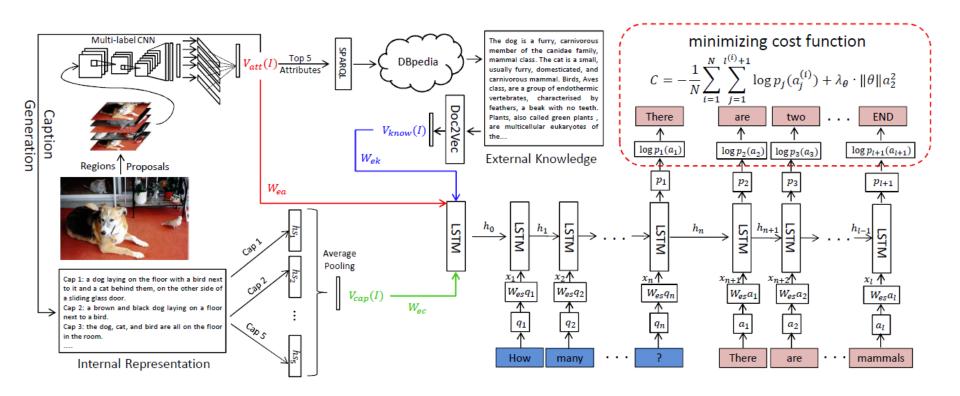
Discover and Learn New Objects from Documentaries



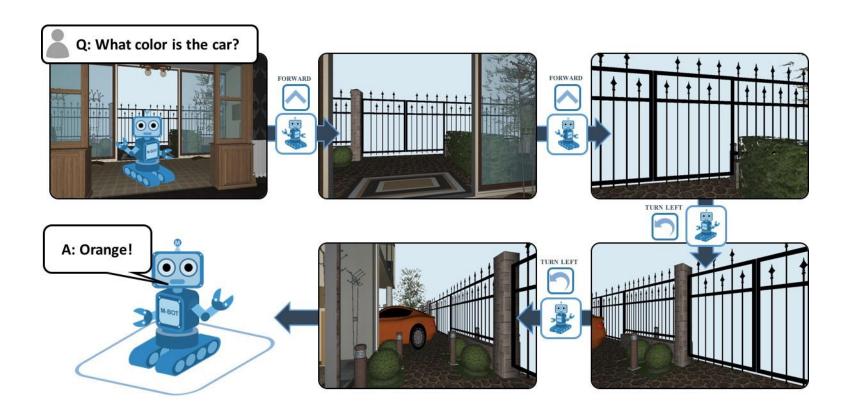
From Red Wine to Red Tomato: Composition With Context



Ask Me Anything: Free-form Visual Question Answering Based on Knowledge from External Sources



Embodied Question Answering



MovieQA: Understanding Stories in Movies through Question-Answering

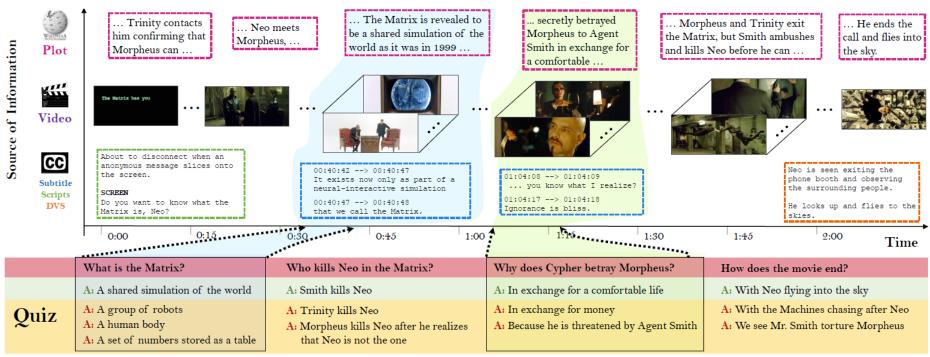


Figure 1: Our MovieQA dataset contains 14,944 questions about 408 movies. It contains multiple sources of information: plots, subtitles, video clips, scripts, and DVS transcriptions. In this figure we show example QAs from *The Matrix* and localize them in the timeline.

Automatic Understanding of Image and Video Advertisements

Zaeem Hussain, Mingda Zhang, Xiaozhong Zhang, Keren Ye, Christopher Thomas, Zuha Agha, Nathan Ong, Adriana Kovashka University of Pittsburgh



Understanding advertisements is more challenging than simply recognizing physical content from images, as ads employ a variety of strategies to persuade viewers.











Atypical Objects

We collect an advertisement dataset containing 64,832 images and 3,477 videos, each annotated by 3-5 human workers from Amazon Mechanical Turk.

Image	Topic	204,340	Strategy	20,000
	Sentiment	102,340	Symbol	64,131
	Q+A Pair	202,090	Slogan	11,130
Video	Topic	17,345	Fun/Exciting	15,380
	Sentiment	17,345	English?	17,374
	Q+A Pair	17,345	Effective	16,721

Here are some sample annotations in our dataset.



What's being advertised in

Cars, automobiles

What sentiments are provoked in the viewer?

Amused, Creative, Impressed, Youthful. Conscious



What strategies are used to persuade viewer?

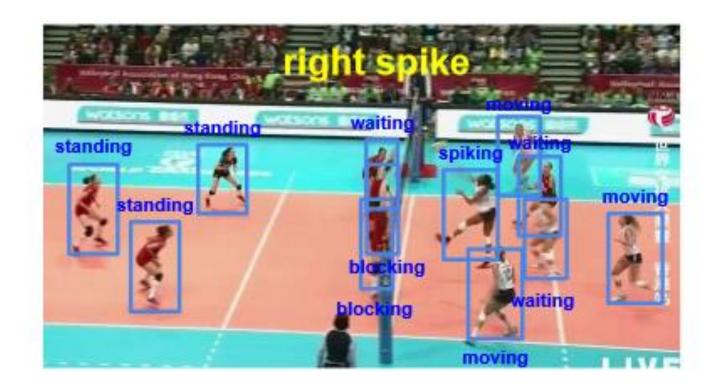
Symbolism, Contrast, Straightforward, Transferred qualities

What should the viewer do, and why should they do this?

- I should buy Volkswagen because it can hold a big bear.
- I should buy VW SUV because it can fit anything and everything in it.
- I should buy this car because it can hold everything I need.

More information available at http://cs.pitt.edu/~kovashka/ads

Social Scene Understanding: End-To-End Multi-Person Action Localization and Collective Activity Recognition



Anticipating Visual Representations from Unlabeled Video



Figure 5: **Example Action Forecasts:** We show some examples of our forecasts of actions one second before they begin. The left most column shows the frame before the action begins, and our forecast is below it. The right columns show the ground truth action. Note that our model does not observe the action frames during inference.

Generating the Future with Adversarial Transformers





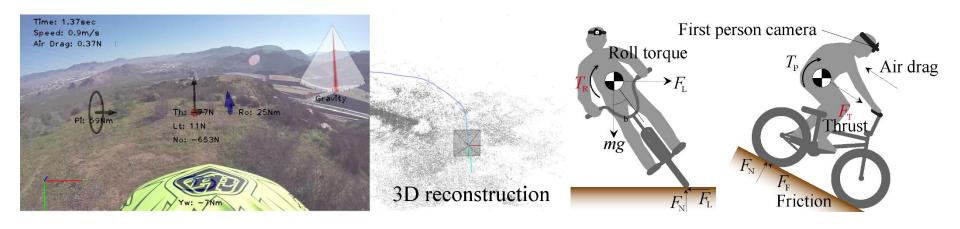








Force from Motion: Decoding Physical Sensation from a First Person Video



Scribbler: Controlling Deep Image Synthesis with Sketch and Color



Figure 1. A user can sketch and scribble colors to control deep image synthesis. On the left is an image generated from a hand drawn sketch. On the right several objects have been deleted from the sketch, a vase has been added, and the color of various scene elements has been constrained by sparse color strokes. For best resolution and additional results, see scribbler.eye.gatech.edu

What are we going to talk about?

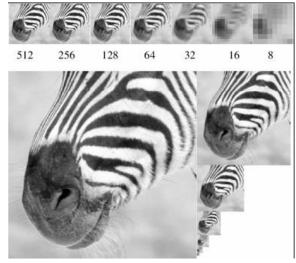
The Basics

Features and filters











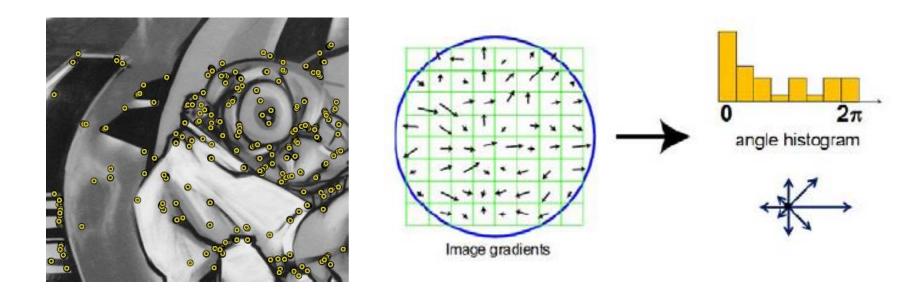




 Transforming and describing images; textures, colors, edges

Features and filters

- Detecting distinctive + repeatable features
- Describing images with local statistics



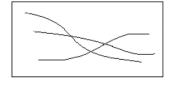
Grouping and fitting



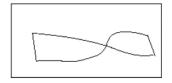
Parallelism



Symmetry



Continuity



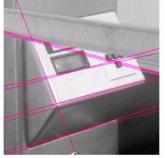
Closure

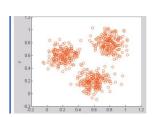
 Clustering, segmentation, fitting; what parts belong together?



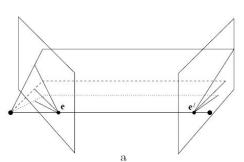
[fig from Shi et al]







Multiple views









 Multi-view geometry, matching, invariant features, stereo vision

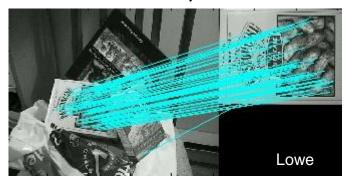
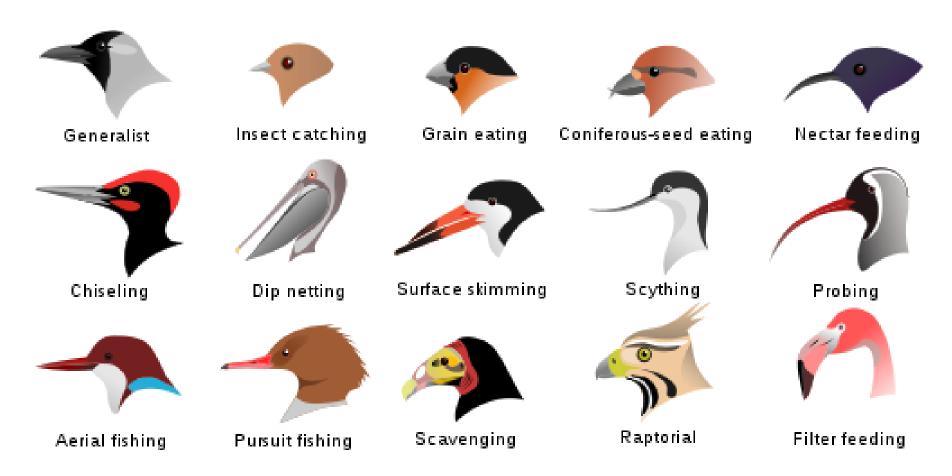




Image categorization

Fine-grained recognition



Visipedia Project

Image categorization

Material recognition







[Bell et al. CVPR 2015]

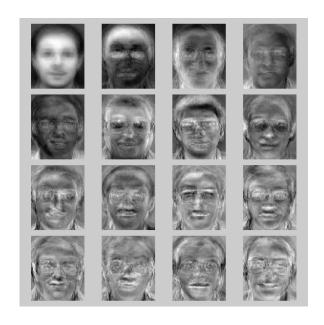
Image categorization

Image style recognition

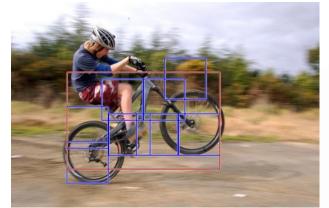


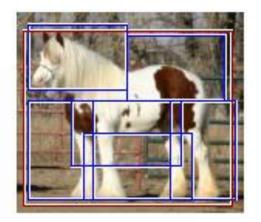
[Karayev et al. BMVC 2014]

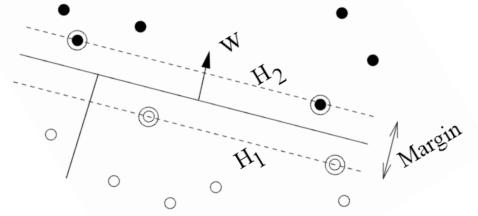
Visual recognition and SVMs







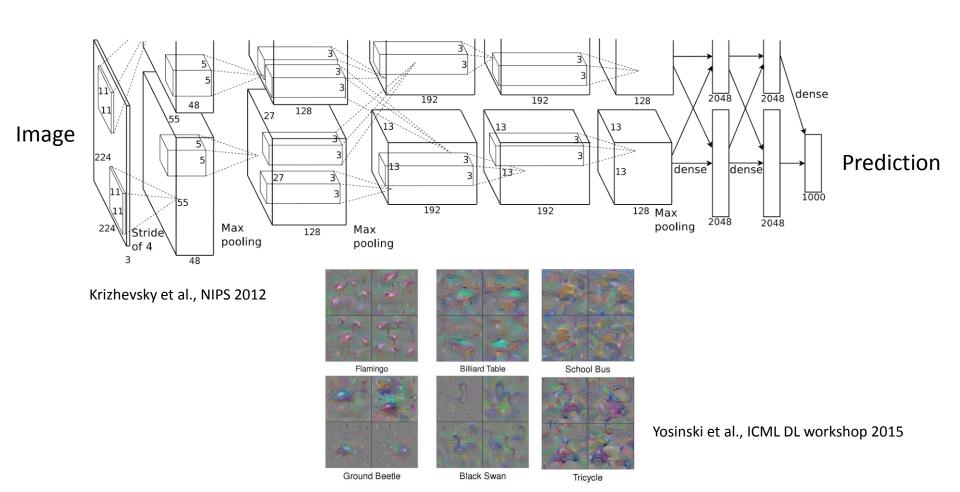




 Recognizing objects and categories, learning techniques

Convolutional neural networks (CNNs)

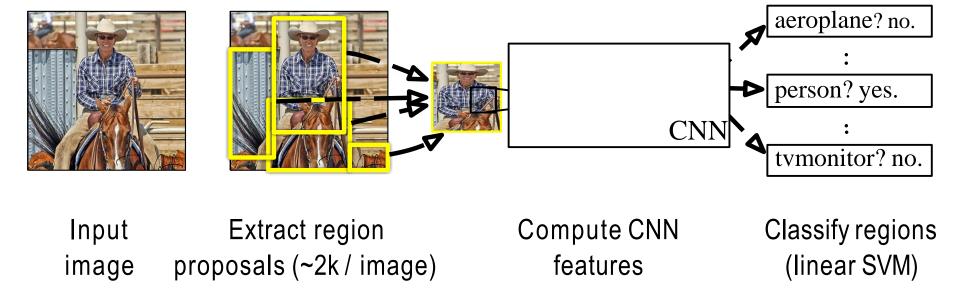
State-of-the-art on many recognition tasks



The Classics

Object Detection

Regions with CNN features



Accurate object detection in real time

	Pascal 2007 mAP	Speed	
DPM v5	33.7	.07 FPS	14 s/img
R-CNN	66.0	.05 FPS	20 s/img
Fast R-CNN	70.0	.5 FPS	2 s/img
Faster R-CNN	73.2	7 FPS	140 ms/img
YOLO	69.0	45 FPS	22 ms/img



in 2016

Our ability to detect objects has gone from 34 mAP in 2008 to 73 mAP at 7 FPS (frames per second) or 63 mAP at 45 FPS



YOLO: Real-Time Object Detection



You only look once (YOLO) is a system for detecting objects on the Pascal VOC 2012 dataset. It can detect the 20 Pascal object classes:

- person
- · bird, cat, cow, dog, horse, sheep
- · aeroplane, bicycle, boat, bus, car, motorbike, train
- bottle, chair, dining table, potted plant, sofa, tv/monitor

Recognition in novel modalities



Figure 6: Qualitative Results. YOLO running on sample artwork and natural images from the internet. It is mostly accurate although it does think one person is an airplane.

Vision and Language

Image Captioning

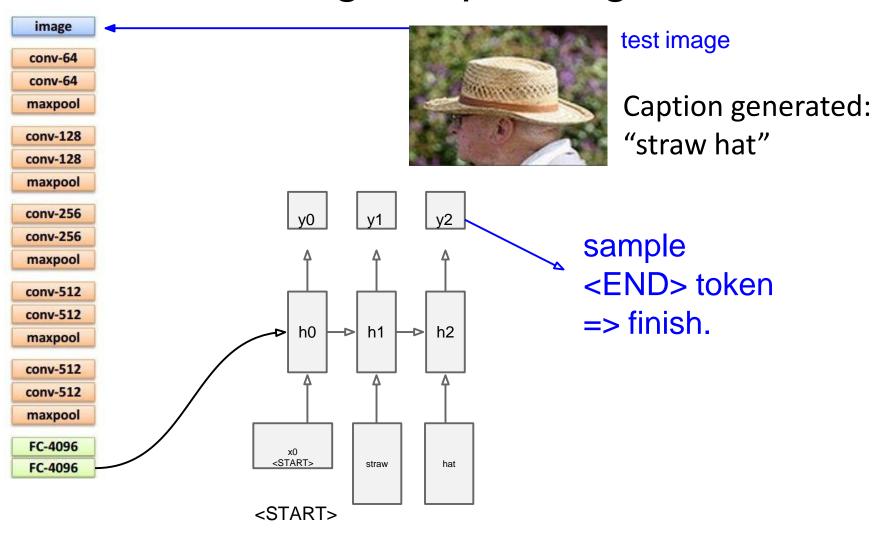


Image Captioning



"man in black shirt is playing guitar."



"construction worker in orange safety vest is working on road."



"two young girls are playing with lego toy."



"boy is doing backflip on wakeboard."



"a young boy is holding a baseball bat."



"a cat is sitting on a couch with a remote control."



"a woman holding a teddy bear in front of a mirror."



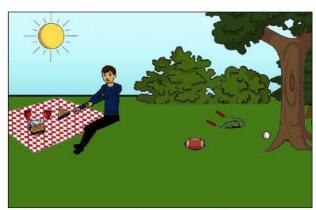
"a horse is standing in the middle of a road."

Visual Question Answering (VQA)

Task: Given an image and a natural language open-ended question, generate a natural language answer.



What color are her eyes? What is the mustache made of?



Is this person expecting company? What is just under the tree?



How many slices of pizza are there? Is this a vegetarian pizza?



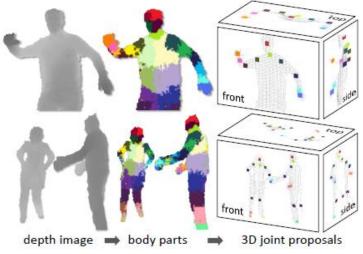
Does it appear to be rainy? Does this person have 20/20 vision?

Video and Motion

Tracking and Pose

- Tracking objects, video analysis
- Automatically annotating human pose (joints)



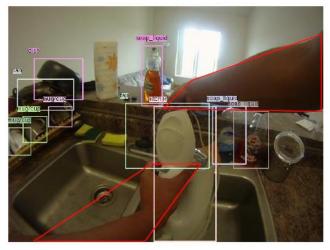


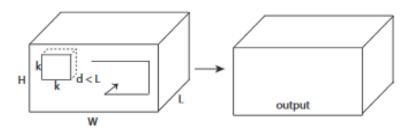
Recognizing Actions

Actions in movies, sports, first-person views







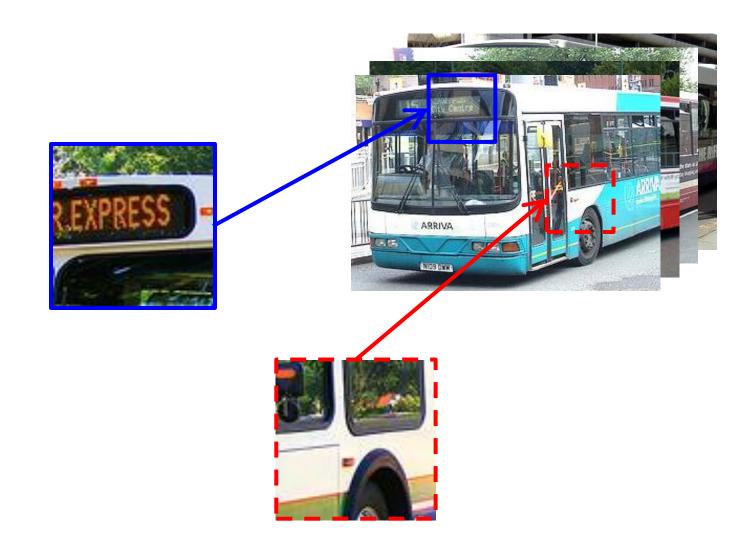


Emergent Topics

Self-Supervised Learning

Context Prediction for Images

Semantics from a non-semantic task



Embodied learning

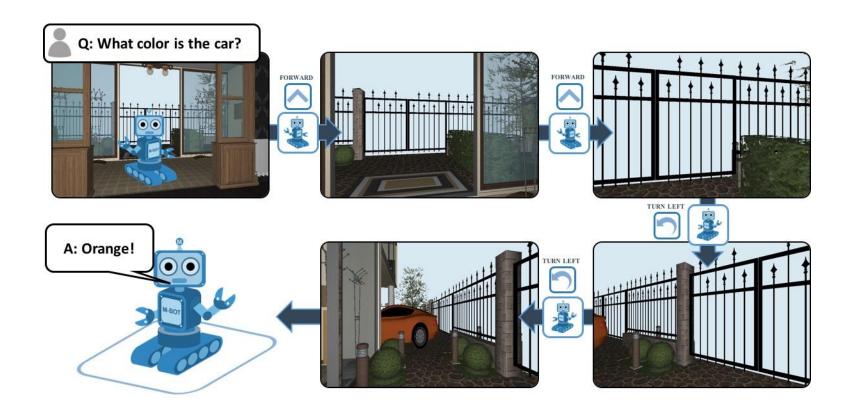
Status quo: Learn from "disembodied" bag of labeled snapshots.



Goal: Learn in the context of acting and moving in the world.



Embodied QA with reinforcement learning

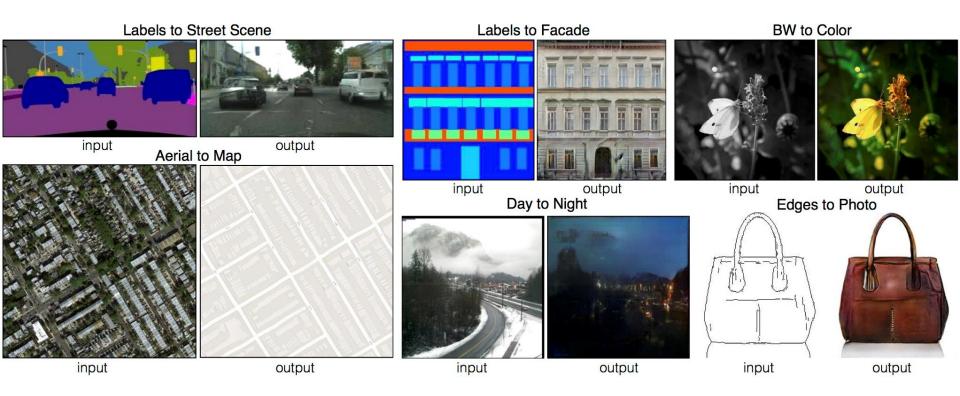


Generative Models

Celebrities Who Never Existed



Image-to-Image Translation with Conditional Adversarial Nets



Is computer vision solved?

- Given an image, we can guess with 96% accuracy what object categories are shown (ResNet)
- ... but we only answer "why" questions about images with 14% accuracy!

Why does it seem like it's solved?

- Deep learning makes excellent use of massive data (labeled for the task of interest?)
 - But it doesn't work well when massive data is not available and your task is different than tasks for which data is available
 - It's hard to understand how it does so

Linear Algebra Review

What are images? (in Matlab)

- Matlab treats images as matrices of numbers
- To proceed, let's talk very briefly about how images are formed

Image formation Illumination (energy) source Imaging system

(Internal) image plane (film)

Scene element

Digital camera

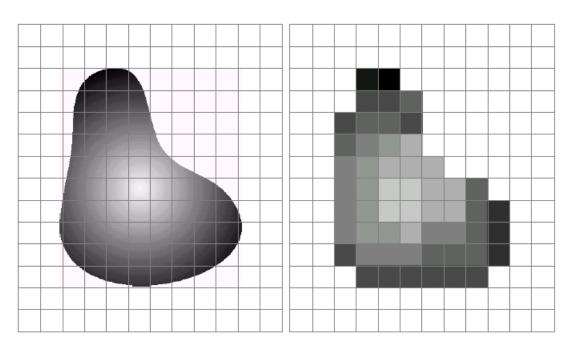


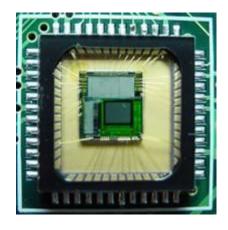
A digital camera replaces film with a sensor array

 Each cell in the array is light-sensitive diode that converts photons to electrons

http://electronics.howstuffworks.com/cameras-photography/digital/digital-camera.htm

Digital images





a b

FIGURE 2.17 (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.

- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)

Digital images

- Sample the 2D space on a regular grid
- Quantize each sample (round to nearest integer)
- What does quantizing signal look like?

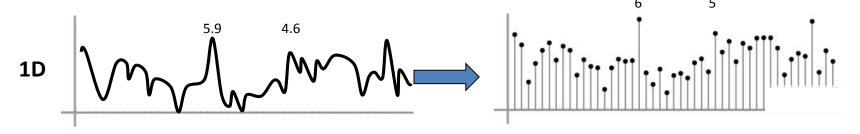
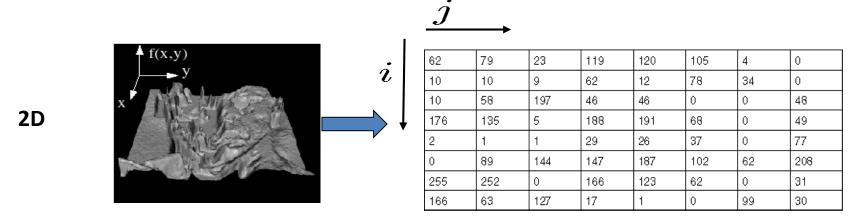
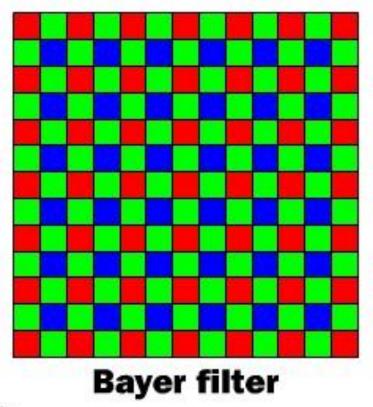


Image thus represented as a matrix of integer values.



Adapted from S. Seitz

Digital color images

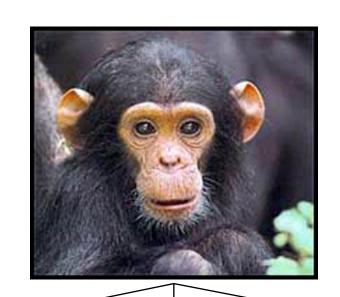


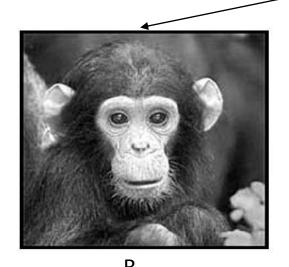
© 2000 How Stuff Works

Digital color images

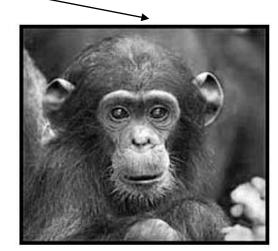
Color images, RGB color space:

Split image into three channels









G B Adapted from Kristen Grauman

Images in Matlab

- Color images represented as a matrix with multiple channels (=1 if grayscale)
- Suppose we have a NxM RGB image called "im"
 - im(1,1,1) = top-left pixel value in R-channel
 - im(y, x, b) = y pixels down, x pixels to right in the bth channel
 - im(N, M, 3) = bottom-right pixel in B-channel
- imread(filename) returns a uint8 image (values 0 to 255)
 - Convert to double format with double or im2double

		colu	ımn														
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. •	-	0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99					
		0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91			_		
		0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92	0.92 0.99	l n aa	_I G		
		0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95		0.91	-		_
		0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.93				B
		0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.91	1	0.92	0.99	
		0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74		0.95	0.95	0.91	
		0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.79	0.85	0.91	0.92	
		0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.45	0.49 0.74	0.97	0.95	
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				0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.82	0.93	
				0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	
						0.03	0.73	0.50	0.67	0.73	0.72	0.77	0.70	0.71			
						0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
						0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

Vectors and Matrices

- Vectors and matrices are just collections of ordered numbers that represent something: movements in space, scaling factors, word counts, movie ratings, pixel brightnesses, etc.
- We'll define some common uses and standard operations on them.

Vector

• A column vector $\mathbf{v} \in \mathbb{R}^{n \times 1}$ where

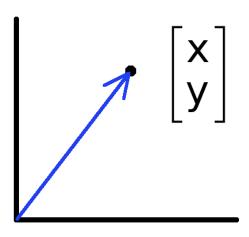
$$\mathbf{v} = \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{bmatrix}$$

• A row vector $\mathbf{v}^T \in \mathbb{R}^{1 \times n}$ where

$$\mathbf{v}^T = \begin{bmatrix} v_1 & v_2 & \dots & v_n \end{bmatrix}$$

 ${\cal T}$ denotes the transpose operation

Vectors have two main uses



- Vectors can represent an offset in 2D or 3D space
- Points are just vectors from the origin

- Data can also be treated as a vector
- Such vectors don't have a geometric interpretation, but calculations like "distance" still have value

Matrix

• A matrix $A \in \mathbb{R}^{m \times n}$ is an array of numbers with size $m \downarrow$ by $n \rightarrow$, i.e. m rows and n columns.

$$\mathbf{A} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & \dots & a_{1n} \\ a_{21} & a_{22} & a_{23} & \dots & a_{2n} \\ \vdots & & & & \vdots \\ a_{m1} & a_{m2} & a_{m3} & \dots & a_{mn} \end{bmatrix}$$

• If m=n , we say that ${\bf A}$ is square.

Addition

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} = \begin{bmatrix} a+1 & b+2 \\ c+3 & d+4 \end{bmatrix}$$

Can only add matrices with matching dimensions,
 or a scalar to a matrix.

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} + 7 = \begin{bmatrix} a+7 & b+7 \\ c+7 & d+7 \end{bmatrix}$$

Scaling

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \times 3 = \begin{bmatrix} 3a & 3b \\ 3c & 3d \end{bmatrix}$$

- Inner product (*dot* · product) of vectors
 - Multiply corresponding entries of two vectors and add up the result
 - We won't worry about the geometric interpretation for now

$$\mathbf{x}^T \mathbf{y} = \begin{bmatrix} x_1 & \dots & x_n \end{bmatrix} \begin{bmatrix} y_1 \\ \vdots \\ y_n \end{bmatrix} = \sum_{i=1}^n x_i y_i \quad \text{(scalar)}$$

Inner vs outer vs matrix vs element-wise product

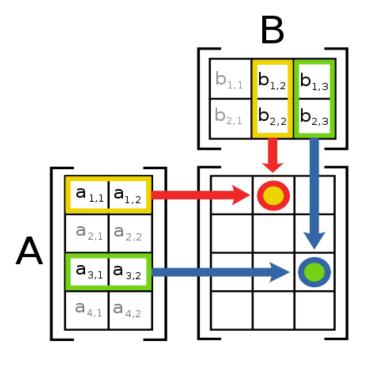
- x, y = column vectors (nx1)
- X, Y = matrices (mxn)
- x, y = scalars (1x1)
- $x \cdot y = x^T y = inner product (1xn x nx1 = scalar)$
- $x \otimes y = x y^T = \text{outer product (nx1 x 1xn = matrix)}$
- **X** * **Y** = matrix product
- X.* Y = element-wise product

Matrix Multiplication

- Let X be an axb matrix, Y be an bxc matrix
- Then Z = X*Y is an $\alpha x c$ matrix
- Second dimension of first matrix, and first dimension of first matrix have to be the same, for matrix multiplication to be possible
- Practice: Let X be an 10x5 matrix. Let's factorize it into 3 matrices...

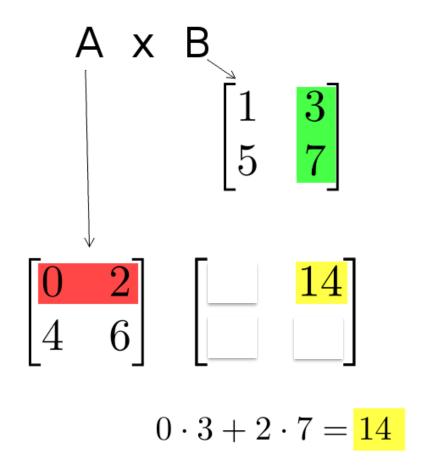
Multiplication

The product AB is:



 Each entry in the result is (that row of A) dot product with (that column of B)

Multiplication example:



 Each entry of the matrix product is made by taking the dot product of the corresponding row in the left matrix, with the corresponding column in the right one.

Matrix Operation Properties

Matrix addition is commutative and associative

$$-A + B = B + A$$

 $-A + (B + C) = (A + B) + C$

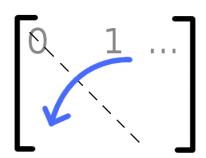
 Matrix multiplication is associative and distributive but not commutative

$$-A(B*C) = (A*B)C$$

$$-A(B+C) = A*B+A*C$$

$$- A*B != B*A$$

 Transpose – flip matrix, so row 1 becomes column 1



$$\begin{bmatrix} 0 & 1 \\ 2 & 3 \\ 4 & 5 \end{bmatrix}^T = \begin{bmatrix} 0 & 2 & 4 \\ 1 & 3 & 5 \end{bmatrix}$$

A useful identity:

$$(ABC)^T = C^T B^T A^T$$

Special Matrices

- Identity matrix I
 - Square matrix, 1's along diagonal, 0's elsewhere
 - I · [another matrix] = [that matrix]

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

- Diagonal matrix
 - Square matrix with numbers along diagonal, 0's elsewhere
 - A diagonal [another matrix]
 scales the rows of that matrix

$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 2.5 \end{bmatrix}$$

Norms

• L1 norm

$$\left\|oldsymbol{x}
ight\|_1 := \sum_{i=1}^n \left|x_i
ight|$$

L2 norm

$$\|oldsymbol{x}\| := \sqrt{x_1^2 + \cdots + x_n^2}$$

• L^p norm (for real numbers $p \ge 1$)

$$\left\|\mathbf{x}
ight\|_p := \left(\sum_{i=1}^n \left|x_i
ight|^p
ight)^{1/p}$$

Your Homework

- Read entire course website
- Do first reading
- Fill out Doodle for TA's office hours
- Sign up to be a panelist
- Sign up for Piazza
- Start thinking about your project!