

Recursion

- n A problem solving technique where an algorithm is defined in terms of itself
- n A recursive method is a method that calls itself
- n A recursive algorithm breaks down the input or the search space and applies the same logic to a smaller and smaller piece of the problem until the remaining piece is solvable without recursion.
- n Sometimes called “divide and conquer”

Recursion vs. Iteration

- n in general, any algorithm that is implemented using a loop can be transformed into a recursive algorithm
- n moving in the reverse direction is not always possible unless you maintain an additional data structure (stack) yourself.

Recursion Analysis

- n in general, recursive algorithms are
 - | more efficient
 - | more readable (but occasionally quite the opposite!)
 - | more “elegant”

- n side effects
 - | mismanagement of memory
 - | “over head” costs

Recursion Components

- n Solution to the “base case” problem
 - | for what values can we solve without another recursive call?’
- n Reducing the input or the search space
 - | modify the value so it is closer to the base case
- n The recursive call
 - | Where do we make the recursive call?
 - | What do we pass into that call?

How recursion works

When a method calls itself – it is just as if that method is calling some other method. It is just a coincidence that the method has the same name, args and code. A recursive method call creates an identical copy of the calling method and everything else behaves as usual.

Think of the method as a rectangle containing that method's `**code` and data, and recursion is just a layering or tiling of those rectangles with information passing to with each call and information returning from each call as the method finishes.

(`** code` is not actually stored in the call stack)

GCD Algorithm

given two positive integers X and Y ,

where $X \geq Y$,

the $\text{GCD}(X, Y)$ is

- | equal to Y if $X \bmod Y = 0$
 - | else
- | equal to the $\text{GCD}(Y, X \bmod Y)$

- | Algorithm terminates when the $X \% Y$ is zero.
- | Notice that each time the function calls it self, the 2nd arg gets closer to zero and must eventually reach zero.

What is the output of this program?

```
public void foo( int x)
{
    if (x ==0)
        return;
    else
        {   System.out.println( x );
            foo( x - 1 );
        }
}
public static void main( String args[])
{
    foo( 7 );
}
```

** Identify the Base case, recursive call and reduction / modification of the input toward the base case.

What is the output of this program?

```
public int foo( int x)
{
    if (x ==0)
        return 0;
    else
        return x + foo(x-1);
}
public static void main( String args[])
{
    System.out.println( foo(7) );
}
```

** Identify the Base case, recursive call and reduction / modification of the input toward the base case.

What is the output of this program?

```
public int foo( int x, int y)
{
    if (x == 0)
        return y;
    else
        return foo( x-1, y+1 );
}
public static void main( String args[] )
{
    System.out.println( foo( 3, 4 ) );
}
```

** Identify the Base case, recursive call and reduction or modification of the input toward the base case.

What is the output of this program?

```
public int foo( int x, int y )
{
    if (x == 0)
        return y;
    else
        return foo( x-1, y+x );
}
public static void main( String args[])
{
    System.out.println( foo( 3, 4 ) );
}
```

Now.. You help me write this

- n Write a recursive function that accepts an int and prints that integer out in reverse on 1 line
- n What is the base case ?
- n How do I reduce the input toward base case ?
- n What do I pass to the recursive call ?

One more try!

- n Write a recursive function that accepts a string and prints that string out in reverse on 1 line.
- n What is the base case ?
- n How do I reduce the input toward base case ?
- n What do I pass to the recursive call ?

Other Examples ...

- n Bad examples (but for illustration/teaching)
 - | factorial
 - | exponential
 - | Fibonacci numbers
 - | power

Other Examples ...

n Good examples

- | Towers of Hanoi
- | GCD
- | Eight Queens
- | Binary Search Trees
- | Maze traversal
- | Backtracking (i.e recovery from dead ends)

Tail Recursion optimization

- n Recursion can use up a lot of memory very quickly!
- n The compiler can generate assembly code that is iterative but guaranteed to compute the exact same operation as the recursive source code.
- n It only works if the very last statement in your method is the recursive call. This is tail recursion.
- n Java does not tail optimize recursive code.