

1. $(\text{Cube}(a) \wedge \text{Small}(a)) \vee \text{Small}(b)$

2. $\text{Cube}(a) \wedge \text{Small}(a)$

3. $\text{Small}(a)$

✓ \wedge **Elim** 2

4. $\text{Small}(a) \vee \text{Small}(b)$

✓ \vee **Intro** 3

5. $\text{Small}(b)$

6. $\text{Small}(a) \vee \text{Small}(b)$

✓ \vee **Intro** 5

7. $\text{Small}(a) \vee \text{Small}(b)$

✓ \vee **Elim** 1,2-4,5-6

1. $(P \vee Q \vee R) \rightarrow S$

2.  Q

3. $P \vee Q \vee R$

4. S

5. $Q \rightarrow S$

 \vee **Intro** 2

 \rightarrow **Elim** 3,1

 \rightarrow **Intro** 2-4

1. $\neg Q \rightarrow \neg P$

2. P

3. $\neg Q$

4. $\neg P$

5. \perp

6. $\neg\neg Q$

7. Q

8. $P \rightarrow Q$

✓ \rightarrow Elim 3,1

✓ \perp Intro 4,2

✓ \neg Intro 3-5

✓ \neg Elim 6

✓ \rightarrow Intro 2-7

1. $\neg(A \wedge B)$

2. $B \vee C$

3. $C \rightarrow D$

4. A

5. B

6. $A \wedge B$

7. \perp

8. $\neg B$

9. B

10. \perp

11. C

12. C

13. C

14. C

15. D

16. $A \rightarrow D$

✓ \wedge Intro 4,5

✓ \perp Intro 1,6

✓ \neg Intro 5-7

✓ \perp Intro 8,9

✓ \perp Elim 10

✓ Reit 12

✓ \vee Elim 2,9-11,12-13

✓ \rightarrow Elim 3,14

✓ \rightarrow Intro 4-15