Not All Samples Are Equal: Class Dependent Hierarchical Multi-Task Learning for Patient Diagnosis Classification

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Abstract
An interesting machine learning problem is to learn predictive models that can automatically assign diagnoses or diagnostic categories to patient cases. However, we often do not have enough positive samples for many of diagnoses either due to their rare nature or a limited size of available datasets. This motivates the use of multi-task learning methods that tend to improve model performance by imposing model similarities between related tasks. In this work, we tackle this important problem by exploring the benefits of existing expert-defined diagnostic hierarchies. We argue that related tasks (models) organized in expert-defined hierarchies do not have the same level of similarity for different classes of samples. We discuss how task similarities will be different for positive and negative samples and between parent and child diagnoses. We propose a new asymmetric version of Hierarchical Adaptive Multi-task Learning (HA-MTL) method (Malakouti and Hauskrecht 2019b).

In the rest of this paper, we first provide introductory information on Hierarchical Adaptive Multi-task Learning (HA-MTL) method (Malakouti and Hauskrecht 2019b). Next we study how HA-MTL is imposing similarities among the tasks in top-down and bottom-up transfer of model parameters. Next, we propose a new hierarchical version of HA-MTL method that allows asymmetric class dependent between behaviour of related models. However, past work has shown that multi-task learning methods can result in negative transfer if task similarities are not properly formulated (Rosenstein et al. 2005; Pan and Yang 2010) Therefore, past research work have proposed methods that model relationships between tasks by learning tasks relatedness coefficients (Ben-David and Schuller 2003; Kang, Grauman, and Sha 2011), creating task clusters, or by considering hierarchical structure of tasks (Jacob, Vert, and Bach 2009; Zhou, Chen, and Ye 2011a; Kumar and Daume III 2012).

In this paper we argue that it is important not only to consider which tasks to transfer from but also when to transfer from them as similarity does not imply that models' behaviour will be similarly related for all examples. In hierarchical settings such as patient diagnoses classification problem, parent diagnostic categories include similar groups of diagnostic codes. Therefore, there will be similarities between the diagnostic parent’s predictions and its children. This has motivated methods that allow transfer of model parameters in a top-down fashion (Dumais and Chen 2000; Wu, Zhang, and Honavar 2005). However, one can argue that this adaptation may not be symmetric for positive and negative classes (in binary classification tasks). In other words, it is intuitive to think that negative class label of the parent diagnostic task is more likely to translate to a negative class label of its particular children, however, it is not possible to make the same claim for positive instances. In fact we often expect positive class label of the parent to imply that at least one but not all child tasks to have positive class as well. Therefore, imposing same weight for the parent diagnostic model for both classes during a top-down learning mechanism seems counter intuitive. One would expect that the relatedness of parent and child tasks to be asymmetric instead, but to the extent of our knowledge none of the existing work have studied this in hierarchical multi-task learning settings.

Introduction
Large scale adoption of Electronic Health Records (EHR) has facilitated many interesting problems such as automatic classification of patient diagnoses and diagnostic categories. Automatic classification and assignment of diagnoses at different levels of abstraction during patient’s hospitalization is extremely useful for concisely summarizing the patient’s condition. Additionally, it helps one explaining the patient’s condition, as well as defining a proper context for choosing future patient management actions, or for supporting prediction and estimation of future outcomes.

However, a problem one often encounters when learning such classification models from data is that the number of positive samples available for some of the diagnoses (diagnostic codes) is very small. This is either due to the rare nature of the diseases or a limited size of available datasets. This motivates the use of multi-task learning methods that can take advantage of available data for similar diagnostic tasks. This is achieved by imposing similarities
adaptation of model behaviours by learning class specific relatedness coefficients. Finally, we show our method can learn models with improved classification performance and analyze the difference between model adaptation from parent diagnostic categories for positive and negative classes.

Related Work

The problem of modelling patient wide range of diagnoses has recently become a focus of machine learning research. Some of existing work tackle the problem of predicting future admission diagnoses using past history of patients (Lipton et al. 2015; Choi et al. 2017) while others have taken on the challenge of assigning diagnostic codes to current patient’s visit (Pakhomov, Buntrock, and Chute 2006; Miotto et al. 2016). Recently new methods have been proposed to take advantage of hierarchical structure of patient diagnoses to expand the training features (Choi et al. 2017). Other methods have attempted to leverage task hierarchies to improve learning of diagnostic models using hierarchical classification methods (Perotte et al. 2013) and finally new methods have been proposed to use the hierarchical relationships of diagnostic codes in multi-task learning settings (Malakouti and Hauskrecht 2019a).

Hierarchical Multi-task learning for large number of tasks is closely related to the two types of machine learning methods: Hierarchical Learning and Multi-task Learning itself. In the hierarchical learning community top-down learning of machine learning models have been commonly studied before (Koller and Sahami 1997). In the top-down approach a classifier on a low-level of the hierarchy is defined using a decision or a signal generated by its parent classifiers. There are different versions of the top-down approach that place various consistency constraints on predictions of the parent and child tasks and their classifier outputs, most frequently assuring the probability of a parent (diagnostic category) is higher than the probability of a low-level class or class category (Dumais and Chen 2000; Wu, Zhang, and Honavar 2005). The main problem with the top-down approach is that learning of higher level class models from data may omit details that the low-level class models could capture. For example, some of the findings for a patient may point specifically and with a high accuracy to a low-level diagnosis while the higher level class model marginalizes it out during the learning and as a result does not include it in the model. In such a case the probability of a lower-level class may be higher than the probability of a higher level class category violating the constraint consistency. One way to correct for child-to-parent effects is to define and add a bottom-up process that assures positive lower-level class predictions aggregate properly in the parent tasks (Valentini 2011). However, pure bottom-up approach would require the presence of accurate classifier models on the leaf classification layer, which is hard to achieve in practice when datasets of a limited size are used to train such models and the count of positive instances for such classes are very low. There exists a variety of hierarchical classification methods that try to account for both the top-down and bottom-up classification processes. One example is a Bayesian aggregation method by (DeCoro and Barutcuoglu 2006) that compiles the hierarchy into the Bayesian belief network and uses inferences to support the classification on a different level of hierarchy. Other methods that account for both top-down (negative) and bottom-up (positive) effects are based on structured margin classifiers (Dekel, Keshet, and Singer 2004).

Multi-task learning methods tackle this problem by devising machine learning algorithms that tend to improve individual task performance by simultaneously learning of all tasks (Zhang and Yang 2017). These methods tend to promote sharing of information between related tasks by imposing similarities between them. Evgeniou and Pontil proposed a multi-task learning method based on SVM algorithm that learns all tasks simultaneously by regularizing their differences from their average (Evgeniou and Pontil 2004). Other methods have been proposed to tackle this problem by performing shared feature learning (Argyriou, Evgeniou, and Pontil 2007; 2008).

It has been shown that multi-task learning methods are highly sensitive to relatedness of tasks, and if not modeled properly, they can result in negative transfer (Rosenstein et al. 2005; Pan and Yang 2010). One approach to solve this problem is to explicitly model and learn task relationships (Ben-David and Schuller 2003; Kang, Grauman, and Sha 2011; Zhang and Yeung 2012; Zhou, Chen, and Ye 2011b). The second group of methods attempted to learn task groups or clusters to prevent negative transfer from unrelated tasks (Jacob, Vert, and Bach 2009; Zhou, Chen, and Ye 2011a; Kumar and Daume III 2012). However, none of these methods take advantage of the complex hierarchical relationships between tasks when they are organized in hierarchies. Some earlier work have studied and proposed hierarchical multi-task learning problem in which task relationships cannot simply be modeled using flat task clusters (Liu et al. 2017; Kim and Xing 2010; Xue et al. 2007; Malakouti and Hauskrecht 2019a). However, there are yet many open questions to be answered. One interesting question is to investigate whether positive transfer of model parameters between tasks happen equally across different classes. In other words, are the negative samples and positive samples equally important in imposing similarities between related tasks.

In the rest of this section we first review HA-MTL method and propose an asymmetric class dependent extension for it called asymmetric HA-ML. Next we evaluate our method’s performance on the patient diagnosis classification task and study class-dependent transfer weights.

Methodology

Assume we have $T$ diagnoses and diagnostic categories, each covered by a separate binary classification task. The tasks are organized in a hierarchical structure $H$. Additionally, we assume each patient’s $X \in \mathbb{R}^D$ consists a $D$ dimensional dense representation of patient’s EHR data. Our objective is to learn $T$ discriminant functions $f_1, f_2, \ldots, f_T$ in which $f_t : \mathbb{R}^D \rightarrow \mathbb{R}$. Hence, the predicted score of the discriminant function $f_t$ can be mapped to one of the binary labels 0, 1 using a task specific threshold $\gamma_t$. Finally, we introduce a $\phi_t, H$ as the parent of tasks $t$ in the hierarchy $H$. 
The conventional method is to learn the $T$ discriminant functions independently. However, recent work has shown that by adapting model parameters in a top-down fashion one can improve lower level diagnostic models by taking advantage of more general diagnostic models trained for their parent diagnostic categories. In this section, we first formalize Hierarchical Adaptive Multi-task Learning method (Malakouti and Hauskrecht 2019a). Next, we show that the transfer of model parameters is achieved by minimizing the difference between the target task parameters and a weighted sum of auxiliary tasks. Finally, we propose a new class dependent extension of HA-MTL that allows class dependent asymmetric adaptation from parent diagnostic models.

**HA-MTL: Hierarchical Adaptive Multi-task Learning**

HA-MTL’s goal is to adapt model parameters from parent and child diagnostic tasks while simultaneously learning the importance of the set of auxiliary models. They define the set of auxiliary tasks for the target task $t$ as the set of its parent and child diagnostic tasks. HA-MTL improves each diagnostic task in an iterative fashion by proposing a two phase (top-down and bottom-up) adaptation algorithm that transfers model parameters from either their parent or child diagnostic models. In order to perform the model parameter adaptation and simultaneously learn the importance of auxiliary task they propose Regularized Adaptive SVM (RA-SVM) as shown in equation 1.

$$\min_{v_t, \varepsilon, \tau} \sum_{i}^{N_t} \varepsilon_i + C_1 \|v_t\|^2 + C_2 \|\tau\|^2$$

$$s.t. \quad y_i \sum_{a \in aux(t)}^{aux(t)} \tau_a f_a(x_i) + y_i v_t^T x_i \geq 1 - \varepsilon_i \quad (1)$$

Where $v_t$ corresponds to the model parameters for $\Delta f_t = f_t - \sum_{a \in aux(t)}^{aux(t)} \tau_a f_a$ and $\tau_a$ refers to the relatedness or usefulness coefficient of auxiliary task $a$ for target task $t$. The function $aux(t)$ provides the set of auxiliary tasks of $t$ in the corresponding top-down or bottom-up step. Finally, values of $C_1$ and $C_2$ determine the trade-off between regularizing model parameters and auxiliary task weights. The optimization problem in Equation 1 is minimizing the hinge loss while also regularizing both the auxiliary task weights and model parameters of $\Delta f_t$.

RA-SVM improves upon Adaptive SVM algorithm first proposed by Yang et al. (Yang, Yan, and Hauptmann 2007). The advantage of RA-SVM is two fold. First, it attempts to simultaneously learn the importance of each auxiliary task, while, the original A-SVM method relied on input to provide this information. Second, RA-SVM can be optimized using any standard SVM library by relaxing the assumption that $\sum_{a \in aux(t)}^{aux(t)} \tau_a = 1$ in which $\tau_a$ is the influence of auxiliary task $a$. This is done by defining a feature map over the original features and prediction scores of auxiliary tasks.

**Lemma 1.** RA-SVM finds a trade off between imposing similarities between the predictions of the target task and the weighted average predictions of the auxiliary task models while regularizing auxiliary task weights or in other words learning the target task independently.

This can be shown by re-writing the optimization problem in Equation 1 and by replacing $f_a(x_i)$ with $w_a^T x_i$ assuming all auxiliary tasks are trained using linear models. Additionally, the final model parameters for task $t$ can be written as $w_t = \sum_a \tau_a w_a^T x_i + v_t$. Therefore, Equation 1 can be re-written as:

$$\min_{v_t, \varepsilon, \tau} \sum_{i}^{N_t} \varepsilon_i + C_1 \|w_t - \sum_{a \in aux(t)}^{aux(t)} \tau_a w_a^T \|^2$$

$$+ C_2 \|\tau\|^2$$

$$s.t. \quad y_i w_t^T x_i \geq 1 - \varepsilon_i \quad (2)$$

$$i = 1, ..., N_t, \quad \varepsilon_i \geq 0$$

The term $\|w_t - \sum_a \tau_a w_a^T\|$ in Equation 2 attempts to regularize the difference between target task model outcomes from the weighted average of the auxiliary tasks. This is while $\|\tau\|^2$ promotes smaller influence of auxiliary tasks. This creates a trade-off between masking the impact of unnecessary auxiliary tasks and imposing similarities between the target task and chosen auxiliary tasks. In fact high values of $C_2$ promotes further regularization of $\|w_t - \sum_a \tau_a w_a^T\|$ and therefore promotes higher impact of auxiliary weights. On the other hand lower ratios of $C_1$ and $C_2$ promote independent learning of target task.

**Not All Samples are Equal**

RA-SVM method assumes the signal from auxiliary tasks are equally useful in improving target task model’s performance. However, intuitively one can imagine that auxiliary model scores in a hierarchical structure can have different meaning or impact based on the type of the dependency between related tasks. For instance, in the top-down adaptation phase a negative score of parent model (assuming parent model has a higher performance) is more likely to translate to a negative label for the child task. In contrast, a positive class prediction of the parent may not necessarily mean that the child task will also be positive. As previously discussed in the hierarchical classification literature (Silla and Freitas 2011) negative samples in a hierarchy are passed top-down while positive class samples are promoted in a bottom-up fashion. Therefore, in this work, we propose an asymmetric adaptation mechanism based on ReLU operation to break down the scores of RASVM models to a pair of class dependent signals $f^+_a = \max(0, f_a)$ and $f^-_a = \min(0, f_a)$.

The signals $f^+_a \in [0, \infty]$ and $f^-_a \in [\infty, 0]$ allow target task models to learn two different relatedness coefficients $\tau^+_{a}$ and $\tau^-_{a}$ for positive and negative signals from auxiliary tasks. RA-SVM optimization problem in Equation 1 can be written for AsymRA-SVM as shown in equation below:
AsymRA-SVM enables the target task model to learn how important each signal from auxiliary tasks is by minimizing $|w_t - \sum_a \tau_a^p f_a^p(x_i) - \tau_a^n f_a^n(x_i)|$ and learning two separate weights for each auxiliary task.

\[
\min_{v_i, \xi_i, \tau} \sum_i \xi_i + C_1|v_i|^2 + C_2|\tau|^2
\]
\[
s.t. \quad y_i \sum_{a \in aux(t)} \tau_a^p f_a^p(x_i) + \tau_a^n f_a^n(x_i) + y_i v_i^T x_i \geq 1 - \xi_i, \quad i = 1, \ldots, N, \quad \xi_i \geq 0
\]  

### Experiments

We conducted our experiments on 22046 ICU patient admissions from MetaVision subset of MIMIC-III dataset (Johnson et al. 2016). MIMIC III provides patient diagnosis using International Classification of Diseases (ICD-9) (Slee 1978) codes. Therefore, we rely on ICD-9 hierarchy to obtain diagnostic tasks and their hierarchical structure. We obtained categorical ground truth labels by applying a logical OR operation between all its children. Finally, we omitted any diagnostic code with less than 30 positive samples (imbalance ratio of 0.001) while keeping 2019 diagnostic codes as learning tasks.

The problem of learning a dense representation of patient EHR data as $X \in R^D$ has been studied in past (Miotto et al. 2016; Hauskrecht et al. 2016). In this paper we followed the method proposed in the original HA-MTL paper (Malakouti and Hauskrecht 2019a). We used Latent Semantic Indexing (LSI) method which uses singular value decomposition (SVD) to learn a lower dimensional representation of the admission-event matrix. In order to create admission-event matrix to be used by SVD, we converted patient’s EHR data to a set of meaningful binary events by converting medication and procedure orders to indicators events. Laboratory results and physiological measurements with numerical values were converted to Normal and Abnormal Low or High events based on their standard normal ranges. Finally, Discrete valued measurements and pain level assessments were also converted to specific events matching each unique value.

After the conversion, our new EHR events data consisted of 4826 clinical events. This includes 2420 for medication orders, 116 for procedure orders, 2012 for laboratory results and 278 for physiological and pain assessment measurements. Finally, we created admission-event matrix by obtaining a BoW representation of patient event data with normalized frequencies.

We evaluate our method by comparing the performance of AsymHA-MTL to three baselines including random guessing model, individually trained SVM models and the original HA-MTL algorithm. We used Area Under Receiver Operating Curve (AUROC) and F1 score to provide quantitative comparison of the methods over a random stratified (70%-30%) split of data to train and test set. Finally, we used random sub-sampling to generate 10 different 75%/25% train/validation splits from the train set for hyper parameters optimization.

Table 1 shows the average AUROC and F1 for all 2019 diagnostic tasks. AsymHA-MTL method is outperforming the baselines and symmetric HA-MTL method. However as discussed in (Malakouti and Hauskrecht 2019a) we expect the majority of improvements to happen on lower level child diagnosis. Therefore, in Table 2 we have provided results for parts of two sub branches of ICD-9 hierarchy for Fracture of ribs and Diabetes. Our results show that considerable improvements has been gained by both HA-MTL and AsymHA-MTL while AsymHA-MTL is outperforming others. Similar trends are visible across different sub branches of the hierarchy.

Table 3 shows the improvements (AUROC) of models across different ranges of task priors or $P(y_i = 1)$. AsymHA-MTL is outperforming HA-MTL across different ranges of tasks priors while both methods have higher gains in tasks with fewer number of positive samples.

Despite the improvements of HA-MTL and AsymHA-MTL, one negative observation is that both HA-MTL and AsymHA-MTL is that in many case RASVM methods fail to prevent negative transfer from auxiliary tasks. This is more common in tasks with very high imbalance ratio (near 0.001) and small number of positive samples. Analysis of tasks results suggests that this is because RA-SM sometimes fails to prevent negative transfer by failing to choose right values of $\gamma$.

Figure 1 depicts the distribution of $\tau_{p_a}$ (impact of positive signals) and $\tau_{n_a}$ (impact of negative signals) in a top-down transfer of model parameters. The contrast between the distribution of positive and negative signals show that models are more likely to learn a higher impact for $f_a^n$ when

<table>
<thead>
<tr>
<th>Method Name</th>
<th>AUROC</th>
<th>F1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Random</td>
<td>0.5</td>
<td>0.0247</td>
</tr>
<tr>
<td>SVM</td>
<td>0.764</td>
<td>0.0755</td>
</tr>
<tr>
<td>HA-MTLtd</td>
<td>0.770</td>
<td>0.110</td>
</tr>
<tr>
<td>AsymHA-MTLtd</td>
<td>0.778</td>
<td>0.135</td>
</tr>
</tbody>
</table>

Table 1: Average performance for all diagnostic tasks
Table 2: Comparison of methods for example branches of ICD9

<table>
<thead>
<tr>
<th>Diagnostic Task Name</th>
<th>SVM AUROC</th>
<th>HA-MTL AUROC</th>
<th>AsymmmHA-MTL AUROC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diabetes mellitus</td>
<td>0.866</td>
<td>0.863</td>
<td>0.864</td>
</tr>
<tr>
<td>Diabetes mellitus without mention of complication</td>
<td>0.714</td>
<td>0.718</td>
<td>0.773</td>
</tr>
<tr>
<td>Diabetes mellitus without mention of complication, type II</td>
<td>0.689</td>
<td>0.68</td>
<td>0.757</td>
</tr>
<tr>
<td>Diabetes with hyperosmolarity</td>
<td>0.774</td>
<td><strong>0.863</strong></td>
<td>0.858</td>
</tr>
<tr>
<td>Diabetes with renal manifestations, type II</td>
<td>0.805</td>
<td>0.823</td>
<td>0.852</td>
</tr>
<tr>
<td>Fracture of rib(s) sternum larynx and trachea</td>
<td>0.914</td>
<td>0.912</td>
<td>0.919</td>
</tr>
<tr>
<td>Closed fracture of rib(s)</td>
<td>0.90</td>
<td>0.911</td>
<td>0.915</td>
</tr>
<tr>
<td>Closed fracture of multiple ribs, unspecified</td>
<td>0.690</td>
<td>0.764</td>
<td><strong>0.833</strong></td>
</tr>
</tbody>
</table>

Table 3: Average model improvements (AUROC) for diagnostic tasks within different ranges of prior for positive class

<table>
<thead>
<tr>
<th>Average model improvements</th>
<th>0 - 0.0016</th>
<th>0.0016 - 0.003</th>
<th>0.003 - 0.01</th>
<th>0.01 - 0.05</th>
<th>0.05 - 0.1</th>
<th>0.1 - 0.5</th>
<th>0.5 - 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of tasks</td>
<td>91</td>
<td>467</td>
<td>763</td>
<td>495</td>
<td>95</td>
<td>100</td>
<td>8</td>
</tr>
<tr>
<td>AsymmmHA-MTL</td>
<td><strong>0.0252</strong></td>
<td>0.0158</td>
<td><strong>0.0092</strong></td>
<td>0.0051</td>
<td>0.0001</td>
<td>-0.0003</td>
<td>0.0002</td>
</tr>
<tr>
<td>HA-MTL</td>
<td>0.0180</td>
<td>0.0095</td>
<td>0.0055</td>
<td>0.0030</td>
<td>-0.0011</td>
<td>-0.0018</td>
<td>0.0001</td>
</tr>
</tbody>
</table>

α is a parent of target task. This agrees with our hypothesis discussed in section that negative signals from parent diagnostic tasks are more likely to translate to a negative score in the child diagnostic model.

Figure 1: Distribution of \( \tau_p \) and \( \tau_\alpha \) values in the top-down transfer of model parameters

**Conclusion**

In this paper we argued that usefulness and impact of related tasks in hierarchical multi-task learning problems can depend not only to the tasks but also on the classes of samples. For example in the top-down transfer of parameters high negative scores of parent models are more likely to translate to negative scores of lower child models as negative labels are passed from a parent to child while this is not necessary true for positive labels. Therefore, we proposed an asymmetric hierarchical adaptive multi-task learning method that allows models to simultaneously learn model parameters and importance of positive and negative scores of auxiliary tasks independently. Our results show that during a top-down model adaptation phase our model is able to improve model performances compared to symmetric version of the algorithm and baseline SVM models.

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