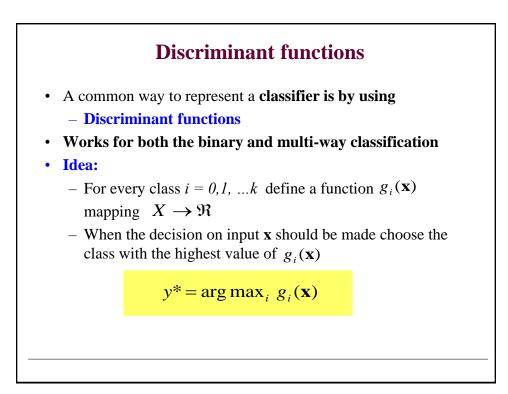
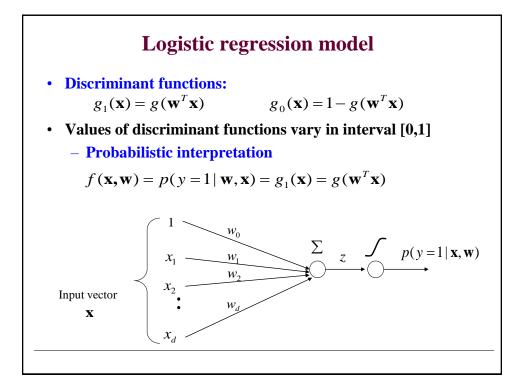
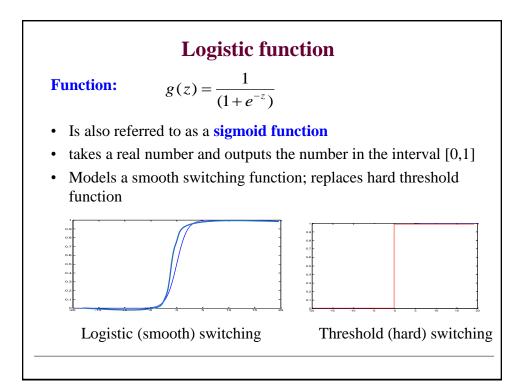
#### CS 2750 Machine Learning Lecture 10

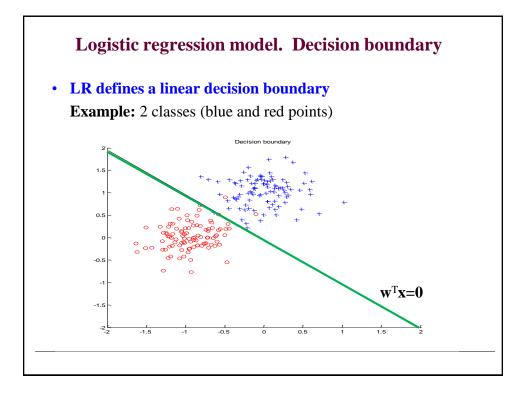
# Linear models for classification

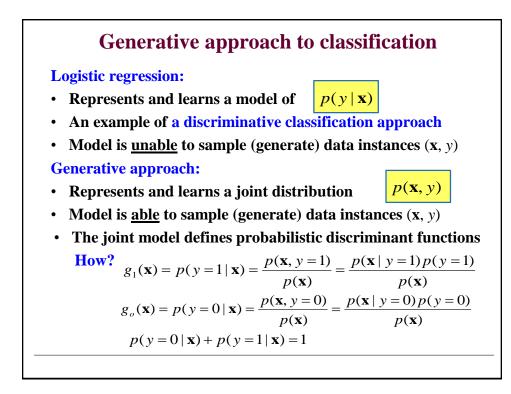
Milos Hauskrecht <u>milos@cs.pitt.edu</u> 5329 Sennott Square

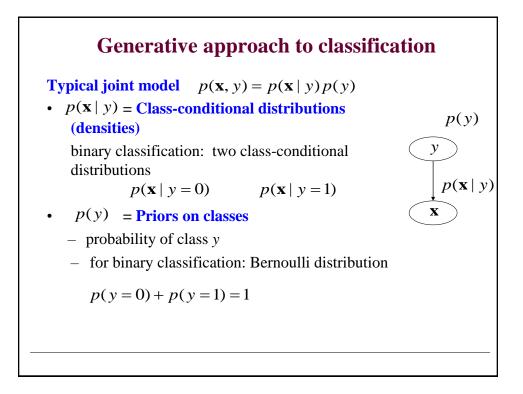


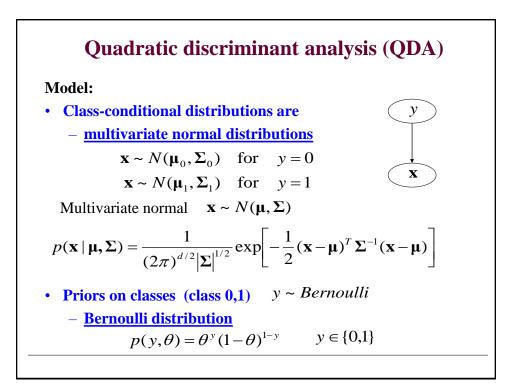


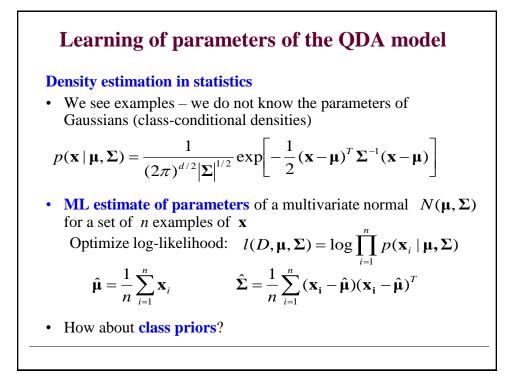


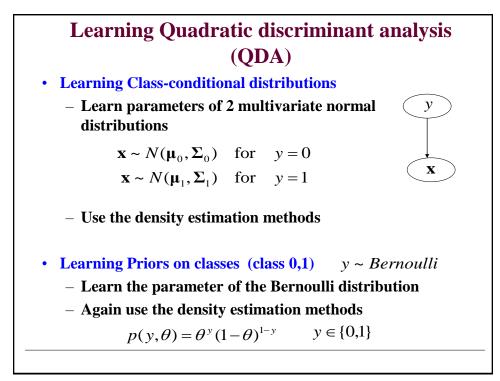


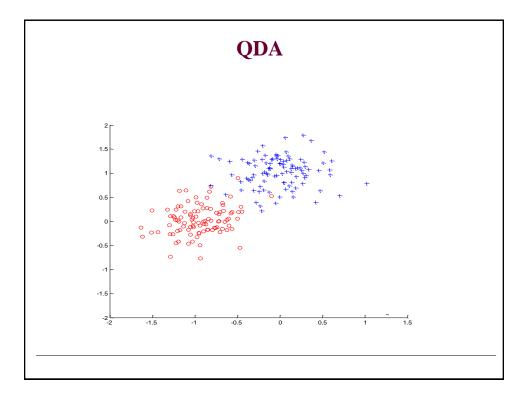


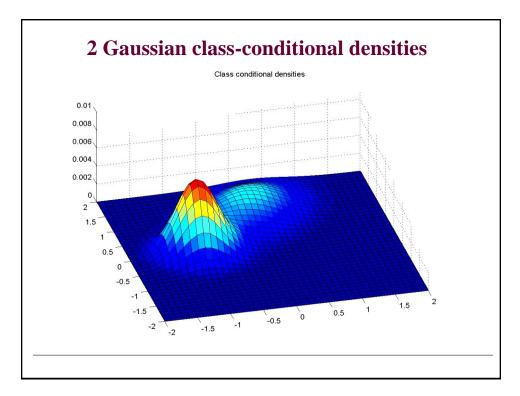


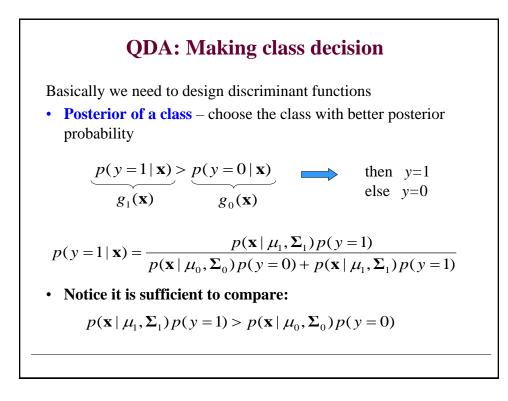


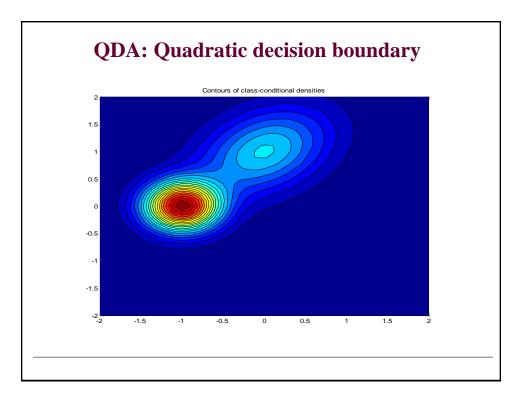


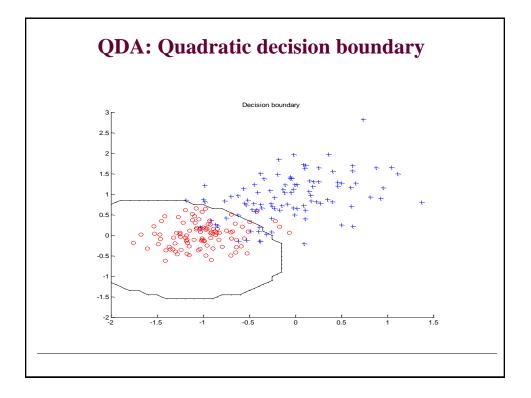


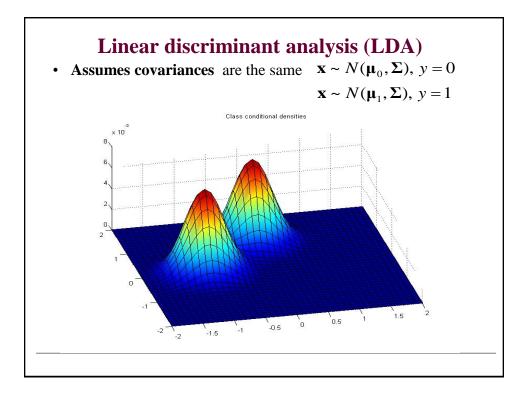


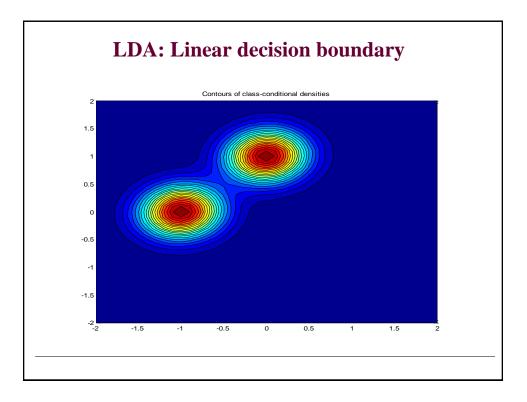


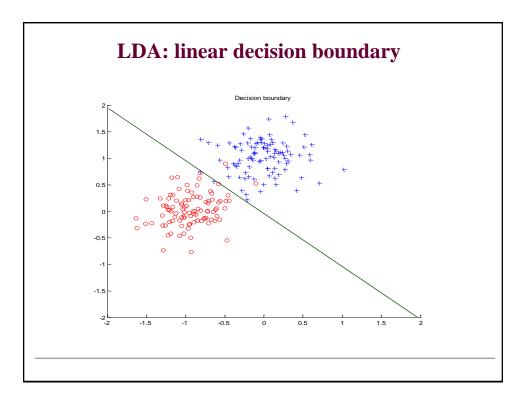


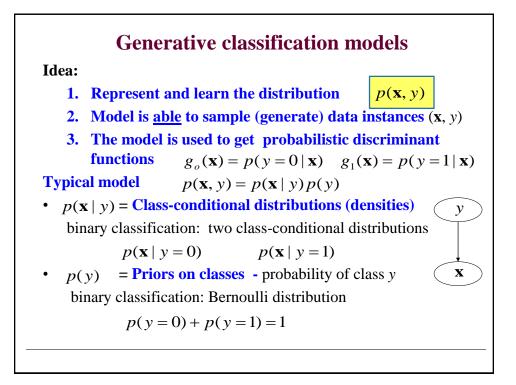


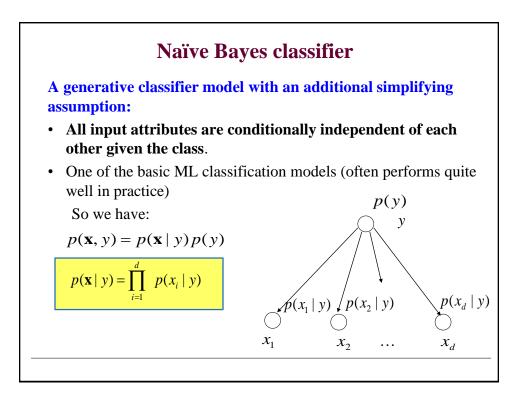












### Learning parameters of the model

Much simpler density estimation problems

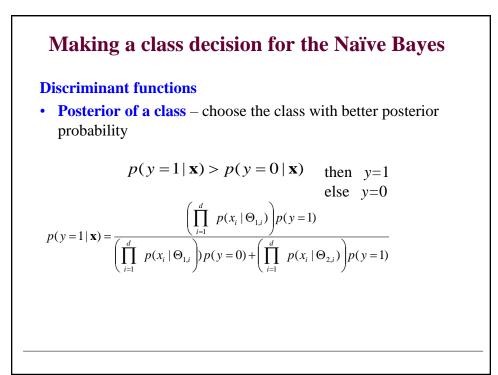
• We need to learn:

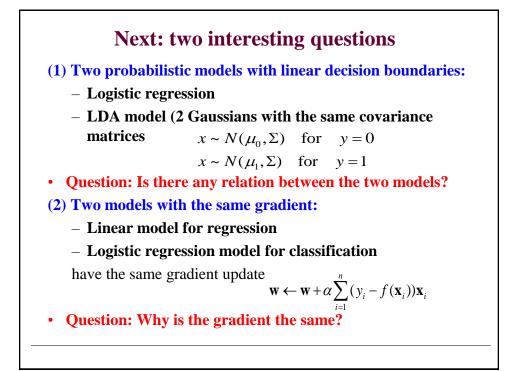
 $p(\mathbf{x} | y = 0)$  and  $p(\mathbf{x} | y = 1)$  and p(y)

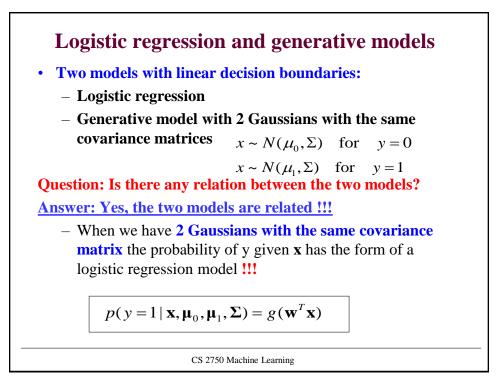
• Because of the assumption of the conditional independence we need to learn:

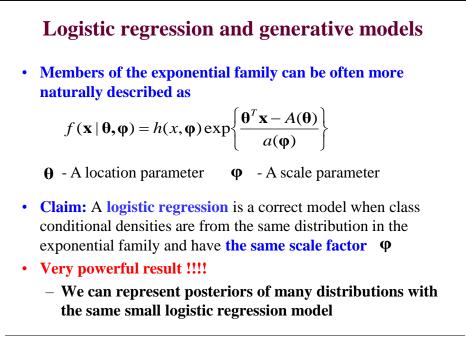
for every input variable i:  $p(x_i | y = 0)$  and  $p(x_i | y = 1)$ 

- Much easier if the number of input attributes is large
- Also, the model gives us flexibility to represent input attributes of different forms !!!
- E.g. one attribute can be modeled using the Bernoulli, the other using Gaussian density, or a Poisson distribution

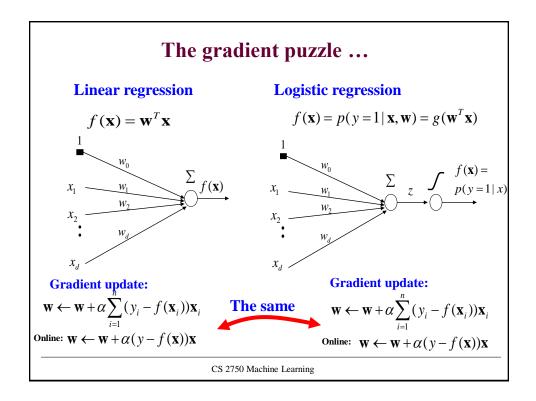


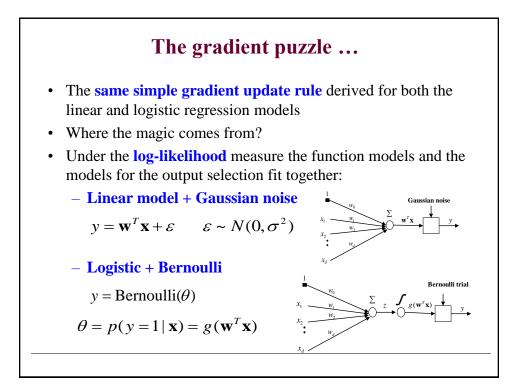


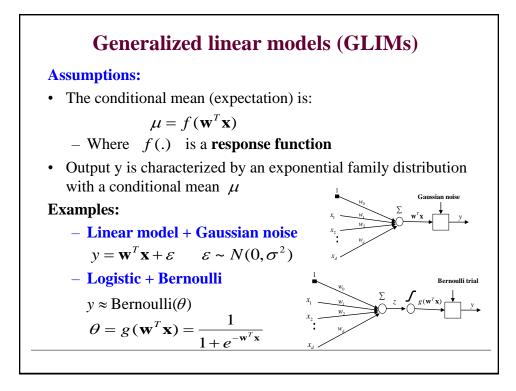


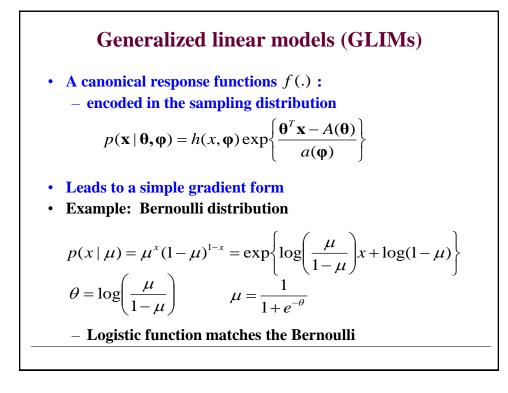


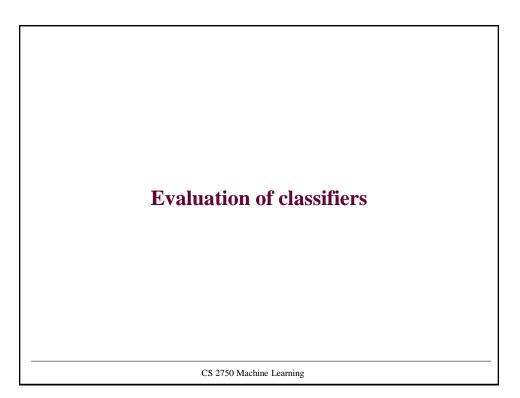
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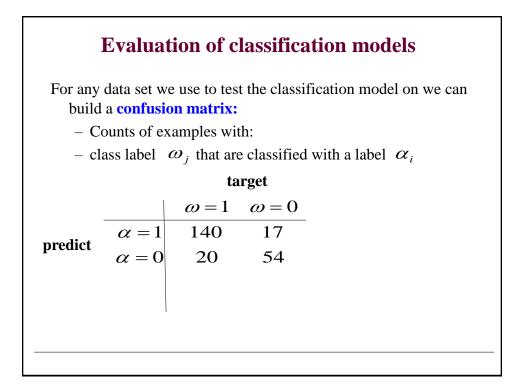
## **Classification model learning**

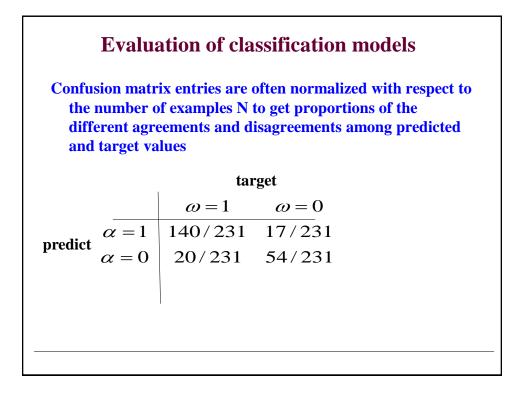
#### Learning:

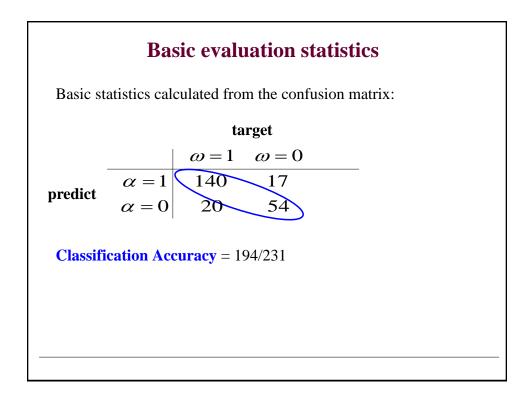
- Many different ways and objective criteria used to learn the classification models. Examples:
  - Mean squared errors to learn the discriminant functions
  - Negative log likelihood (logistic regression)

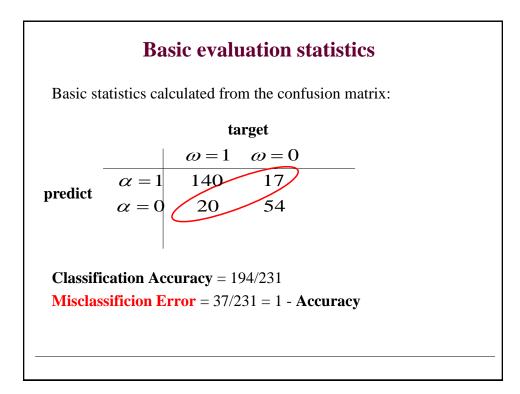
#### **Evaluation:**

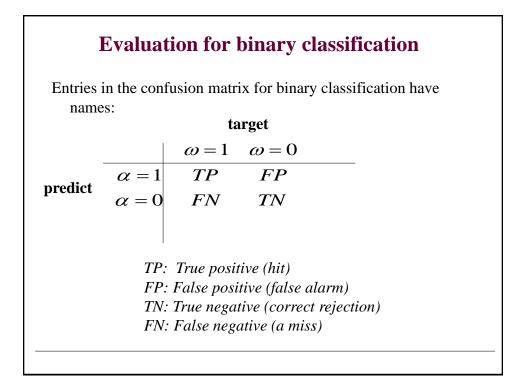
- One possibility: Use the same error criteria as used during the learning (apply to train & test data). Problems:
  - May work for discriminative models
  - Harder to interpret for humans.
- **Question:** how to more naturally evaluate the classifier performance?

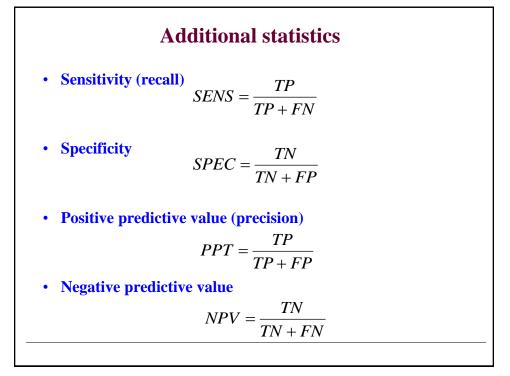


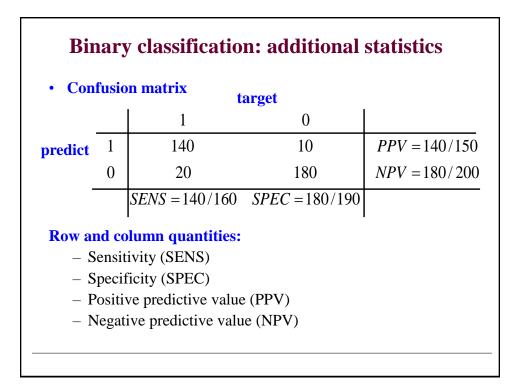


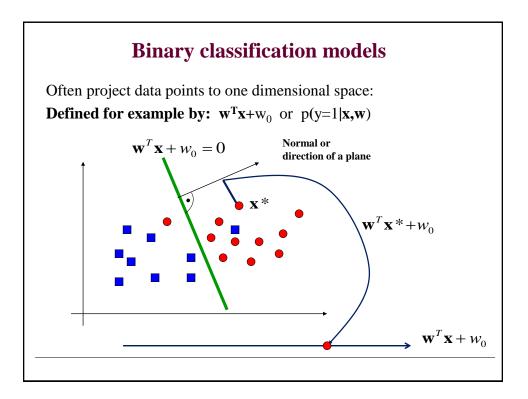


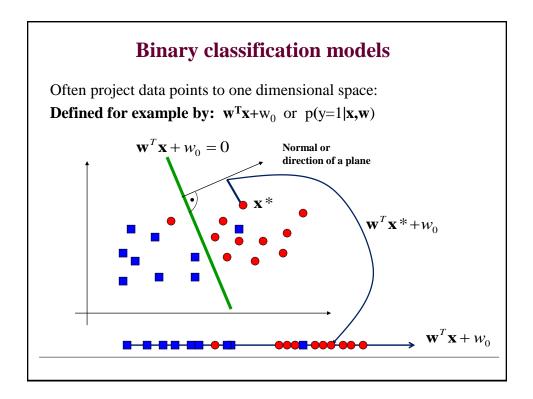


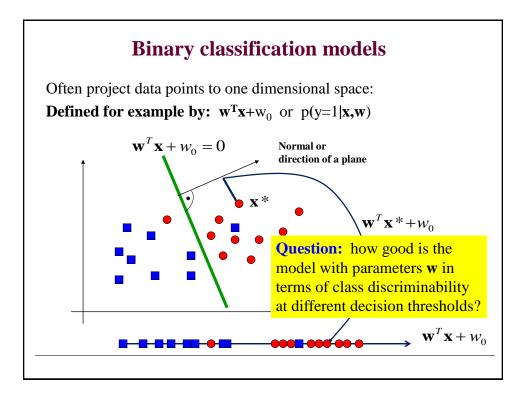


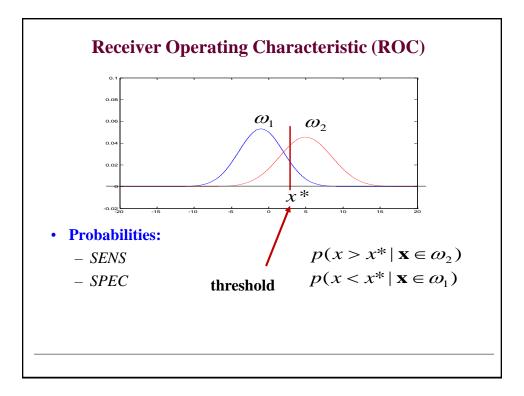


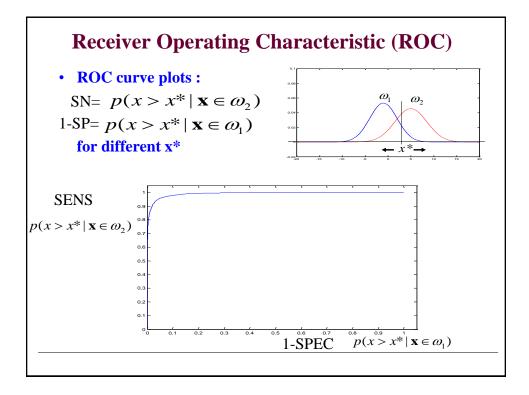


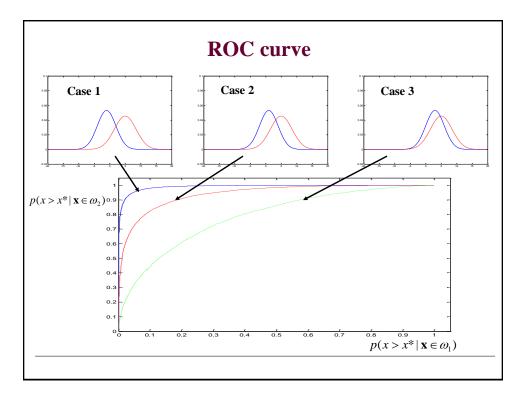












## **Receiver operating characteristic**

- ROC
  - shows the discriminability between the two classes under different thresholds representing different decision biases
- Decision bias
  - can be changed using the different loss function
- Quality of a classification model:
  - Area under the ROC
  - Best value 1, worst (no discriminability): 0.5